



## Model for predicting transmembrane pressure jump for various membrane bioreactors

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### ABSTRACT

Membrane bioreactors (MBRs) are widely used to purify wastewater for reuse. One crucial problem is membrane fouling. To reduce membrane fouling, chemical cleaning must be performed because some foulants cannot be removed by physical cleaning and these foulants will prevent the recovery of membrane performance. Hence, to allow chemical cleaning at an appropriate time, membrane fouling must be predicted in the long term. When an MBR plant is operated under a condition of constant-rate filtration, this corresponds to prediction of the transmembrane pressure (TMP). Because one reason to make TMP difficult to predict is a TMP jump, we have been developing a model that predicts the time of a TMP jump. In this study, many data-sets measured in MBRs that differ in operating conditions, such as flux and reactor size, and water quality, such as viscosity and mixed liquor suspended solids concentration, were collected from the literature. Then, TMP jump prediction models having high prediction performance could be constructed for each type and each material of membrane. In addition, we discussed MBR parameters, such as reactor volume and aeration that would be important for TMP jump prediction and membrane fouling.

*Keywords:* Membrane bioreactor; Fouling; Transmembrane pressure jump; Prediction

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### 1. Introduction

Membrane bioreactors (MBRs) have been widely used in water treatment fields, such as sewage treatment and industrial wastewater treatment, to purify wastewater for reuse [1]. MBRs combine biological treatment with membrane filtration. First, bacteria within activated sludge metabolize the organic pollutants and produce environmentally acceptable metabo-

lites, then a microfiltration or ultrafiltration membrane separates liquids from solids. MBR can be distributed at various locations such as residential sections and industrial plants. Thus, we can create an environment in which treated water is effectively reused in society.

However, MBRs have some practical problems. One of the critical problems is membrane fouling [2]. Membrane fouling is a phenomenon wherein foulants, such as activated sludge, sparingly soluble compounds, and high-molecular-weight solutes and

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colloids, absorb or deposit on the membrane surface and absorb into and block the membrane pores. For example, in cases where the MBR is operated under constant-rate filtration, much energy is required to achieve a constant permeate flow rate owing to membrane fouling. To reduce membrane fouling, physical cleaning and chemical cleaning must be carried out with chemical reagents after a given period of processing time, when the transmembrane pressure (TMP) exceeds a given value, because some foulants cannot be removed by physical cleaning such as aeration, backwashing, or back pulsing, and these residual foulants will prevent the recovery of membrane performance. Frequent chemical cleaning and replacement of membranes are both expensive.

Hence, to allow chemical cleaning at an appropriate time, membrane fouling must be predicted in the long term [3–8]. When an MBR plant is operated under a condition of constant-rate filtration, this corresponds to prediction of the TMP [9–17]. Moreover, for MBR systems to be used widely as mentioned above, each MBR must be able to be operated automatically and controlled remotely. The TMP must be predicted *a priori* and a schedule of chemical cleaning must be created in advance, because a certain amount of time, for example, one week, is required for preparation of the chemicals for chemical cleaning. In addition, when distributed MBR systems are operated, it is difficult to check each MBR manually and we must make a schedule of chemical cleaning and prepare for chemical cleaning for each MBR beforehand.

One of the reasons to make TMP difficult to predict is a TMP jump [18]. After the long-term operation of MBR under the condition of constant-rate filtration, TMP increases rapidly [19]. This is called a TMP jump. Yu et al. proposed a mechanism for the TMP jump whereby the membrane is partially blocked by foulants, after which the local flux exceeds a critical flux [20], below which only reversible fouling happens and irreversible fouling can be neglected [21]. It can be said that a TMP jump is a rapid increase in TMP after a period of processing even though the measured flux is less than the critical flux.

We proposed the construction of a model that predicts the time of a TMP jump previously [22], which is based on the concept of critical flux [20] and statistical methods. The model where input variables  $X$  are time, flux, TMP and other MBR parameters such as operating conditions (aeration rate, hydraulic retention time (HRT), sludge retention time (SRT), and so on), and water quality (water temperature, total organic carbon, concentrations of extracellular polymeric substances (EPS) and soluble microbial products (SMP), and so on), and an output variable  $y$  is a label variable repre-

senting whether TMP jumps happen or not is constructed by using physical and statistical approaches. The model used to detect a TMP jump is called as a discriminant model. This model  $f$  is represented as  $y = f(X)$  and constructed with data of  $X$  measured in MBRs and those of  $y$  where the presence of TMP jumps is labeled. A support vector machine (SVM) [23], which is a nonlinear classification method, was applied for the construction of  $f$ . By inputting new data of  $X$  into  $f$ , we can estimate whether a TMP jump happens or not at the time when the new data are measured. Also, the presence of a TMP jump can be predicted at the target time by inputting setting values into  $f$ . In addition, the domains, where a discriminant model estimates TMP jumps happen, can be visualized to discuss the possibility of TMP jumps and the ways to prevent TMP jumps in the future [24].

However, each discriminant model must be constructed for each MBR, i.e. a discriminant model constructed with data measured in an MBR cannot be applied to other MBRs. In this study, therefore, we construct discriminant models that can be used for various types of MBR plants. First, from the literature, we collect many data-sets measured in MBRs that differ in operating conditions such as flux, HRT, SRT, and reactor size, and water quality such as viscosity and mixed liquor suspended solids (MLSS) concentration. Second, discriminant models are constructed for each type and each material of membrane because the interactions between foulants and membrane are different in each type and each material of membrane [25]. The type means flat membrane and hollow fiber membrane, and the material means polyvinylidene (PVDF), polyethylene (PE), polyethersulfone (PES), and so on.

In addition, we discuss MBR parameters that are important for TMP jump prediction and membrane fouling. The relationships between membrane fouling and MBR parameters, such as flux [26], SRT [27], temperature [28–31], MLSS [32,33], EPS [32–34], SMP [35], and F/M [36], have been investigated by many groups. Though some MBR parameters cannot be included in input variables of discriminant models when those parameters are not measured in many papers, we check the effect of as many parameters as possible to the performance of the discriminant models, as long as several data-sets remain.

## 2. Method

To predict the time of TMP jumps, a nonlinear function was derived, based on Darcy's law, the relationship between flux and flow rate, resistance-in-series model, parallel resistance model and the

equation of cake fouling [22]. The details of derivation of a nonlinear function for predicting the presence or absence of TMP jumps are shown in Appendix A. However, the derived function is difficult and impractical to solve. Therefore, the function judging whether TMP jumps will happen or not is solved statistically using various data-sets measured in many MBRs. The basic concept of the TMP jump discriminant model is shown in Fig. 1. Input variables  $X$  are time, flux, TMP, and other MBR parameters, and an output variable  $y$  is a label variable representing whether there are TMP jumps. The data before TMP jumps are labeled  $-1$ , the data after TMP jumps are labeled  $1$ , and an SVM model determining values of  $-1$ , and  $1$  is then constructed for  $X$  and  $y$ . The details of SVM are shown in Appendix B.

Fig. 2 shows image of the actual use of the TMP jump discriminant model. In the prediction of a TMP jump in the long term, the target time is input, a set flux relating to the constant-rate filtration is entered, and the predicted TMP should be entered into the SVM model. The TMP values are predicted with Eqs. (A1) and (A4) in Appendix A. Fortunately, the increase in TMP is represented as a linear function of time because the initial increase in the fouling resistance can be assumed to be due to cake fouling. Predicted TMP values are then entered into the discriminant model. For other parameters, predicted values or set values are entered into the model. Accordingly, we can predict whether a TMP jump will happen at target time.

Using the constructed discriminant model and inputting future set values of flux and water quality with changing them, i.e. repeating trial and error, we can search the conditions where a TMP jump will hardly happen. MBR can be accordingly controlled for a TMP jump not to happen in the future. In addition,

by projecting the results of a discriminant model to a two-dimensional map with visualization methods such as principal component analysis [37], kernel PCA [38], self-organizing map [39], and generative topographic mapping [40], we can discuss optimal MBR conditions where TMP jumps hardly happen [24].

### 3. Results and discussion

We analyzed discriminant models using operating data measured in various MBRs. The data-sets were collected from the literature. The types of membrane are flat membrane and hollow fiber membrane, and the materials of membrane are PVDF, PE, and PES. Table 1 shows the numbers of papers from which MBR data were collected and batches for each type and each material of membrane. A batch of data means the operation from the start or membrane fouling to next membrane cleaning or the end of operation. Quality and quantity of raw water and operating conditions are varied by MBRs.

To determine  $y$  in Fig. 1, we defined the data before TMP jumps ( $-1$ ) and the data after the TMP jumps ( $1$ ). First, a straight line approximating TMP by time was constructed with the first some data. The data whose absolute error of the approximation was less 2 kPa were labeled as  $-1$ , and the data whose absolute error of the approximation was equal to or more than 2 kPa were labeled as  $1$ . The detailed process should be referred to the papers [22].

Table 2 shows the input variables for each type and each material of membrane. Time, flux, and TMP are included in all types and materials of membrane. However, other variables representing operating conditions and water quality are different in types and materials of membrane because there is no information on an MBR parameter for some papers.

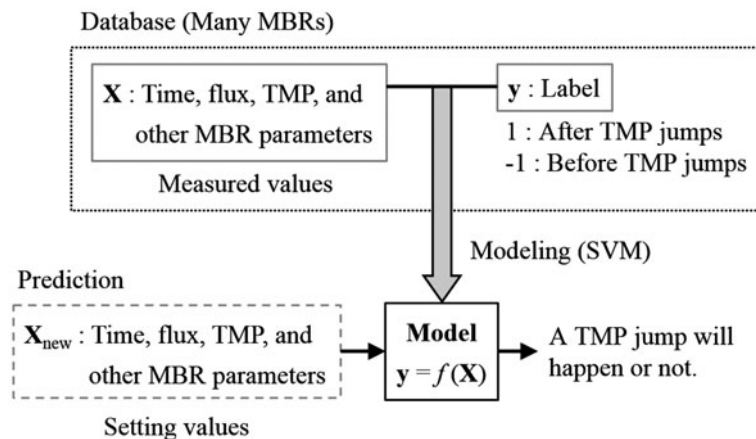


Fig. 1. TMP jump discriminant model.

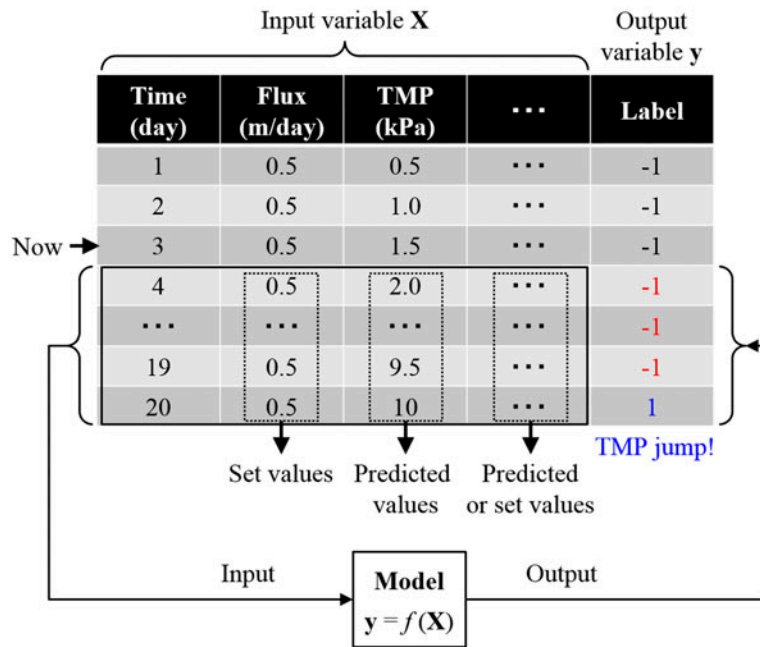


Fig. 2. Image of the actual use of the TMP jump discriminant model.

Table 1

The number of papers and batches that are collected for the analysis of TMP jump discriminant models in this paper

| Type<br>Material      | Flat membrane |           |           | Hollow fiber membrane |                  |
|-----------------------|---------------|-----------|-----------|-----------------------|------------------|
|                       | PVDF          | PE        | PES       | PVDF                  | PE               |
| The number of papers  | 13 [41–53]    | 2 [54,55] | 3 [56–58] | 7 [59–65]             | 14 [58,59,66–77] |
| The number of batches | 26            | 5         | 6         | 13                    | 22               |

Table 2

The input variables for each type and each material of membrane

| Type                  | Material | The number of input variables | Input variables   |
|-----------------------|----------|-------------------------------|---|
| Flatmembrane          | PVDF     | 11                            | Time, flux, TMP, MBR type (2), filtration mode (2), tank type for membrane (3), and viscosity |
|                       | PE       | 7                             | Time, flux, TMP, MBR type (2), reactor volume, and mixed liquor suspended solids (MLSS)       |
|                       | PES      | 7                             | Time, flux, TMP, MBR type (2), pore size, and reactor volume                                  |
| Hollow fiber membrane | PVDF     | 7                             | Time, flux, TMP, MBR type (2), pore size, and viscosity                                       |
|                       | PE       | 7                             | Time, 1/V, TMP, MBR type (2), and tank type for membrane (2)                                  |

The discriminant models were constructed with the data-set of each type and each material of membrane for the accurate prediction of TMP jumps. Table 3 shows the results of construction of discriminant models. The accuracy rate (AR), precision (PR), and the detection rate (DR) are defined as follows [Eqs. (1)–(3)]:

$$AR = \frac{TP + TN}{TP + FP + TN + FN} \tag{1}$$

$$PR = \frac{TP}{TP + FP} \tag{2}$$

Table 3  
Modeling and prediction results

|                      | Flat membrane |      |      | Hollow fiber membrane |      |
|----------------------|---------------|------|------|-----------------------|------|
|                      | PVDF          | PE   | PES  | PVDF                  | PE   |
| AR [%]               | 95.6          | 99.9 | 93.5 | 90.4                  | 91.6 |
| PR [%]               | 94.2          | 100  | 90.1 | 97.5                  | 99.4 |
| DR [%]               | 94.6          | 99.6 | 97.3 | 85.5                  | 73.8 |
| AR <sub>CV</sub> [%] | 94.4          | 99.4 | 83.0 | 91.2                  | 88.0 |
| PR <sub>CV</sub> [%] | 92.3          | 97.0 | 75.8 | 88.1                  | 88.2 |
| DR <sub>CV</sub> [%] | 93.7          | 99.6 | 96.0 | 97.9                  | 71.4 |

$$DR = \frac{TP}{TP + FN} \tag{3}$$

Here, TP denotes the number of true positives, i.e. the number of samples for which the state after TMP jumps is correctly detected; TN represents the number of true negatives, i.e. the number of samples for which the state after TMP jumps is not detected and the transition is, indeed, incomplete; FP denotes the number of false positives, i.e. the number of samples for which the state after TMP jumps is incorrectly detected; and FN represents the number of false negatives, i.e. the number of samples for which TMP jumps is actually

complete but it is not detected. AR<sub>CV</sub>, PR<sub>CV</sub>, and DR<sub>CV</sub> are the AR, PR, and DR calculated by using cross-validation based on batches. First, the original data are divided into batches. Then, one batch is used as the data for validating the model constructed using the data of the other batches. This procedure is repeated so that each batch is used once as the validation data. Finally, not calculated but predicted values of *y* can be obtained. Therefore, AR<sub>CV</sub>, PR<sub>CV</sub>, and DR<sub>CV</sub>, which are obtained by this cross-validation, mean the predictive ability of the constructed model, while AR, PR, and DR mean the accuracy of the model.

From Table 3, the discriminant models having high AR, PR, and DR values of more than 90% could be constructed for flat membrane. We achieved highly accurate discriminant models. In addition, AR<sub>CV</sub>, PR<sub>CV</sub>, and DR<sub>CV</sub> that are indexes of the predictive performance indicated over 90% for flat membrane of PVDF and PE, and over 85% for hollow fiber membrane of PVDF. It was confirmed that some discriminant models can predict TMP jumps appropriately even in inputting data measured in MBRs different from the MBRs that are used for the model construction into the discriminant model if the same type and the same material of membrane are used.

Fig. 3 shows the plots of actual and predicted time of TMP jump. The unit of time is the second. From Fig. 3(a), one point is far from the diagonal, which

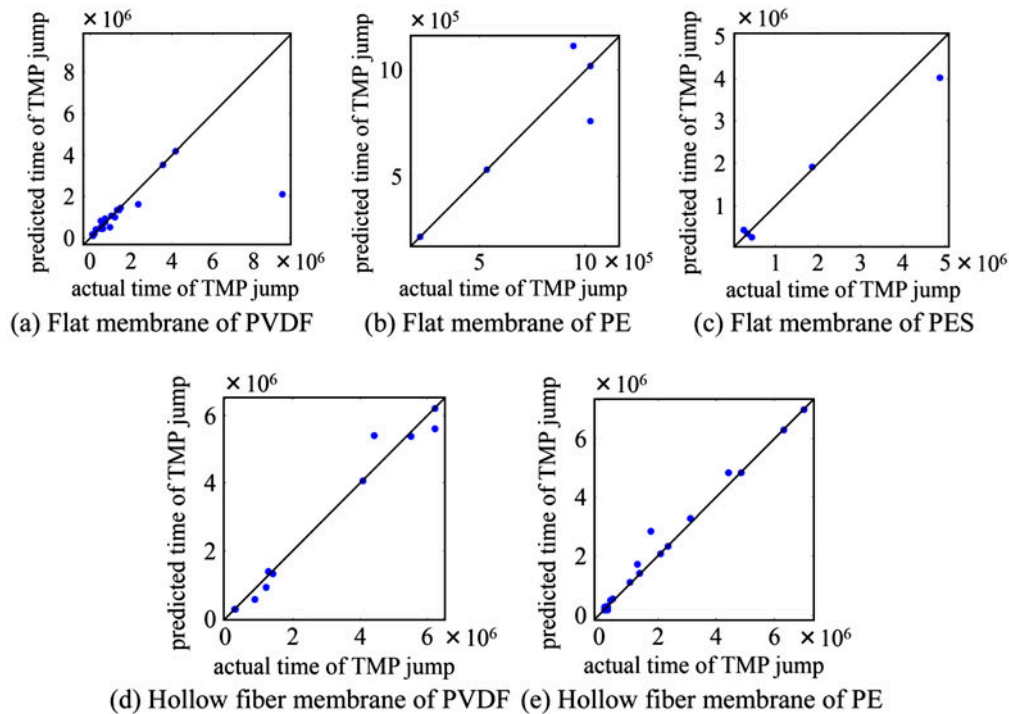


Fig. 3. The plots of actual and predicted time of TMP jump. The unit of time is the second.

means the prediction was failed. This would be because only one datum of time of the TMP jump exceeded  $9 \times 10^6$  s and the TMP jump discriminant model constructed with the other data could not predict the time of the TMP jump of the datum, which was completely different from the other data. Applicability domain [78–80] of the constructed model must be considered in practice. On the other hand, most data in Fig. 3 are close to the diagonal, reflecting that the TMP jump discriminant models can predict the time of TMP jumps correctly.

Examples of TMP jump prediction results of flat membrane of PVDF and PE, and hollow fiber membrane of PVDF are shown in Fig. 4. The four batches in Fig. 4 came from the different papers. Although the time scale and the TMP scale are different in Fig. 4(a) and (b), the discriminant model could predict the times of TMP jumps accurately. The TMP jump discriminant models can be applied to MBRs other than the MBRs where training data are measured and can be used to discuss optimal MBR systems where TMP jumps hardly happen.

However, the  $PR_{CV}$  value in the cross-validation is not so high in the case of flat membrane of PES and

the  $DR_{CV}$  value in cross-validation is not so high as well in the case of hollow fiber membrane of PE (see Table 3). For the case of flat membrane of PES, the number of batches is small in Table 1, and then, we focused on the case of hollow fiber membrane of PE in this paper. To increase predictive performance of the TMP jump discriminant model, other MBR parameters should be added to the input variables. However, an MBR parameter is not measured or described in all papers on hollow fiber membrane of PE. The addition of a new input variable means the decrease of batches or data-sets. Hence, we added new MBR parameters to the input variables one by one. Table 4 shows the additional input variables. These parameters were selected so that the number of batches was as large as possible.

Table 5 shows the modeling and prediction results when each MBR parameter is added to the seven input variables shown in Table 2 for hollow fiber membrane of PE. For A: pore size, and B: viscosity; the number of batches did not decrease so much, but the  $DR_{CV}$  value remained small. On the other hand, the  $DR_{CV}$  value greatly increased by adding C: reactor volume, D: HRT, or E: aeration, and especially the

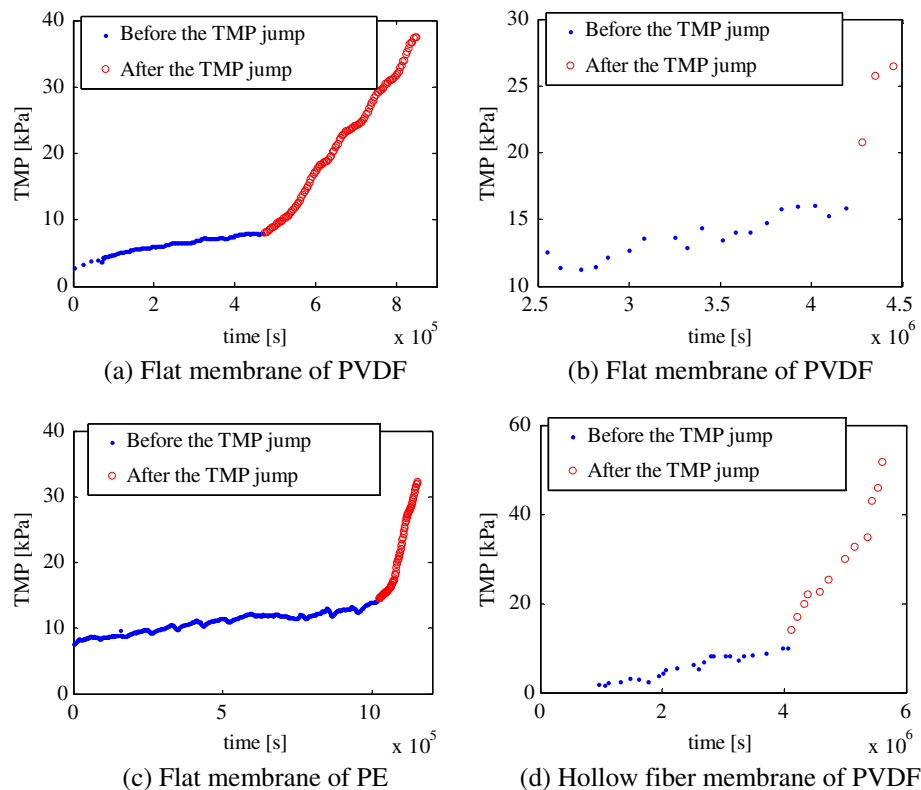


Fig. 4. Examples of prediction results.

Table 4

The additional input variables for hollow fiber membrane of PE

|   |                          |
|---|--------------------------|
| A | Pore size                |
| B | Viscosity                |
| C | Reactor volume           |
| D | Hydraulic retention time |
| E | Aeration                 |

Table 5

Modeling and prediction results for hollow fiber membrane of PE when each MBR parameter was added to the input variables. A, B, C, D, and E should be referred to Table 4

|                       | A    | B    | C    | D    | E    |
|-----------------------|------|------|------|------|------|
| The number of batches | 21   | 21   | 16   | 14   | 14   |
| AR [%]                | 92.1 | 90.9 | 95.5 | 95.5 | 96.1 |
| PR [%]                | 98.0 | 94.6 | 92.3 | 99.1 | 99.1 |
| DR [%]                | 75.5 | 76.3 | 94.7 | 86.6 | 90.0 |
| AR <sub>CV</sub> [%]  | 88.8 | 88.3 | 92.8 | 92.9 | 94.0 |
| PR <sub>CV</sub> [%]  | 93.7 | 87.1 | 96.9 | 95.6 | 92.2 |
| DR <sub>CV</sub> [%]  | 67.9 | 74.9 | 81.6 | 81.3 | 90.0 |

DR<sub>CV</sub> value was 90.0% and the AR<sub>CV</sub> and DR<sub>CV</sub> values exceeded 90% when the discriminant model had aeration as an input variable. Although the number of batches were smaller than that of only seven input variables because there are no information on such MBR parameters in several papers, reactor volume, HRT, and aeration would be important for the prediction of TMP jumps and understanding MBR fouling.

To discuss the important variables for the prediction of TMP jumps, new MBR parameters were added to the input variables for flat sheet membrane of PVDF as is the case in hollow fiber membrane of PE. Table 6 shows the additional input variables for flat membrane of PVDF. A: pore size, B: HRT, and D: reactor volume are included also in Table 4. Table 7 shows the modeling and prediction results when each

Table 6

The additional input variables for flat membrane of PVDF

|   |                          |
|---|--------------------------|
| A | Pore size                |
| B | Hydraulic retention time |
| C | Sludge retention time    |
| D | Reactor volume           |
| E | MLSS concentration       |

Table 7

Modeling and prediction results for flat membrane of PVDF when each MBR parameter was added to the input variables. A, B, C, D, and E should be referred to Table 6

|                       | A    | B    | C    | D    | E    |
|-----------------------|------|------|------|------|------|
| The number of batches | 23   | 20   | 19   | 17   | 14   |
| AR [%]                | 96.0 | 95.4 | 96.0 | 90.8 | 96.0 |
| PR [%]                | 94.8 | 94.7 | 94.9 | 94.6 | 98.5 |
| DR [%]                | 95.0 | 93.5 | 94.9 | 87.9 | 94.1 |
| AR <sub>CV</sub> [%]  | 94.6 | 93.5 | 94.3 | 84.6 | 94.2 |
| PR <sub>CV</sub> [%]  | 92.1 | 90.9 | 91.4 | 83.5 | 97.4 |
| DR <sub>CV</sub> [%]  | 94.4 | 92.8 | 94.3 | 88.8 | 91.7 |

MBR parameter is added to the eleven input variables shown in Table 2 for flat membrane of PVDF. When A: pore size, B: HRT, C: SRT, or E: MLSS concentration was added to the input variables, the AR<sub>CV</sub>, PR<sub>CV</sub>, and DR<sub>CV</sub> values were more than 90%. However, those values of D: reactor volume was lower than 90% and the predictive performance of the discriminant model decreased (see Tables 3 and 7). On the other hand, for hollow fiber membrane of PE, the predictive performance increased by adding reactor volume to the input variables (see Tables 3 and 5). This difference would be because the batches before the addition of reactor volume and the batches after the addition are different; the important input variables for the prediction of TMP jumps depend on the types and the materials of membrane; not one input variable but the combination of input variables relates TMP jumps and the relationships between reactor volume and other MBR parameters are considerable. The more data-sets and more information on MBR parameters are required to investigate the important variables and combinations of variables for TMP jumps and membrane fouling.

#### 4. Conclusion

In this paper, we constructed discriminant models for predicting TMP jumps with MBR parameters. In the construction of the models, the operating data-sets measured in various MBRs were given in the literature. The high predictive accuracy of the models could be achieved for some types and some materials of membrane used in MBR plants. To increase the predictive performance for the model, whose AR<sub>CV</sub>, PR<sub>CV</sub>, and DR<sub>CV</sub> values were low, we added several MBR parameters as the input variable one by one and checked the performance of the model. Then, reactor volume, HRT, and aeration would be important for

the prediction of TMP jumps and understanding MBR fouling. However, reactor volume decreased the  $AR_{CV}$ ,  $PR_{CV}$ , and  $DR_{CV}$  values in another type and material of membrane. The more data-sets and more information on MBR parameters are required to further investigate the important MBR parameters for TMP jumps and membrane fouling. When the important parameters can be found for a discriminant model, in the reference [24], the domains where a discriminant model estimates TMP jumps will happen is visualized. By visualizing the results of a discriminant model and analyzing set values of the MBR parameters using the visualization result, we can discuss the possibility of TMP jumps and the ways to prevent TMP jumps in the future.

By parameterizing the type and the material of membrane appropriately and using data-sets of various types and materials of membrane, the integrated discriminant model will be constructed with high prediction ability. To improve the performance of the discriminant models, the compressibility of cake appropriately. Using the TMP jump discriminant models, we will achieve the effective control of an MBR.

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## Appendix A. Derivation of a nonlinear function for predicting the presence or absence of TMP jumps [22]

Viscosity,  $\mu$ ; transmembrane flux,  $J$ ; and total filtration resistance,  $R$ , have the following Eq. (A1)

$$TMP_t = \mu_t J_t R_t \quad (A1)$$

where  $t$  is the time and these variables are functions of time. This equation is called Darcy's law. The resistance-in-series model of  $R$  is represented as follows [Eq. (A2)]:

$$R_t = R_m + R_{f,t} + R_{other,t} \quad (A2)$$

where  $R_m$  is the intrinsic membrane resistance;  $R_f$  is the fouling resistance; and  $R_{other}$  is the other resistance due to water quality, such as EPS and SMP, in MBRs.  $R_f$  and  $R_{other}$  are functions of  $t$ . If cake filtration is assumed, the parallel resistance model of  $R_f$  is given as follows [Eq. (A3)]:

$$R_{f,t} = \frac{A_0}{A_t} R_{c,t} \quad (A3)$$

where  $A_0$  is the total membrane area;  $A_t$  is the usable membrane area that is not blocked at time  $t$ ; and  $R_c$  is the resistance due to cake fouling. When MBR is operated under constant-rate filtration,  $R_c$  is given as follows [Eq. (A4)]:

$$R_{c,t} = at + b \quad (A4)$$

where  $a$  and  $b$  are constant values. Though  $R_c$  is an exponential function of  $t$ , considering the compressibility of the filter cake [81], the function of initial  $R_c$  before a TMP jump will be approximated by the linear function of  $t$  like Eq. (A4).

$J$  in Eq. (A1) is represented with treatment flow rate,  $V$ , as follows [Eq. (A5)]:

$$J_t = \frac{V_t}{A_t} \quad (A5)$$

The following Eq. (A6) is derived from Eqs. (A1)–(A5).

$$TMP_t = \mu_t \frac{V_t}{A_t} \left( R_m + \frac{A_0}{A_t} (at + b) + R_{other,t} \right) \quad (A6)$$

Then, if a mechanism of a critical flux,  $J_{crit}$ , proposed by Yu et al. [20] is adopted, a local flux exceeds  $J_{crit}$ , that is, the following [Eq. (A7)] meets, when a TMP jump happens.

$$J_t \geq J_{crit} \quad (A7)$$

Eqs. (A6) and (A7) are summarized as follows [Eq. (A8)]:

$$TMP_t - \mu J_{crit} \left( R_m + A_0(at + b) \frac{J_{crit}}{V_t} + R_{other,t} \right) \geq 0 \quad (A8)$$

Therefore, when the left-hand value of (A8) exceeds zero, a TMP jump happens. (A8) is a nonlinear function of  $t$ ,  $TMP$ ,  $V$ , and other MBR parameters such as operating conditions and water quality, which are assumed to relate  $\mu$ ,  $a$ ,  $b$ ,  $J_{crit}$ , and  $R_{other}$ . It is totally impractical to solve the function (A8) exactly and hence, this function is handled statistically. Input variables  $X$  are  $t$ ,  $TMP$ ,  $V$  (or flux  $J$ ), and other MBR parameters such as operating conditions and water quality; the labels of data before TMP jumps are set as  $-1$ ; the labels of data after TMP jumps are set as  $1$ ; and then, a model determining  $1$  or  $-1$  is constructed by using a statistical method.

## Appendix B. SVM [23]

For constructing an above discriminant model, an SVM method is used in this paper. An SVM is one of the classification methods used to generate nonlinear classifiers by applying the kernel approach. In a linear SVM, the discriminant function  $f(x)$  is defined as follows [Eq. (B1)]:

$$f(x) = x \cdot w + b \quad (B1)$$

where  $x$  is a query sample;  $w$  is a weight vector; and  $b$  is a bias. The primal form of the SVM can be expressed as an optimization problem:

Minimize [Eq. (B2)]

$$\frac{1}{2} \|w\|^2 + C \sum_i \xi_i \quad (B2)$$

subject to [Eq. (B3)]

$$y_i(x_i \cdot w + b) \geq 1 - \xi_i \\ y_i \in \{-1, 1\} \quad (B3)$$

where  $y_i$  and  $x_i$  represent training data;  $\xi_i$  is slack variables; and  $C$  is the penalizing factor that controls the trade-off between a training error and a margin. By minimizing (B2), we can construct a discriminant model that shows a good balance between the ability to adapt to the training data and the ability to generalize. In our application, a kernel function is a radial basis function as follows [Eq. (B4)]:

$$K(x, x') = \exp(-\gamma \|x - x'\|^2) \quad (B4)$$

where  $\gamma$  is the tuning parameter that controls the width of the kernel function. Using (B.4), a nonlinear model can be constructed because the inner product of  $x$  and  $w$  in (B.1) is represented as the kernel function of  $x$ . In this study, LIBSVM [82] is used as the machine learning software.