



Synthesis, characterization, and evaluations of Cu-doped TiO₂/Bi₂O₃ nanocomposite for Direct red 16 azo dye decolorization under visible light irradiation

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ABSTRACT

In this study, a statistical analysis based on the response surface methodology (RSM) was employed to investigate the individual and interaction effects of critical operating and dopant concentration on photocatalytic decolorization of Direct Red 16 under visible-light by Cu-doped TiO₂/Bi₂O₃. Cu-doped TiO₂/Bi₂O₃ is a visible-light-driven nano-catalyst which was synthesized by applying the sol-gel technology for the removal of Direct Red 16. The studied operating parameters include the Bi₂O₃/TiO₂ ratio, Cu/Ti ratio, and reaction time. The statistics-based experimental design and RSM were utilized to find a quadratic model as a functional relationship between the decolorization efficiency and the three operating parameters. Initially, the optimum ranges of Cu/Ti and Bi₂O₃/TiO₂ compounds on the removal of the dye pollution were experimentally obtained, which is 2, 4, and 6 wt.% for Cu/Ti ratio and 8, 9, and 10 wt.% for the Bi₂O₃/TiO₂ ratio. Then, a set of TiO₂/Bi₂O₃-Cu nano-catalysts with various ingredients was synthesized based on the RSM method, and field emission scanning electron microscopy, diffuse reflection spectroscopy, and X-ray diffraction were performed. The performed experiments on the removal of the pollution showed that the produced nano-catalyst with 6 wt.% Cu/Ti ratio, 8 wt.% Bi₂O₃/TiO₂ ratio and reaction time of 3 h had the maximum removal efficiency of 99%. The regression analysis with an *R*² value of 0.99 showed the right consistency between the model prediction and experimental data of the decolorization efficiency. Using the quadratic model of RSM, the optimum contents of the nano-catalyst was 5.9 wt.% Cu/Ti ratio and 8.0 wt.% Bi₂O₃/TiO₂ ratio with a removal efficiency of 99.4% while the efficiency of the experiments was 99.0% ± 0.7% by application of this synthesized nano-catalyst.

Keywords: Azo dye decolorization; TiO₂/Bi₂O₃-Cu nano-catalysts; RSM; Visible light

1. Introduction

Today, the presence of dyes and organic pollutants of industries in our natural water and wastewater constitutes a significant problem [1]. Textile wastewater containing dyes, detergents, acids, organic compounds, and heavy

metals is a global environmental problem [2–4]. Due to their intense color, the paints represent a major ecological problem, and their treatment is a necessary step before discharging them into the aquatic environment, and physical and chemical methods are currently being used to eliminate them. However, such methods do not destroy the pollutants

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but only transfer them from the liquid to the solid phase, and their reconstruction requires investment [5]. Azo dyes, known as p-bond nitrogen, are the most widely used synthetic dyes and are generally critical industrial wastewaters. Due to their slow degradation and toxicity, these dyes are classified as hazardous substances [6]. One of the dyes used in the textile industry is Direct red 16. This dye is azo and therefore pollutes the environment [7,8].

Photocatalytic and advanced oxidation processes (AOPs) play an essential role in the drinking water and wastewater treatment industry. Photocatalytic processes break down the organic compounds into non-toxic minerals [3,9]. Soluble organic dyes are an extraordinary group of industrial wastewater pollutants that must be removed before discharging the treated wastewater to the environment or its reuse [10]. Various semiconductors such as TiO_2 , Fe_2O_3 , ZnO , CdS , and WO_3 had been used in photocatalytic processes [11]. As a consequence of TiO_2 properties such as high photocatalytic value, non-toxicity, sustainability, and reasonable price, it becomes the most popular photocatalyst. TiO_2 is the most popular photocatalyst because of its unique properties such as high photocatalytic value, non-toxicity, sustainability, and reasonable price [9,12,13]. There are many research studies on the application of TiO_2 under ultraviolet (UV) radiations in photocatalytic processes for the decolorization of azo dyes [14].

In a photocatalytic process, radiation of the light to the nano-catalyst results in the excitation of electrons and the formation of holes [15]. The photocatalytic process depends on conducting a photochemical reaction on the semiconductor surface, which has two primary reactions. The first one includes oxidation from the positive hole, and the second one is a reduction from the negative electron [16].

The goal of researchers is the improvement of efficiency and selectivity of nano-catalyst TiO_2 for various applications. TiO_2 is among the most widely-used materials for the photodegradation process [16], but the performance of TiO_2 for the visible application is greatly restricted because of its wide band gap, which brings some drawbacks [17]. TiO_2 has a wide band gap that is activated by ultraviolet radiation with $\lambda < 400 \text{ nm}$ [18,19]. Doping of TiO_2 with a metal/non-metal element reduces the TiO_2 band gap [20]. Metals such as Cr, Mn, Fe, Ag, V, and Cu and non-metals such as C, N, S, Si, and F can be used for doping [21–23].

Also, the low quantum yield rate of visible light activation is another major drawback [17]. To overcome this shortcoming, TiO_2 can be coupled with narrow band gap semiconductors such as Bi_2WO_6 , WO_3 , ZnO , FeTiO_3 , SiO_2 ,

CdS , Bi_2O_3 , and Al_2O_3 [24]. Bi_2O_3 with a band gap of 2.8 eV is widely applied as a visible driven photocatalyst. However, it has low quantum efficiency [17,25]. The $\text{TiO}_2/\text{Bi}_2\text{O}_3$ heterojunction not only decreases the band gap of TiO_2 into the visible region but also facilitates the separation of charge carriers during the photodegradation process [17,25,26].

In this work, the focus is given on modified TiO_2 and a set of nano-catalysts was synthesized by doping of Cu and coupling Bi_2O_3 with TiO_2 with various loadings that were optimized based on the RSM. The synthesized nano-catalysts were used to decolorize Direct Red 16 dye. Direct Red 16 decolorization was also modeled and optimized using the central composite design (CCD).

2. Experimental and methods

2.1. Material

Titanium tetraisopropoxide (TTIP) and isopropanol were used for the synthesis of the catalysts in the current study. To modify TiO_2 , $\text{Bi}(\text{NO}_3)_3 \cdot 5\text{H}_2\text{O}$, and $\text{CuN}_2\text{O}_6 \cdot 3\text{H}_2\text{O}$ were used as the precursors of Cu and Bi, respectively. During the preparation of the $\text{TiO}_2/\text{Bi}_2\text{O}_3$ -Cu solution, the solution pH was adjusted by the addition of HCl and NaOH. A list of materials used in the experimental study is presented in Table 1.

2.2. Synthesis of $\text{TiO}_2/\text{Bi}_2\text{O}_3$ -Cu by the sol-gel technology

In order to control the process of synthesizing nanocrystalline TiO_2 powder, hydrolysis of TTIP in the mixture of isopropanol and deionized water was used. Achieve to reduced rate of the hydrolysis process results in the synthesis of TiO_2 powders revealing favorable optical transparency, porosity, and thermal stability [27,28].

Grzeszkowiak et al. [28] reported that titania synthesized via hydrolysis of titanium (IV) isopropoxide (TTIP) and calcined at 400°C in air for a period of 3 h. It consists of just anatase phase and the material did not contain carbon originating from the solvent or from the additives used to stimulate pH. TiO_2 thin films with different titanium isopropoxide (TTIP): acetylacetonone (AcacH) molar ratios in solution were prepared by the chemical spray pyrolysis method [29]. Titania (TiO_2) photocatalysts are produced using the hydrolysis of TTIP at 100°C – 600°C [30].

The first solution was prepared by dissolving 0.024 g of copper nitrate nanohydrate in 5 mL isopropanol, and the mixture was stirred for 1 h. The second solution was resulted from solving 0.098 g of bismuth nitrate nanohydrate

Table 1
List of used chemicals

Materials	Chemical formula	Purity (wt.%)	Manufactured company
Titanium tetraisopropoxide (TTIP)	$\text{C}_{12}\text{H}_{28}\text{O}_4\text{Ti}$	99.999	Merck KgaA, Darmstadt, Germany
Isopropanol	$\text{C}_3\text{H}_7\text{OH}$	99.5	Sigma-Aldrich
Copper nitrate nanohydrate	$\text{Cu}(\text{NO}_3)_2 \cdot 3\text{H}_2\text{O}$	99.99	Merck KgaA, Darmstadt, Germany
Bismuth nitrate nanohydrate	$\text{Bi}(\text{NO}_3)_3 \cdot 5\text{H}_2\text{O}$	99.99	Merck KgaA, Darmstadt, Germany
Hydrochloric acid	HCl	37	Merck KgaA, Darmstadt, Germany
Direct Red 16	$\text{C}_{26}\text{H}_{17}\text{N}_5\text{Na}_2\text{O}_8\text{S}_2$	100	Ningbo

in 10 mL isopropanol, and the mixture was stirred for 12 h. For adjusting the pH between 2 and 3, three drops of HCl were added to the solution [31]. The third solution, for the synthesis of Cu-doped TiO_2 nano-catalyst, solution number of 1 was mixed with 3 mL TTIP and 35 mL isopropanol (Fig. 1a). The solution pH was kept within the range of 2–3 by HCl. The prepared solution was ultrasonicated for 20 min and stirred continuously for 12 h. For the synthesis of $\text{TiO}_2/\text{Bi}_2\text{O}_3$ -Cu nano-catalyst, the second solution was added to the third solution, and the prepared solution was ultrasonicated for 20 min and stirred continuously for 12 h (Fig. 1b). The nano-catalysts were placed in an oven at 60°C for 12 h and then were calcined by leaving it in a furnace at 500°C for 2 h.

2.3. Photoreactor

The photocatalytic experiments were conducted in a batch glass cylindrical reactor with an inner diameter of 70 mm, the height of 100 mm, and liquid hold up to 100 mL. The reactor was equipped with an LED light source 12V/30 W and a magnetic stirrer for homogenizing the mixture during the experiment.

2.4. Nano-catalyst characterization

The X-ray diffraction (XRD) pattern of the synthesized nano-catalyst was recorded by a Philips (X'pert Pro MPD, Almelo, Netherlands) X-ray diffractometer with Ni-filtered Cu K_α radiation (wavelength 1.5406 Å) equipped with a Ni filter. Diffuse reflection spectroscopy UV-Vis (DRS) was used to determine the band gap energy of the nano-catalyst and to investigate the effect of type and amount of Cu and Bi_2O_3 on the diffuse reflection spectroscopy UV-Vis.

Also, the morphology of the surface structure of the synthesized nanoparticles was investigated by a field emission scanning electron microscopy (TESCAN FE-SEM MIRA3, Kohoutovice, Czech Republic).

2.5. Procedure and analysis

The decolorization of Direct Red 16 from aqueous solution was investigated under the irradiation of visible light. In order to measure the photocatalytic activity, experiments were done in a batch reactor containing the 100 mL dye solution with a concentration of 25 mg/L. After the addition of 1 g/L of the nano-catalyst, the solution was stirred at a mixing rate of 600 rpm. Initially, the solution was stirred in the dark for 30 min to have a complete equilibrium between solution and nano-catalyst. Then, the solution was mixed for 3 h under the radiation of visible light. All of the experiments were performed at a pH of 6.8. For analyzing tests, 5 mL of the solution samples were centrifuged with a speed of 5,000 rpm for 15 min to separate the nano-catalyst particles. A UV-Vis spectrophotometer at a wavelength of 526 nm was used for measuring the dye concentration. The photocatalytic decolorization efficiency was calculated according to Eq. (1).

$$\text{Removal}(\%) = \left(1 - \frac{C_t}{C_0}\right) \times 100 \quad (1)$$

where C_0 and C_t are the initial and the final concentrations of dye in the solution, respectively.

2.6. Experimental design and statistical analysis

RSM was employed to evaluate the effect of two-component loadings ($\text{Bi}_2\text{O}_3/\text{TiO}_2$ ratio (A , wt.%), Cu/Ti ratio (B , wt.%)) and operational parameters (time (C , min)) on the Direct Red 16 decolorization under visible light illumination. The three parameters (A , B , C) were chosen as independent variables, while the decolorization efficiency of Direct red 16 was the output response. The experimental ranges and the levels of the independent variables for Direct red 16 photocatalytic decolorization are shown in Table 2. The preliminary screening experiments were used to obtain effective

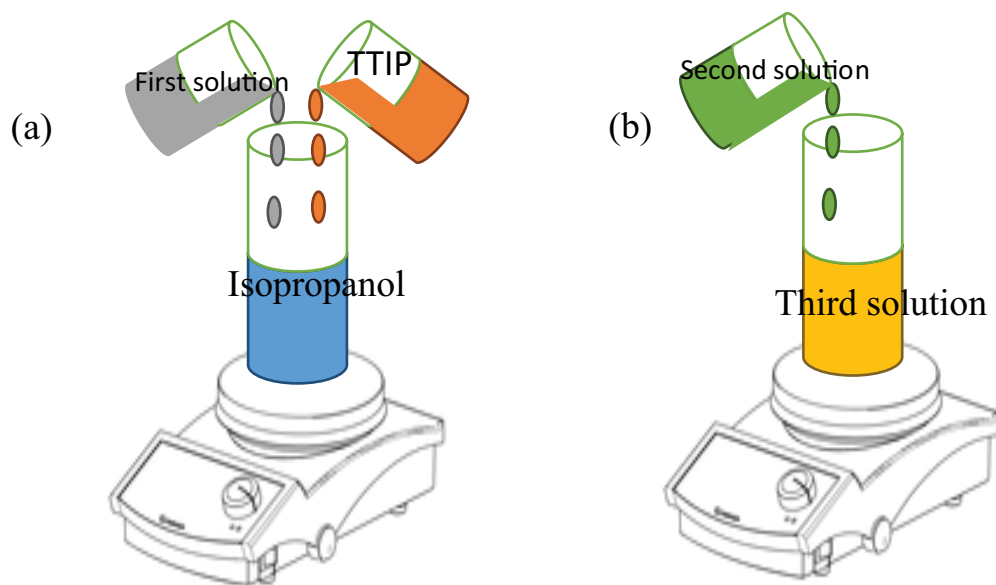


Fig. 1. Synthesis nanocatalyst (a) Cu-TiO_2 and (b) $\text{TiO}_2/\text{Bi}_2\text{O}_3$ -Cu.

Bi₂O₃/TiO₂ and Cu/Ti concentrations values. Based on the results of these experiments that are presented in Fig. 2, the best-produced nano-catalyst for removal of the dye contained 9 wt.% Bi₂O₃/TiO₂ and 4 wt.% Cu/Ti. According to the preliminary experiments, the values of 2, 4, and 6 wt.% for Cu/Ti ratio and the values of 8, 9, and 10 wt.% for the Bi₂O₃/TiO₂ ratio were selected for further experiments. The RSM based on the central composite experimental design (CCD), which is one of the most usual methods of using a response surface methodological approach, was utilized to evaluate the combined effects of the three independent variables using twenty experiment data [25].

Moreover, a quadratic equation was obtained to relate the response variable to the three independent variables, as follows:

$$Y = a_{00} + a_{01}A + a_{02}B + a_{03}C + a_{12}AB + a_{13}AC + a_{23}BC + a_{11}A^2 + a_{22}B^2 + a_{33}C^2 \quad (2)$$

Where Y (%) is the predicted response (decolorization efficiency of Direct red 16), *a_{ij}* are the coefficients and A, B, and C are the values of independent variables (Bi₂O₃/TiO₂ ratio, Cu/Ti ratio, and time, respectively). Decolorization conditions determined by the CCD method along with the predicted and experimental values of the response are presented in Table 3. Data were analyzed by the analysis of

variance (ANOVA), and the optimal values of the variables were obtained using the Design Expert software.

3. Results and discussion

3.1. X-ray diffraction

XRD patterns of the modified TiO₂ is shown in Fig. 3. The characteristic peaks can be well indexed to the anatase phase anatase TiO₂. The sharp and symmetrical diffraction peaks of pure synthesized TiO₂ show the high crystallinity of the studied sample. Based on the pattern of this figure, no diffraction peaks of Cu²⁺ are detected, which can be due to the low doping amount or excellent size of Cu²⁺ cation (radius of Cu²⁺ = 73 pm and Ti³⁺ = 88 pm [26]). Furthermore, as a result of the lack of Cu separation, clustering, or oxide formation complete dissolution of Cu²⁺ cations for the formation of Cu–O–Ti bonds occurred [18]. Besides, no visible diffraction peaks of Bi₂O₃ was observed in the XRD patterns for TiO₂/Bi₂O₃-Cu. That implies a perfect dispersion of the Bi₂O₃ particles. This issue has been reported by Kumar and Devi [19].

The average crystalline sizes can be calculated based on the anatase diffraction peaks using the Debye–Scherrer equation [32]:

$$D = \frac{k\lambda}{\beta \cos\theta} \quad (3)$$

where D is the crystalline size, λ stands for the wavelength of X-ray (nm), and k is considered to be 0.89, assuming that the particles are spherical. β is the full width in radius at half maximum (FWHM) of the highest peak (rad), and θ represents the Bragg angle of the highest peak. The results given in Table 4 show that a reduction in the crystallite size leads to

Table 2
Ranges and values of the variables for experimental design

Ranges and values	Variables	-1	0	+1
Bi ₂ O ₃ /TiO ₂ ratio (wt.%)	A	8	9	10
Cu/Ti ratio (wt.%)	B	2	4	6
Time (h)	C	1	2	3

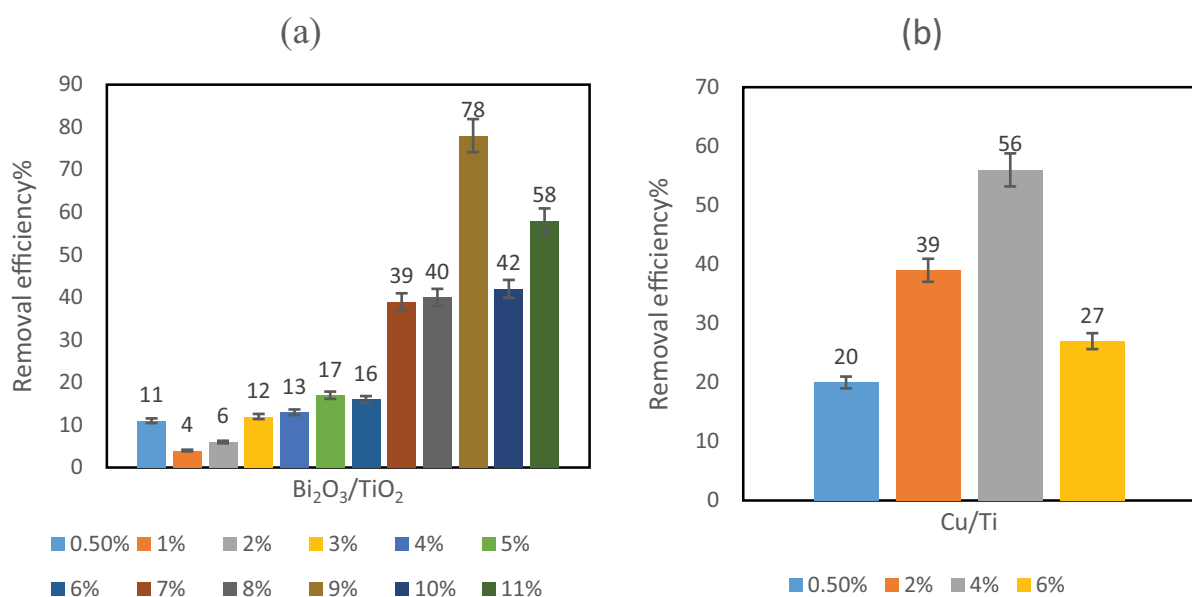


Fig. 2. Removal efficiency of the photocatalytic decolorization reaction: (a) pH = 6.8, [Bi₂O₃/TiO₂] = 1 g/L, C₀ = 25 mg/L reaction time = 3 h and (b) pH = 6.8, [TiO₂-Cu] = 1 g/L, C₀ = 25 mg/L, and reaction time = 3 h.

Table 3
Experimental design matrix and the value of responses based on the experiment runs

Run	Bi ₂ O ₃ /TiO ₂ ratio (wt.%)	Cu/Ti ratio (wt.%)	Time (h)	Actual decolorization efficiency (%)	Predicted decolorization efficiency (%)
1	9	4	2	65	65.6
2	10	4	2	67	66.2
3	9	4	1	44	44.3
4	8	6	3	99	99.5
5	8	6	1	56	55.6
6	9	4	2	64	65.6
7	9	4	2	66	65.6
8	10	2	3	97	97.7
9	10	6	3	59	59.6
10	8	4	2	64	64.9
11	10	6	1	21	21.2
12	9	4	3	88	85.8
13	9	2	2	53	52.6
14	9	6	2	59	57.1
15	8	2	1	23	22.9
16	8	2	3	45	45
17	9	4	2	67	65.6
18	9	4	2	64	65.6
19	10	2	1	51	50.9
20	9	4	2	66	65.6

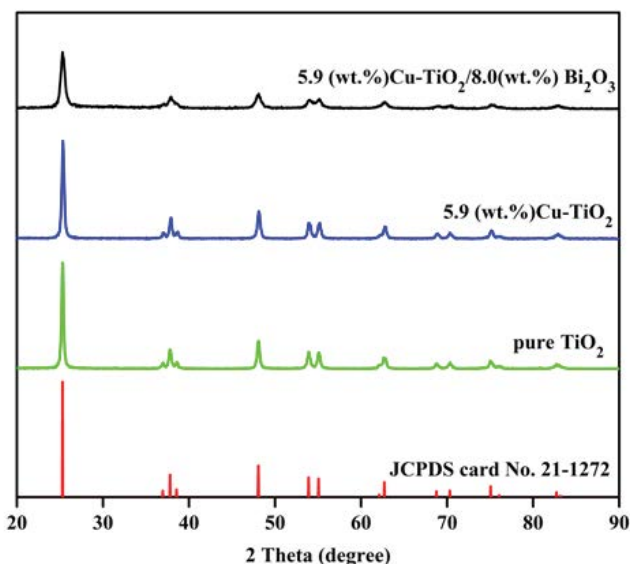


Fig. 3. XRD patterns of the modified TiO₂.

distortion in the lattice structure of the modified TiO₂ due to the modifying process.

3.2. UV-vis DRS

The band gap of the TiO₂ synthesized nanocatalyst was determined using the UV-Vis spectrum. The obtained

Table 4
Crystalline size for the modified TiO₂

Samples	Crystalline size (nm)
Pure synthesized TiO ₂	32.1
5.9 (wt.%) Cu-TiO ₂	26.8
5.9 (wt.%) Cu-TiO ₂ /8.0 (wt.%) Bi ₂ O ₃	17.7

absorption spectra are shown in Fig. 4. The pure TiO₂ absorption spectrum includes an absorption peak of about 360 nm, due to the transfer of electrons from the valence band to the conduction band. In the DRS spectrum of the nano-catalyst 5.9 (wt.%) Cu-TiO₂, the absorption peak was observed in the region of 420 nm, which is the result of the introduction of copper metals in the structure of TiO₂. This issue results in transferring of absorption from UV spectra to the visible one.

The band gap energy of the nanocatalyst 5.9 (wt.%) Cu-TiO₂/8.0 (wt.%) Bi₂O₃ was also represented in Fig. 4, which shows a broad absorption peak in the 460 nm region. By modifying TiO₂ with Bi₂O₃ semiconductor, its absorption was increased from 420 to 460 nm, indicating a decrease in the band gap energy of the synthesized nanocatalyst. The bang gap energy values are also shown in Table 5.

3.3. Field emission scanning electron microscopy

The morphology of samples pure TiO₂, 5.9 (wt.%) Cu-TiO₂ and 5.9 (wt.%) Cu-TiO₂/8.0 (wt.%) Bi₂O₃ is shown

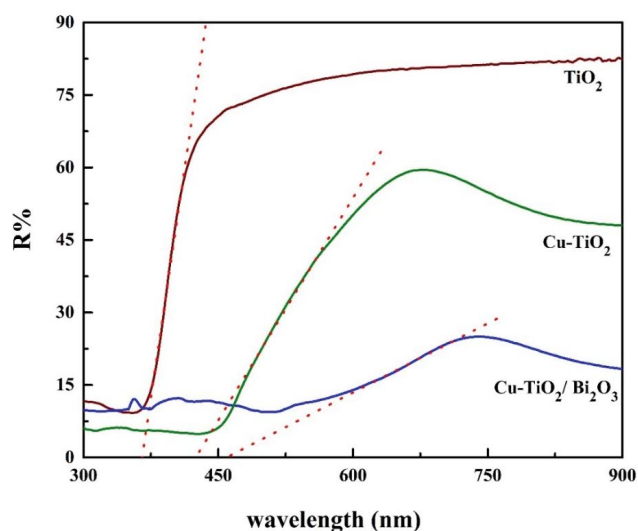


Fig. 4. DRS patterns of the modified nano-catalyst TiO_2 .

Table 5
Band gap energy of the modified nano-catalyst

Samples	Band gap energy (eV)
Pure synthesized TiO_2	3.4
5.9 (wt.%) Cu-TiO_2	2.9
5.9 (wt.%) $\text{Cu-TiO}_2/8.0$ (wt.%) Bi_2O_3	2.7

in Fig. 5. Reduction in the size of the particles results in higher uniformity, and the spherical structure of a modifying nanocatalyst. The particle size measured in the field emission scanning electron microscopy (FE-SEM) test is shown. The process of reducing the particle size remains the process of reducing particle size using the XRD test. As shown in Fig. 5, by modifying the nanocatalyst, the particle size was reduced, which increases the contact area.

3.4. Model fitting and statistical analysis

The gained experimental data were analyzed, and a quadratic model is proposed. ANOVA investigated variables impact, their interaction in experiments, and studying the significance of the model. ANOVA investigated the effect of variables and their interaction in experiments as well as studying the significance of the model. In this case, the quadratic model is selected, and its ANOVA analysis is shown in Table 6. The model p and F -values were used as a tool to check the relative significance of the variables. In general, coefficients with higher F -value and lower p -value indicate that their corresponding variables have more significance in comparison to other variables [33]. In this case, p -value higher than 0.05 shows that the parameter is ineffective on the model, and according to Table 6, the most significant p -value belongs to parameter A^2 and eliminating this parameter leads to a more appropriate model. As can be seen in Table 7, all p -value parameters are below 0.05, which indicates the effect of these parameters

in the model, and using these parameters, a suitable model for data analysis is obtained. Besides the very low model p -value, the model F -value of 880.27 also showed the adequacy of the model since it was much higher than the theoretical F -value. Also, a lack of fit F -value of 0.83 indicated good predictability of the model, which implied that lack of fit was not significant relative to the pure error.

Based on the Direct red 16 photocatalytic decolorization results, the following quadratic model was obtained:

$$(\text{Efficiency } \%)^{0.43} = -11.55724 + 1.53791 \times A + 4.78710 \times B + 0.018588 \times C - 0.43535 \times AB + 0.11776 \times AC + 0.038939 \times BC - 0.11217 \times B^2 - 0.098027 \times C^2 \quad (4)$$

The positive coefficients (A , B , C , AC , and BC) resulted in an increase in the decolorization efficiency, while negative coefficients (AB , B^2 , and C^2) affected the decolorization efficiency. The model adequacy was further checked using the diagnostic plots (Figs. 6 and 7). As can be seen in figures, the values of R^2 and Adj. R^2 were calculated as 0.998 and 0.997, respectively, implying that the experimental data were fitted very well by the proposed model. In addition to the correlation coefficient, the normal probability plot of the externally studentized residuals was also studied to evaluate the adequacy of the model Fig. 6. According to Fig. 6, the extra points fell near to the straight line, indicating that there was almost no severe departure of the assumptions underlying the analysis and also a good agreement between the actual and predicted values.

The plot of the externally studentized residuals vs. predicted responses is illustrated in Fig. 7. As shown in this figure, all design points of the experimental runs were randomly scattered within the constant range of residuals across the graph (± 4.00453), suggesting that the variance of the original observations is constant for all values of the response and the approximation of the fitted model to the response surface was quite acceptable and adequate [34].

3.5. Analysis of response surface

The effects of the operating and nano-catalyst parameters and their interaction effect on the decolorization efficiency of Direct Red 16 are graphically represented by three-dimensional RSM plots and two-dimensional contour plots in Fig. 8.

As shown in Fig. 8a, at low values of $\text{Bi}_2\text{O}_3/\text{TiO}_2$ ratio, efficiency is low unless Cu/Ti ratio values are high. In fact, at low values of $\text{Bi}_2\text{O}_3/\text{TiO}_2$ and Cu/Ti ratios, the nano-catalyst band gap energy is high, and the used light source cannot activate the nano-catalyst that results in low efficiency of the nano-catalyst. Furthermore, at lower values of Cu/Ti ratio, higher values of $\text{Bi}_2\text{O}_3/\text{TiO}_2$ ratio result in a reduction of the nano-catalyst bandgap energy. This issue is due to the occurrence of the recombination phenomenon in the nano-catalyst by increasing doping values to an optimum level [35]. On the other hand, for higher values of both $\text{Bi}_2\text{O}_3/\text{TiO}_2$ and Cu/Ti ratios, the efficiency decreases. As shown in Fig. 8b, increasing as expected by processing time, the decolorization efficiency is enhanced. The photocatalytic process is a time-consuming process. In the current study, modified nano-catalyst will examine

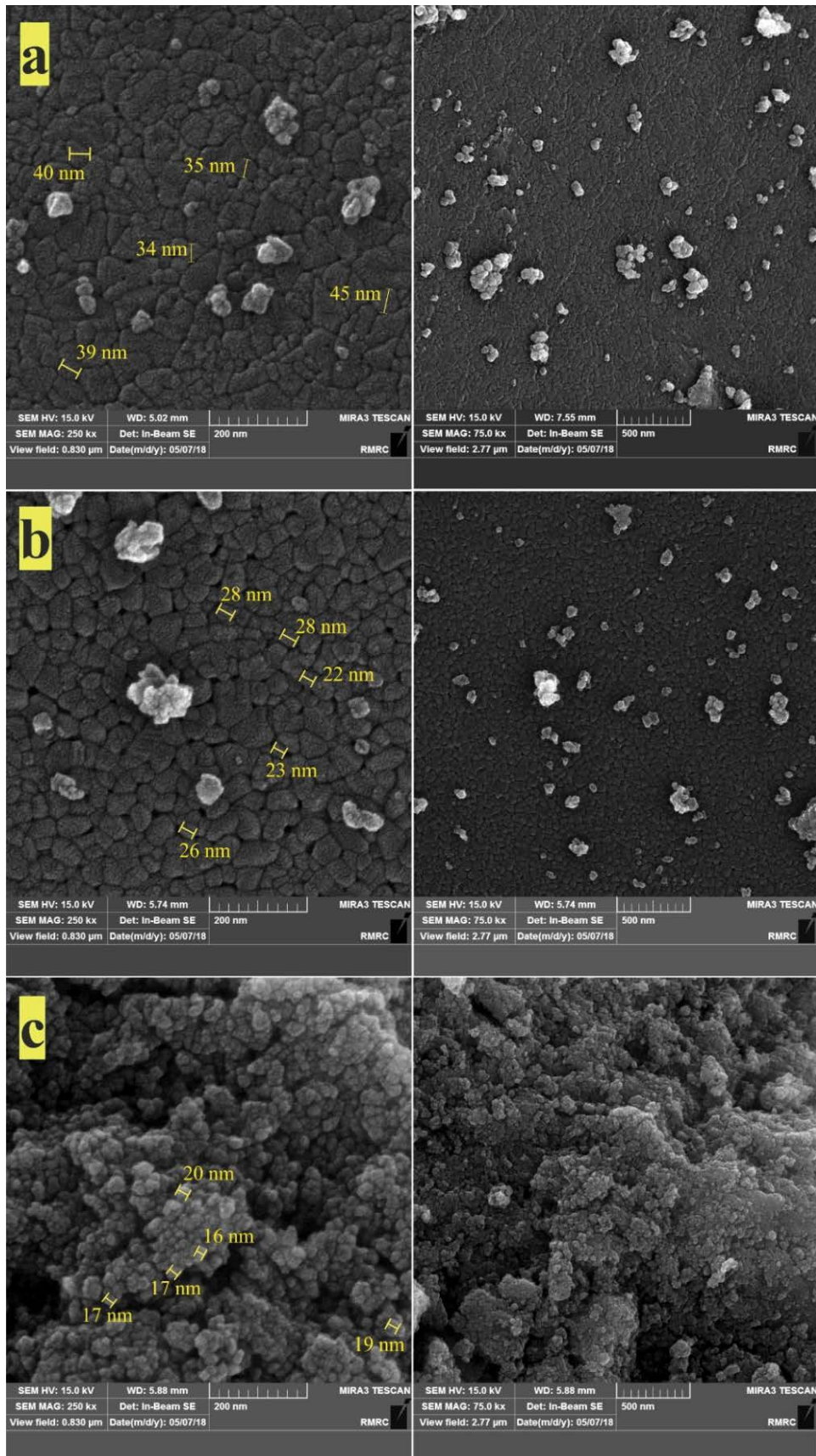


Fig. 5. FE-SEM of samples (a) pure TiO_2 , (b) 5.9 (wt.%) Cu-TiO_2 , and (c) 5.9 (wt.%) $\text{Cu-TiO}_2/8.0$ (wt.%) Bi_2O_3 .

Table 6
Power transform ANOVA results

Source	F-value	P-value			
Model	761.95	<0.0001	Significant		
A-Bi ₂ O ₃ /TiO ₂ ratio	4.78	0.0537	Not significant		
B-Cu/Ti ratio	45.64	<0.0001	Significant	R ²	0.998
C-time	3,298.14	<0.0001	Significant	Adj. R ²	0.997
AB	2,820.90	<0.0001	Significant	Pred. R ²	0.993
AC	51.60	<0.0001	Significant	Adeq. precision	107.27
BC	22.57	0.0008	Significant		
A ²	0.71	0.4190	Not significant		
B ²	247.44	<0.0001	Significant		
C ²	10.17	0.0097	Significant		
Lack of fit	0.86	0.5635	Not significant		

Table 7
Power Transform ANOVA results after remove A² parameter

Source	F-value	P-value			
Model	880.27	<0.0001	Significant		
A-Bi ₂ O ₃ /TiO ₂ ratio	4.91	0.0488	Significant		
B-Cu/Ti ratio	46.88	<0.0001	Significant	R ²	0.998
C-time	3,387.27	<0.0001	Significant	Adj. R ²	0.997
AB	2,897.13	<0.0001	Significant	Pred. R ²	0.994
AC	52.99	<0.0001	Significant	Adeq. precision	114.59
BC	23.18	0.0005	Significant		
B ²	307.72	<0.0001	Significant		
C ²	14.69	0.0028	Significant		
Lack of fit	0.83	0.5943	Not significant		

Design-Expert® Software
(Efficiency %)*0.43

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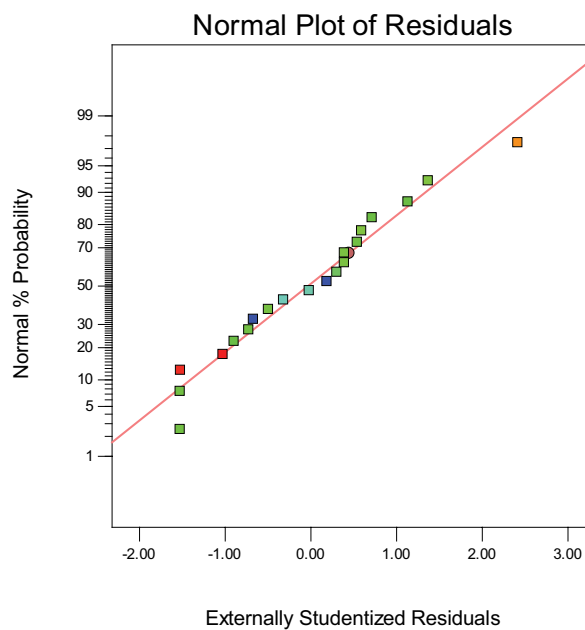


Fig. 6. Normal plot of residual experiments designed by RSM.

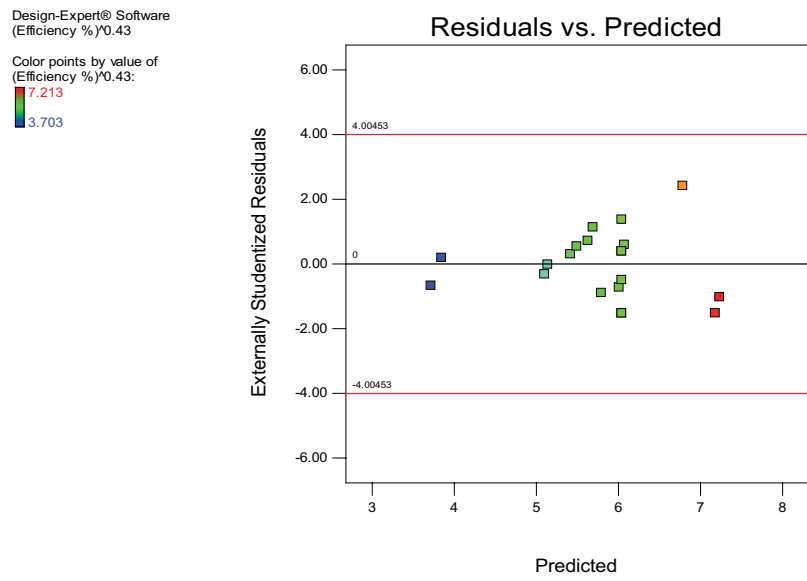


Fig. 7. Plot of the residual vs. model predictions.

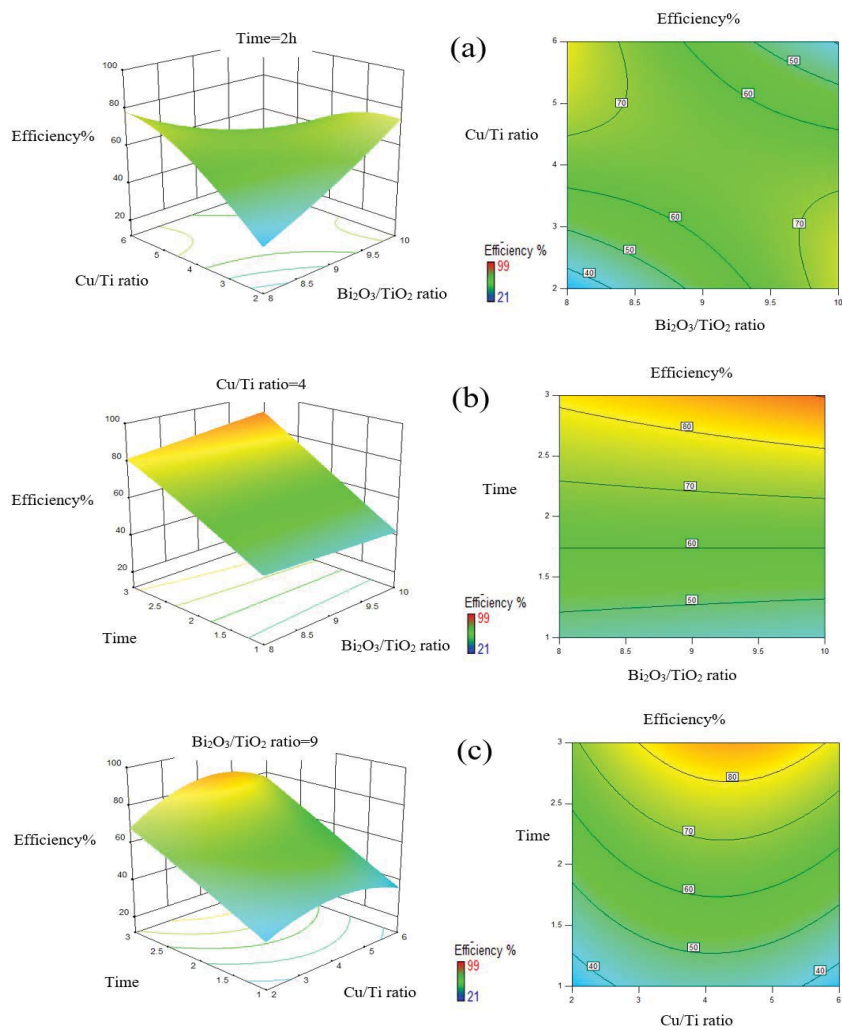


Fig. 8. (a–c) Effects of Cu/Ti, Bi₂O₃/TiO₂ ratios, and reaction time on decolorization efficiency of Direct Red 16.

the reduction of the processing time. Furthermore, at constant the Cu/Ti ratio, by increasing the Bi₂O₃/TiO₂ ratio, the efficiency of decolorization Direct red 16 is enhanced. As shown in Fig. 8c, at a constant Bi₂O₃/TiO₂ ratio, by increasing the Cu/Ti ratio, the decolorization efficiency is initially enhanced and then is reduced. This issue is due to the occurrence of the recombination phenomenon in the nano-catalyst by increasing doping values to an optimum level [35].

3.6. Kinetic study

A kinetic study was done to calculate the constant rate of Direct red 16 photodegradation for pure TiO₂, compared to optimum composites of modified TiO₂ (Cu-TiO₂, Bi₂O₃/TiO₂, and Cu-TiO₂-Bi₂O₃). The pseudo-first-order kinetic model was used to study the photodegradation kinetic for most of the organic molecules as described:

$$-\frac{dc}{dt} = K_{ap} C \tag{5}$$

$$\ln\left(\frac{C_0}{C_t}\right) = K_{ap} t \tag{6}$$

where C₀, C_t, K_{ap}, and t are concentrations at time zero and time t, constant rate, and time, respectively. The kinetic plot (ln(C₀/C_t) vs. irradiation time) is depicted in Fig. 9. The Cu-TiO₂-Bi₂O₃ indicates a much higher K_{ap} than pure TiO₂, Cu-TiO₂, and Bi₂O₃/TiO₂, which is 31.0, 9.4, and 7.0 times, respectively. It is approved more photocatalytic activity of Cu-TiO₂-Bi₂O₃ nanocomposites.

3.7. Optimization

The suggested model [Eq. (2)] was used to estimate maximum decolorization efficiency, and the corresponding

parameters to achieve it. The model predicted a maximum decolorization efficiency of 99.4% under the optimum conditions of the Bi₂O₃/TiO₂ ratio of 8.0 (wt.%), Cu/Ti ratio of 5.9 wt.%, and time of 2.9 h.

In order to confirm the accuracy of the proposed model, four replicate experiments were conducted under the optimum conditions. The decolorization efficiency was found to be 99.0% ± 0.7%, being reasonably close to the predicted value, and the model was successfully validated.

According to the results, the boundary of the lower bounds is considered to be the optimal final, which shows the synergistic effect of the simultaneous presence of Cu and Bi₂O₃ in the nano-catalyst TiO₂. It can be concluded that the shortcoming of TiO₂ nano-catalyst can be resolved by the simultaneous application of Cu and Bi₂O₃.

A comparison is made between the nano-catalyst TiO₂/Bi₂O₃-Cu and pure TiO₂ efficiencies to investigate the modified nano-catalyst. In two experiments with the same conditions, the efficiency of TiO₂/Bi₂O₃-Cu nano-catalyst is 98%, and pure TiO₂ nano-catalyst efficiency is 38% after 3 h. By comparing these two efficiencies, the effect of the modified nano-catalyst is determined in the process.

3.8. Reusability performance of Cu (5.9 wt.%) doped-TiO₂-Bi₂O₃ (8 wt.%) photocatalyst

Reusability of the Cu (5.9 wt.%) doped-TiO₂-Bi₂O₃ (8 wt.%) photocatalyst for decolorization of Direct red 16 was studied at optimum conditions (initial pH of 6.8, Direct red 16 concentration of 25 mg/L and catalyst loading of 1 g/L) after 3 h. Fig. 10 displays Direct red 16 removal efficiency and recovered photocatalyst (wt.%) for five cycles. After the first cycle, the catalyst was recovered by centrifugation, washed with distilled water, then illuminated under visible light (1 h) to remove the adsorbed pollutants and finally dried at 100°C. The result showed that the photocatalytic activity reduces about 19% after five cycles. It is confirmed that the reused catalyst has a stable structure and could be used in the subsequent runs with relatively sustainable

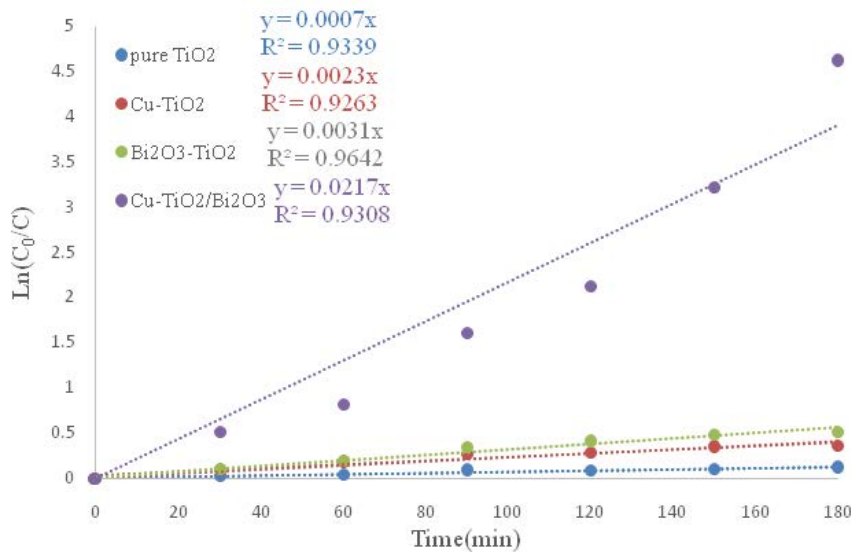


Fig. 9. DR16 photodegradation kinetic (Direct red 16 concentration = 25 mg/L, photocatalyst loading = 1 g/L, and pH of 6.8).

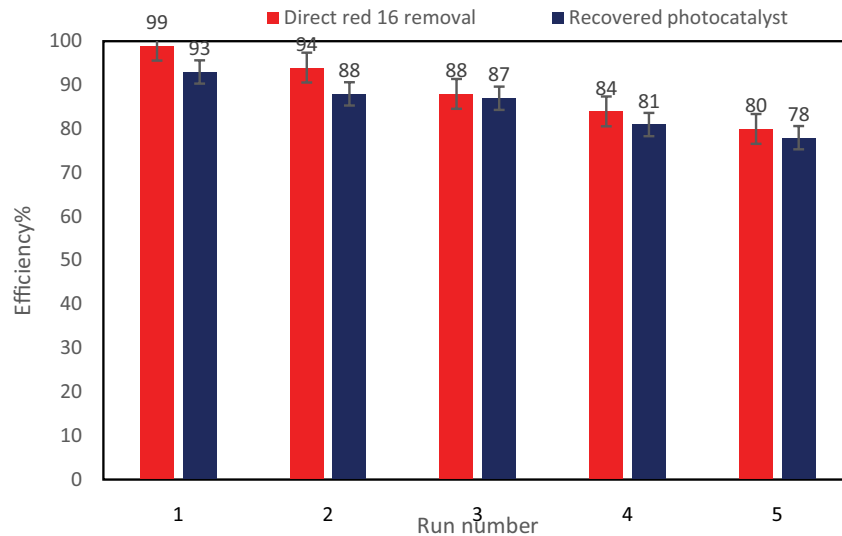


Fig. 10. Reusability results of Cu (5.9 wt.%) doped-TiO₂-Bi₂O₃ (8 wt.%) at pH of 6.8, catalyst loading of 1 g/L, and Direct red 16 concentration of 25 mg/L.

catalytic activity. The recovered photocatalyst was about 80% after five cycles.

4. Conclusions

The sol-gel technology was used in the current study to prepare a set of TiO₂/Bi₂O₃-Cu composites, exhibiting better photocatalytic activities and stability for decolorization of Direct Red 16 dye under visible light radiation. By performing the preliminary tests, the values of Cu/Ti and Bi₂O₃/TiO₂ ratio were determined. The synthesized nano-catalyst with 8 wt.% Bi₂O₃/TiO₂ ratio, 6 wt.% Cu/Ti ratio, and duration of 3 h showed the best performance. Applying a quadratic model derived based by using the RSM method showed that a nano-catalyst with optimum contents of 8.0 wt.% Bi₂O₃/TiO₂ ratio, 5.9 wt.% Cu/Ti ratio and 2.9 h had the best efficiency which is consistent with the results of the performed experiment.

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