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# Modeling of nitritation and denitritation in a novel PITSF-SEU process using an extension of ASM2d model

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## ABSTRACT

In this study, an anaerobic-anoxic/oxic (A2/O) multiphased biological process called "phased isolation tank step feed technology of southeast university (PITSF-SEU)" was developed to force the oscillation of organic and nutrient concentrations in process reactors. PITSF reactor is effective for reducing energy consumption because it does not contain the internal recycle of mixed liquor and sludge return device. A computer program was built based on mass balance equations on each tank using an extension activated sludge model for simulating the soluble and particulate compounds in each tank of PITSF-SEU system. The considerable differences between the extension model and other models are two stage for nitrification process and multistage for denitrification process. Also, phosphorus removal was taken into account simultaneously in this model. The difficulty of model simulation is coming from the system operation with unsteady-state condition and the changing of multipoint step feed location with its phase time. Also, there are some tanks in PITSF SEU process are operated under combined effect of nitrification and denitrification (SND) which makes difficulty in the reaction calculation. The results showed that the growth rate constants of  $X_{AOB}$  and  $X_{NOB}$  were 1.4 and 0.4 d<sup>-1</sup>, respectively.  $Y_{AOB}$  value was 0.14, and Y<sub>NOB</sub> value was 0.04. It was showed a good agreement between the observed and simulated data, whereas the sum of squares of the deviations ( $R^2$ ) of soluble components  $S_{NH4}$ ,  $S_{PO4}$ ,  $S_{NO3}$ , and  $S_{NO2}$  were more than 0.95 in all investigated runs. According to extension model simulation, the biomass concentration of X<sub>H</sub>, X<sub>PAO</sub>, X<sub>PP</sub>, X<sub>AOB</sub>, and X<sub>NOB</sub> was decreased in the anaerobic tanks because of the lysis reaction. Then, the X<sub>H</sub>, X<sub>PAO</sub>, X<sub>PP</sub>, X<sub>AOB</sub>, and X<sub>NOB</sub> was increased in the aerobic tanks due to aerobic growth.

Keywords: PITSF-SEU; N–P removal; Mathematical model; Microbial kinetic behaviors

## 1. Introduction

Increasing requirement for nutrient removal during the last decade has led to more complex wastewater treatment processes. Currently, a variety of activated sludge processes have been employed for nutrient removal. One of the widely used BNR processes is the anaerobic, anoxic, and aerobic process (A2/O). The operational cost of A2O process is high due to needing reflow recycling devices of mixed liquor and sludge. Therefore, The A2O process was reconfigured

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into six compartments with multiphased that is called phased isolation tank step feed process (PITSF-SEU). This process was invented in southeast university, and it has been published in our previous study [1]. It was designed like SBR in control methodology and AA/O in spatial structure. Indeed, it is more similar to a normal multitank process, such as A2/O or UCT, but the operational cost of PITSF-SEU is low compared with A2O and UCT process because the operation cost was minimized through omitting the mixed liquor and sludge recycles devices. The direction of flow in this system is changed automatically through changing intake location. In order to understand bacterial conversion in BNR processes and for the optimization of nutrient removal, mathematical modeling and simulation became popular in recent years, and many different types of mathematical models have been proposed [2,3] and applied in the biological nutrient removal processes. Operational scenarios may be tested by simulation rather than conducting trial and error experiments at full scale. To date, the most successful model is activated sludge model No. 1 (ASM1), which is developed in 1986 by the task group for mathematical modeling [4]. ASM1 has been extended to include a description of biological phosphorus removal, resulting in ASM2 [5,6] and ASM2d [7,8]. Recently, some of the model concepts behind ASM1 have been altered in ASM3 [9,10] which also focus on the degradation of carbon and nitrogen. It is well known that influent organic substrate is a key component for denitrification and biological phosphorus removal. If the organic loading is less, remaining nitrate from the preceding cycle affects the phosphorus release in the next feed phase. A significant portion of organic loading was utilized for denitrification. Therefore, the availability of biodegradable carbon for phosphorus-accumulating organisms (PAO) will be reduced which caused a deterioration in biological phosphorus removal. Additionally, the nitrification process was assumed to be a one-stage process [11,12], directly from ammonia  $(S_{NH4})$  to nitrate  $(S_{NO3})$  in these models. The nitrifying bacteria species were not divided into two species, ammonia-oxidizing bacteria  $(AOB, X_{AOB})$  and nitrite-oxidizing bacteria (NOB, $X_{\text{NOB}}$ ). In addition, denitrification was also assumed to be a one-stage process, directly from  $S_{NO3}$  to nitrogen gas. The discussion of nitrite  $(S_{NO2})$  variation was absent in these models. Since nitrogen removal is one of the aims of BNR process, simulation of  $X_{AOB}$ ,  $X_{\text{NOB}}$ , and oxidized nitrogen ( $S_{\text{NO2}}$  and  $S_{\text{NO3}}$ ) becomes important on operation and management of BNR process. In this study, an extension activated sludge model was established in PITSF-SEU process that considered not only the kinetics and stoichiometry of  $X_{AOB}$  and  $X_{NOB}$  but also the reduction of  $S_{NO2}$  and  $S_{NO3}$ . The objectives of this study are listed as follows: (1) to establish an extension model for describing the transformation of different components including carbon, nitrogen, and phosphorus in the PITSF-SEU process, (2) to determine the kinetic parameters of two nitrifying species  $X_{AOB}$  and  $X_{NOB}$  using oxygen uptake rate (OUR) batch experiments, (3) to explore the consistency between simulation and observed values of different soluble and particulate components such as,  $S_{NH4}$ ,  $S_{NO2}$ ,  $S_{NO3}$  and orthophosphate ( $S_{PO4}$ ), and (4) to analyze the kinetics of different micro-organisms, including  $X_{H}$ ,  $X_{PAO}$ ,  $X_{pp}$ ,  $X_{PHA}$ ,  $X_{AOB}$ , and  $X_{NOB}$  in PITSF-SEU process under different runs.

# 2. Materials and methods

#### 2.1. Treatment plant configuration

Laboratory experiments were conducted in a new pilot scale of PITSF-SEU that composed of a rectangular box divided by baffles to form six-tank reactor. All tank except the last one have the same rectangular plane of 280 mm  $\times$  240 mm and supplied with mechanical mixers and air diffusers for providing a suitable state condition (anaerobic-anoxic/oxic) in a same tank. The last tank was operated as a clarifier. The particular advantages of this process, it has a simple structure, compact volume and operated safely. This process is a continuous flow process with a constant water level that makes high utilization capacity in the system. The main parts of a pilot plant utilized in this study are the main body that is a rectangular box of 860 mm × 535 mm × 905 mm, prestatic pumps, PLC programmable logic control, LCD display screen, inlet wastewater electromagnetic valves, outlet water, PVC pipes and others. The principle diagram of pilot plant with all major components is shown in Fig. 1. The effective water depth in the PITSF-SEU process is 700 mm, while the total depth is 900 mm. An operation cycle is composed of two half-cycles with same running schemes as shown in Fig. 2. It is divided into six phases named as phase I, II, and III during the first half-cycle and phase IV, V, and VI during the second half-cycle. An optimized removal efficiency of pollutant was achieved at a HRT of 15 h, SRT of 13 day, aeration ratio of 10% at a temperature range of 11-21°C and sludge recycle ratio of 35%. The optimized running time was 3, 2.5, and 2 h of phase I, II, and III, respectively.

## 2.2. Analytical methods

COD, ammonia–N, nitrate–N, nitrite–N, PO<sub>4</sub>–P, TP, and TN were analyzed according to standard



Fig. 1. Configuration of PITSF-SEU system with all main parts, 1–5, five tank; 6, settling tank; 7, PLC programmable logic controller; 8, feed tank; 9–13, inlet electromagnetic valve; 14–18, mixer; 19, air compressor; 20, touch screen of control panel; 21–25, aeration electromagnetic valve; 26-excess sludge tank 27, 28, 29; sludge return valve; 30, inlet prestatic pump; 31, sludge recycle control meter; 32, excess sludge control meter; 33–34, sludge discharge valves; 35, effluent; 36, electrical mixer line; 37, electrical inlet valve line; 38, electrical sludge return valve line; 39, electrical aeration valve line; 40, electrical sludge discharge valve line.



T1–T6, six tanks; 1 - step feed of raw wastewater; 2 - outlet water; 3 - continuous flow of mixed liquor to tank six; 4 - sludge recycle; 5 - excess sludge

Fig. 2. Run scheme of PITSF-SEU activated sludge system [1].

methods [13]. Nitrate–N were analyzed by the IC method (Metrohm 761 compact IC equipped with Metrosep A Supp 5 column and TN was analyzed by Analytik Jena AG multi N/C 3000.

#### 2.3. Determination of COD fraction and OUR experiments

Several methods have been developed for wastewater characterization, but the two most commonly used processes are the biological and physical/chemical characterizations. The physicochemical method is based on the assumption that COD fractions model can be separated by filtration and flocculation processes and that COD of the gained fractions is easily measurable by standard chemical methods [14]. In this study, wastewater characterization was determined by physicochemical method for determining COD fraction as explained in Fig. 3, which depicts the retention or passage of the influent wastewater COD components through sequential 1.2  $\mu$ m-glass-fiber filtration, flocculation (to remove colloidal matter from liquid phase) and 0.45  $\mu$ m-membrane filtration. The main steps and theoretical formulas of COD fractionation are shown below:



Fig. 3. Summary of influent characterization for organic wastewater components.

 $S_{\rm I}$  = 90% of filtered (0.45 µm) effluent COD or  $S_{\rm I}$  = filtered (0.1 µm) influent COD.

 $S_{\rm S}$  = Flocculated (ZnSO<sub>4</sub>) and filtered (0.45 µm) influent COD– $S_{\rm I}$ .

 $S_{\rm F} = S_{\rm S} - S_{\rm A}$ ;  $X_{\rm S} = \text{BOD}_{\rm ULTIMATE} - S_{\rm S}$ ; and  $X_{\rm I} = \text{COD}_{\rm T} - S_{\rm I} - S_{\rm S} - X_{\rm S}$ .

In addition, OUR was used to calculate the biomass of  $X_{\rm H}$ ,  $X_{\rm AOB}$ , and  $X_{\rm NOB}$  in a raw wastewater. It refers to the amount of oxygen used by a unit mass of active sludge in a unit of time. A certain quantity of MLSS sample was taken from Wuxi wastewater and added into OUR chambers. In order to evaluate the kinetic parameters and active biomass of  $X_{\rm H}$ ,  $X_{\rm AOB}$ , and  $X_{\rm NOB}$ , different types of OUR values should be considered:

Total OUR (OUR<sub>T</sub>); OUR of  $X_{\rm H}$  (OUR<sub>H</sub>); OUR of  $X_{\rm AOB}$  (OUR<sub>AOB</sub>) and OUR of  $X_{\rm NOB}$  (OUR<sub>NOB</sub>). The determination of OURs of  $X_{\rm H}$ ;  $X_{\rm AOB}$  and  $X_{\rm NOB}$  were based on the subsequent addition of allylthiourea (ATU) and NaN<sub>3</sub>, selective inhibitors of  $X_{\rm AOB}$  and  $X_{\rm NOB}$ , to the MLSS sample. As determining OUR<sub>T</sub>, no inhibitor was added. When determining OUR<sub>H</sub>, both allylthiourea (86 µM) and NaN3 (24 µM) [15] were added. If only NaN3 (24 µM) was added, the determined OUR was the sum of OUR<sub>H</sub> and OUR<sub>AOB</sub>, then

 $OUR_{NOB} = OUR_T - (OUR_H + OUR_{AOB}).$ 

 $OUR_{AOB} = (OUR_H + OUR_{AOB}) - OUR_H.$ 

The raw wastewater was typical in Wuxi campus of southeast university, China. COD unfiltrated was fluctuated between 175 and 700.2 mg/L with an average of 575 mg/L, of which  $S_S$ ,  $S_I$ ,  $X_S$  and  $X_I$  accounted for about 38, 2, 43 and 11%, respectively. MLSS was between 45 and 93 mg/L with average of 76 mg/L. NH<sub>4</sub><sup>+</sup>-N was between 16 and 46 mg/L with average of 28 mg/L. TP was between 1.5 and

4.7 mg/L with an average of 3.2 mg/L, of which  $PO_4^{3-}$ -P accounted for about 74–93%.

### 2.4. Mass balance equations and model algorithms

A computer program called "extension of ASM2d model" was built based on mass balance equations on each tank of PITSF-SEU system after solving the differential equation by Euler method. Model configuration of the PITSF-SEU system during a first half-cycle is explained clearly in Fig. 4. The algorithm for implementing the calculation of extending activated sludge model was described as follows:

Inlet–Outlet + Reaction rate = Accumulation

$$QC_{0,j} + r_j V = QC_{2i,j} + V \frac{dC_{i,j}}{dt}$$
(1a)

$$C(t) \times \left(\frac{dc}{dt}\right) = \frac{C_{0i,j} - C_{i,j} + M_{i,j} - N_{i,j}}{V_{i,j} C_{i,j}}$$
 (1b)

where *Q*: inlet flow rate; *V*: volume of each tank; *r*: reaction rate where it was calculated according to extending activated sludge model;  $C_{2i,j}$ : component concentration in the reaction tanks, i = 1, 2, 3, i.e. tank number; j = component number;  $C_{0,j}$ : influent concentration (MT<sup>-1</sup>);  $C_{i,j}$ : effluent concentration.

 $M_{i,j}$ ,  $N_{i,j}$  are production and consumption (MT<sup>-1</sup>) terms of the *j* No. component in the *i* No. tank.

(1) During Phase I, the mass balance equations can be written (from Fig. 5(a)) as:

Tank no. 1:

$$0.5 \times Q \times (C_0 - C_1) + r_1 \times V = V \times \frac{dC_1}{dt}$$
<sup>(2)</sup>

Tank no. 2:

$$0.5 \times Q \times (C_0 + C_1) - Q \times C_2 + r_2 \times V = V \times \frac{dC_2}{dt}$$
(3)

Tank no. 3:

$$Q \times C_2 - Q \times C_3 + r_3 \times V = V \times \frac{dC_3}{dt}$$
(4)

Tank no. 4:

$$Q \times C_3 + Qr \times Cr - (Q + Qr) \times C_4 + r_4 \times V = V \times \frac{dC_4}{dt}$$
(5)



Fig. 4. Layout and algorithms of PITSF-SEU process during a first half cycle.

Tank no. 5:

$$(Q+Qr) \times C_4 - (Q+Qr) \times C_5 + r_5 \times V = V \times \frac{\mathrm{d}C_5}{\mathrm{d}t} \quad (6)$$

(1) During Phase II, the mass balance equations can be written (from Fig. 5(b)) as:



Fig. 5. Diagram of mass balance equation during all phases.

Tank no. 1:

$$0.5 \times Q \times (C_0 - C_1) + r_1 \times V = V \times \frac{dC_1}{dt}$$
(7)

Tank no. 2:

$$0.5 \times Q \times (C_1 - C_2) + r_2 \times V = V \times \frac{dC_2}{dt}$$
(8)

Tank no. 3:

$$0.5 \times Q \times (C_0 + C_2) + Qr \times Cr - (Q + Qr)$$
$$\times C_3 + r_3 \times V = V \times \frac{dC_3}{dt}$$
(9)

Tank no. 4:

$$(Q+Qr) \times C_3 - (Q+Qr) \times C_4 + r_4 \times V = V \times \frac{dC_4}{dt}$$
(10)

Tank no. 5:

$$(Q+Qr) \times C_4 - (Q+Qr) \times C_5 + r_5 \times V = V \times \frac{dC_5}{dt}$$
(11)

(1) During Phase III, the mass balance equations can be written (from Fig. 5(c)) as; Tank no. 2:

$$Q \times C_0 + Qr \times Cr - (Q + Qr) \times C_2 + r_2 \times V = V \times \frac{dC_2}{dt}$$
(12)

Tank no. 3:

$$(Q+Qr) \times C_2 - (Q+Qr) \times C_3 + r_3 \times V = V \times \frac{dC_3}{dt}$$
(13)

Tank no. 4:

$$(Q+Qr) \times C_3 - (Q+Qr) \times C_4 + r_4 \times V = V \times \frac{dC_4}{dt}$$
(14)

Tank no. 5:

$$(Q+Qr) \times C_4 - (Q+Qr) \times C_5 + r_5 \times V = V \times \frac{dC_5}{dt}$$
(15)

where Qr = flow rate of sludge recycle and its value 35% of influent flow rate; V = 47 L the volume of each tank.

The reaction rate  $(r_i)$  is calculated by summing the product of the process rate expression  $(\rho_j)$  (Table 1) and the stoichiometric coefficients  $V_{i,j}$  (Table 2) for the component (No. *i*) being considered in the mass balance:

$$r_i \sum_j v_{i,j} \rho_j \tag{16}$$

The equations that described the transformation of the wastewater quality in the extension model produced an ordinary differential equations system. Then, the set of equations were integrated simultaneously by the first-order Euler numerical method. The entire model was implemented by means of a computer program that was coded with MATLAB 2010 language

Table 1			
Process rate	e equation	of extension	model

j	Process	Process rate equation $\rho_j, \rho_j \ge 0 \ (M_1 \ L^{-3} \ T^{-1})$
He	terotrophic organisms: X <sub>H</sub>	
1	Aerobic growth on $S_{\rm F}$	$\mu_{H} \frac{S_{O2}}{K_{O2H} + S_{O2}} \frac{S_{F}}{K_{FH} + S_{F}} \frac{S_{F}}{S_{A} + S_{F}} \frac{S_{NH4}}{K_{NH4H} + S_{NH4}} \frac{S_{PO4}}{K_{PH} + S_{PO4}} \frac{S_{ALK}}{K_{ALKH} + S_{ALK}} X_{H}$
2	Aerobic growth on $S_A$	$\mu_{H} \frac{S_{O2}}{K_{O2H} + S_{O2}} \frac{S_{F}}{K_{FH} + S_{F}} \frac{S_{A}}{K_{AH} + S_{A}} \frac{S_{A}}{S_{A} + S_{F}} \frac{S_{NH4}}{K_{NH4H} + S_{NH4}} \frac{S_{PO4}}{K_{PH} + S_{PO4}} \frac{S_{ALK}}{K_{ALKH} + S_{ALK}} X_{H}$
3	Anoxic growth on $S_{\rm F}$ , denitrification ( $S_{\rm NO2}$ )	$\mu_H \eta_{\text{NO2H}} \frac{K_{\text{O2H}}}{K_{\text{O2H}} + S_{\text{O2}}} \frac{S_{\text{NO2}}}{K_{\text{NO2H}} + S_{\text{NO2}}} \frac{S_F}{K_{\text{FH}} + S_F} \frac{S_F}{S_A + S_F} \frac{S_{\text{NH4}}}{K_{\text{NH4H}} + S_{\text{NH4}}} \frac{S_{\text{PO4}}}{K_{\text{PH}} + S_{\text{PO4}}} \frac{S_{\text{ALK}}}{K_{\text{ALK}} + S_{\text{ALK}}} X_H$
4	Anoxic growth on $S_{\rm F}$ , denitrification ( $S_{\rm NO3}$ )	$\mu_H \eta_{\text{NO3H}} \frac{K_{\text{O2H}}}{K_{\text{O2H}} + S_{\text{O2}}} \frac{S_{\text{NO3}}}{K_{\text{NO3H}} + S_{\text{NO3}}} \frac{S_F}{K_{\text{FH}} + S_F} \frac{S_F}{S_A + S_F} \frac{S_{\text{NH4}}}{K_{\text{NH4H}} + S_{\text{NH4}}} \frac{S_{\text{PO4}}}{K_{\text{PH}} + S_{\text{PO4}}} \frac{S_{\text{ALK}}}{K_{\text{ALK}} + S_{\text{ALK}}} X_H$
5	Anoxic growth on $S_A$ , denitrification ( $S_{NO2}$ )	$\mu_{H}\eta_{\text{NO2H}} \frac{K_{\text{O2H}}}{K_{\text{O2H}} + S_{\text{O2}}} \frac{S_{\text{NO2}}}{K_{\text{NO2H}} + S_{\text{NO}}} \frac{S_{\text{A}}}{K_{\text{AH}} + S_{\text{A}}} \frac{S_{\text{A}}}{S_{\text{A}} + S_{\text{F}}} \frac{S_{\text{NH4}}}{K_{\text{NH4H}} + S_{\text{NH4}}} \frac{S_{\text{PO4}}}{K_{\text{PH}} + S_{\text{PO4}}} \frac{S_{\text{ALK}}}{K_{\text{ALK}} + S_{\text{ALK}}} . X_{\text{H}}$
6	Anoxic growth on $S_A$ , denitrification ( $S_{NO3}$ )	$\mu_{H}\eta_{\rm NO3H} \frac{K_{\rm O2H}}{K_{\rm O2H} + S_{\rm O2}} \frac{S_{\rm NO3}}{K_{\rm NO3H} + S_{\rm NO3}} \frac{S_{\rm A}}{K_{\rm AH} + S_{\rm A}} \frac{S_{\rm A}}{S_{\rm A} + S_{\rm F}} \frac{S_{\rm NH4}}{K_{\rm NH4H} + S_{\rm NH4}} \frac{S_{\rm PO4}}{K_{\rm PH} + S_{\rm PO4}} \frac{S_{\rm ALK}}{K_{\rm ALK} + S_{\rm ALK}} . X_{\rm H}$
7	Fermentation	$q_{\rm fe} \frac{K_{\rm O2H}}{K_{\rm O2H} + S_{\rm O2}} \frac{K_{\rm NOxH}}{K_{\rm NOxH} + S_{\rm NO}} \frac{S_{\rm F}}{K_{\rm fe} + S_{\rm F}} \frac{S_{\rm ALK}}{K_{\rm ALK} + S_{\rm ALK}} . X_{\rm H}$
8	Lysis	$b_{ m H}X_{ m H}$
Nit	rifying organisms, autotrophic	(Ammonia oxidizing bacteria): X <sub>AOB</sub>
9	Aerobic growth of $X_{AOB}$	$\mu_{AOB} \frac{S_{O2}}{K_{AOB}} \frac{S_{NH4}}{K_{AOB}} \frac{S_{PO4}}{K_{AOB}} \frac{S_{ALK}}{K_{AOB}} X_{AOB}$
10	Lysis	$K_{O2AOB} + S_{O2} \kappa_{NH4AOB} + S_{NH4} \kappa_{PANO} + S_{PO4} \kappa_{ALKANO} + S_{ALK} b_{AOB} X_{AOB}$
Nit	rifying organisms, autotrophic	(nitrite oxidizing bacteria): X <sub>NOB</sub>
11	Aerobic growth of $X_{NOB}$	$\mu_{\text{NOB}} = \frac{S_{02}}{S_{02}} = \frac{S_{\text{NH4}}}{S_{\text{PO4}}} = \frac{S_{\text{PO4}}}{S_{\text{ALK}}} = X_{\text{NOB}}$
12	Lysis	$K_{O2NOB} + S_{O2} K_{NH4NOB} + S_{NH4} K_{PANO} + S_{PO4} K_{ALKANO} + S_{ALK} b_{NOB} X_{NOB}$
Ηv	drolusis process	
13	Aerobic hydrolysis	$K_{\rm h}\eta \frac{S_{\rm O2}}{K_{\rm O2S} + S_{\rm O2}} \frac{X_{\rm S}/X_{\rm H}}{K_{\rm XS} + X_{\rm S}/X_{\rm H}} X_{\rm H}$
14	Anoxic hydrolysis	$K_{h}\eta_{\rm NOXS} \frac{K_{\rm O2S}}{K_{\rm O2S} + S_{\rm O2}} \frac{S_{\rm NOX}}{K_{\rm NO3S} + S_{\rm NOX}} \frac{X_{\rm S}/X_{\rm H}}{K_{\rm XS} + X_{\rm S}/X_{\rm H}}.X_{\rm H}$
15	Anaerobic hydrolysis	$K_h \eta_{\rm fe} \frac{K_{\rm O2S}}{K_{\rm O2S} + S_{\rm O2}} \frac{K_{\rm NOXS}}{K_{\rm NOXS} + S_{\rm NOX}} \frac{X_{\rm S}/X_{\rm H}}{K_{\rm XS} + X_{\rm S}/X_{\rm H}} . X_{\rm H}$
Phe	osphorus accumulating organis	ms (PAO): $X_{PAO}$
16	Storage of X <sub>PHA</sub>	$q_{\rm PHA} \frac{S_{\rm A}}{K_{\rm APAO} + S_{\rm A}} \frac{S_{\rm ALK}}{K_{\rm ALKPAO} + S_{\rm ALK}} \frac{X_{\rm PP}/X_{\rm PAO}}{K_{\rm PP} + X_{\rm PP}/X_{\rm PAO}} . X_{\rm PAO}$
17	Aerobic storage of $X_{PP}$	$q_{\rm PP} \frac{S_{\rm O2}}{K_{\rm O2PAO} + S_{\rm O2}} \frac{S_{\rm PO4}}{K_{\rm PS} + S_{\rm PO4}} \frac{S_{\rm ALK}}{K_{\rm ALKPAO} + S_{\rm ALK}} \frac{X_{\rm PHA}/X_{\rm PAO}}{K_{\rm PHA} + X_{\rm PHA}/X_{\rm PAO}} \frac{K_{\rm MAX} - X_{\rm PP}/X_{\rm PAO}}{K_{\rm IPP} + K_{\rm MAX} - X_{\rm PP}/X_{\rm PAO}}.X_{\rm PAO}$
18	Anoxic storage of $X_{PP}$ , denitrification ( $S_{NO2}$ )	$\rho_{17}\eta_{\text{NOXPAO}} \frac{K_{\text{O2PAO}}}{S_{\text{O2}}} \frac{S_{\text{NOX}}}{K_{\text{NOXPAO}} + S_{\text{NOX}}} \frac{S_{\text{NO2}}}{S_{\text{NOX}}}$
19	Anoxic storage of $X_{PP}$ , denitrification ( $S_{NO3}$ )	$\rho_{17}\eta_{\text{NOXPAO}} \frac{K_{\text{O2PAO}}}{S_{\text{O2}}} \frac{S_{\text{NOX}}}{K_{\text{NOXPAO}} + S_{\text{NOX}}} \frac{S_{\text{NO3}}}{S_{\text{NOX}}}$
20	Aerobic growth of $X_{PAO}$	$\mu_{\text{PAO}} \frac{S_{\text{O2}}}{K_{\text{O2PAO}} + S_{\text{O2}}} \frac{S_{\text{NH4}}}{K_{\text{NH4PAO}} + S_{\text{NH4}}} \frac{S_{\text{PO4}}}{K_{\text{PPAO}} + S_{\text{PO4}}} \frac{S_{\text{ALK}}}{K_{\text{ALKPAO}} + S_{\text{ALK}}} \frac{X_{\text{PHA}}/X_{\text{PAO}}}{K_{\text{PHA}} + X_{\text{PHA}}/X_{\text{PAO}}} X_{\text{PAO}}$
21	Anoxic growth of $X_{PAO}$ , denitrification ( $S_{NO2}$ )	$\rho_{20}\eta_{\text{NOXPAO}} \frac{K_{\text{O2PAO}}}{S_{\text{O2}}} \frac{S_{\text{NOX}}}{K_{\text{NOXPAO}} + S_{\text{NOX}}} \frac{S_{\text{NO2}}}{S_{\text{NOX}}}$

j	Process	Process rate equation $\rho_j, \rho_j \ge 0 \ (M_1 \ L^{-3} \ T^{-1})$
22	Anoxic growth of $X_{PAO}$ , denitrification $(S_{NO3})$	$\rho_{20}\eta_{\text{NOXPAO}} \frac{K_{\text{O2PAO}}}{S_{\text{O2}}} \frac{S_{\text{NOX}}}{K_{\text{NOXPAO}} + S_{\text{NOX}}} \frac{S_{\text{NO3}}}{S_{\text{NOX}}}$
23	Lysis of X <sub>PAO</sub>	$b_{\rm PAO}X_{\rm PAO}$
24	Lysis of X <sub>PP</sub>	$b_{\rm PP}X_{\rm PP}$
25	Lysis of X <sub>PHA</sub>	$b_{\rm PHA}X_{\rm PHA}$

Table 1 (Continued)

according to the program structure of PITSF-SEU reactor. When all the vectors  $\frac{1}{C_{i,j}}(dC/dt)$  were approximately equal to zero, a steady state was observed. The integration was most perfect when time step is very small, but the computing time increased inversely with the size of time step. Conversely, too large time step would result in great errors and other numerical problem. Thus, one criterion for an upper boundary on time step is:

$$\Delta t \ll -C(t) \times (dC/dt)^{-1} \tag{17}$$

where  $\Delta t$  is time step. By combining Eqs. (1b) and (17), and neglecting the  $M_{i,j}$ ,  $N_{i,j}$  terms in the mass balance, resulted the maximum step size as shown below:

$$\Delta t \ll V_j \times C_{ij} / C_{2ij} + N_{ij}) = \varphi_{ij} \tag{18}$$

The term  $\varphi_{ij}$  is the mean residence time of component *j* in reactor component *i* at steady state.

#### 3. Extension ASM2d model development

# 3.1. Two-step nitrification processes of $X_{AOB}$ and $X_{NOB}$

Under aerobic state condition,  $S_{\text{NH4}}$  is oxidized to  $S_{\text{NO2}}$  by  $X_{\text{AOB}}$ ; subsequently,  $S_{\text{NO2}}$  is oxidized to  $S_{\text{NO3}}$  by  $X_{\text{NOB}}$ . The two-step nitrification reactions were described by two Eqs. (process (9) and (11) in Table 1) of extension model.

## 3.2. Decreases of $S_{NO2}$ and $S_{NO3}$ related to $X_{H}$

In ASM2d [16], it was assumed that  $S_{\rm NO3}$  would be transformed directly into molecular nitrogen (N2) under anoxic state condition. Two types of carbon sources were utilized for the decreasing of  $S_{\rm NO3}$ , including readily biodegradable substrate (S<sub>F</sub>) and fermentation products (S<sub>A</sub>). To describe these observing, two equations were adopted in ASM2d [17]. Indeed, nitrate ( $S_{NO3}$ ) may be reduced to nitrite ( $S_{NO2}$ ) and subsequently to molecular N<sub>2</sub> by heterotrophic bacteria ( $X_H$ ) under anoxic state condition. In extension model, decreases of  $S_{NO2}$  and  $S_{NO3}$  using different carbon sources, whereas readily biodegradable fermentable organic substrate ( $S_F$ ) and volatile fatty acids ( $S_A$ ) were considered. As a result, four process Eqs. (process (3–6) in Table 1) were adopted to describe denitrification process in the extension model under anoxic state condition.

# 3.3. Decreases of $S_{NO2}$ and $S_{NO3}$ related to $X_{PAO}$

Previous studies reviewed that nitrite ( $S_{NO2}$ ) also served as the electron acceptors for polyphosphateaccumulating organisms under anoxic state condition excepting nitrate ( $S_{NO3}$ ) [2]. In extension of ASM2d model, it was assumed that the contribution of  $X_{PAO}$ for reducing nitrite and nitrate depended on the ratios of  $S_{NO2}$  and  $S_{NO3}$  to  $S_{NOX}$ .

# 3.4. Heterotrophic nitrification modeling

In PITSF process, SND process was clearly observed in tank two and tank three during phase II and III, respectively, whereas it was operated under a companied effect of nitrification and denitrification as shown in our previous work [1]. Thus, the stoichiometric matrix and process rate equation for both aerobic and anoxic conditions were considered for simulated each compound in these tanks. It is evident from this model (SND model) that two types of carbon sources ( $S_F$  and  $S_A$ ) were modeled separately for reducing nitrate and nitrite under anoxic conditions, and therefore, four process Eqs. (process 3–6) in Table 1), and two types of carbon sources ( $S_F$  and  $S_A$ ) were considered under aerobic condition (process (1) and (2) in Table 1).

Tal Sto	ble 2 vichiometric matrix										
°	. Process	$S_{\rm F}$	S <sub>A</sub> S <sub>NH4</sub>	SNO2	S <sub>NO3</sub>	Spo4	SI SALK XS	X <sub>H</sub> X <sub>PAO</sub> X <sub>A</sub>	OB XNOB XPP XP	HA XI	X <sub>TSS</sub>
- 0 v	Aerobic growth on $S_{\rm F}$ Aerobic growth on $S_{\rm A}$ Anoxic growth on $S_{\rm F}$ , denitrification	$-rac{1}{Y_H}$ $-rac{1}{Y_H}$	$-\frac{V_{1,NI}}{Y_{H}} \frac{V_{1,NI}}{V_{2,NI}}$	$\begin{array}{c} 14 \\ 14 \\ 14 \\ 1.71Y \\ 1.71Y \end{array}$		$V_{1,\mathrm{PO4}}$ $V_{2,\mathrm{PO4}}$ $V_{3,\mathrm{PO4}}$		111			
4	Anoxic growth on $S_{\rm F}$ , denitrification	$-rac{1}{Y_H}$	$V_{4,\mathrm{NI}}$	-14	$-rac{1-Y_H}{2.86Y_H}$	$V_{4,PO4}$		1			
Ŋ	Anoxic growth on $S_{A}$ , Denitrification	·	$-rac{1}{Y_H} V_{5,\mathrm{NH}}$	H4 $-\frac{1-Y_i}{1.71Y}$	H H	$V_{5,\rm PO4}$		1			
9	Anoxic growth on $S_A$ , denitrification		$-rac{1}{Y_H}V_{6,\mathrm{NI}}$	-14 	$-rac{1-Y_H}{2.86Y_H}$	$V_{6,PO4}$		1			
7 8 f <sub>XI</sub>	vonoa Fermentation Lysis		$1 V_{7,N1} V_{8,N1}$	14 14		$V_{7,\mathrm{PO4}}$ $V_{8,\mathrm{PO4}}$		$1-f_{XI}$ $-1$			
9 9 F <sub>XI</sub>	trifying organisms, autotrophic (Ammoni Aerobic growth of X <sub>AOB</sub> Lysis	ia oxidizir	ig bacteria $V_{9,\mathrm{NI}}$ $V_{10,\mathrm{N}}$	): $X_{AOB} - \frac{1}{Y_{AOB}}$		$-i_{\rm PBM}$ $V_{10,\rm PO4}$		$1 - f_{\chi_I}$	-		
11 12 12 12	rifying organisms, autotrophic (nitrite ox Aerobic growth of $X_{\rm NOB}$ Lysis f <sub>XI</sub>	idizing ba	icteria): $X_{\rm h}$ $V_{11,{\rm N}}$ $V_{12,{\rm N}}$	$\frac{1}{114} - \frac{1}{Y_{NOB}}$	$-rac{1}{Y_{ m NOB}}$	— <sup>1</sup> рвм V <sub>12,</sub> ро4		$1-f_{XI}$	1		
Hyc 13 14 15	drolysis process: Aerobic hydrolysis Anoxic hydrolysis Anaerobic hydrolysis	1-f <sub>SI</sub> 1-f <sub>SI</sub> 1-f <sub>SI</sub>	$V_{13,N} \ V_{14,N} \ V_{15,N}$	ІН4 ІН4 ІН4			fsi V <sub>13,</sub> Alk –1 fsi V <sub>14,</sub> Alk –1 fsi V <sub>15,</sub> Alk –1				$V_{ m 13,Tss} V_{ m 14,Tss} V_{ m 14,Tss} V_{ m 15,Tss}$
Ph( 16 17 18	osphorus accumulating organisms (PAO) Storage of $X_{PHA}$ Aerobic storage of $X_{PP}$ Anoxic storage of $X_{PP}$ denitrification	: X <sub>PAO</sub> -1	·	$V_{ m 18,}$		Y <sub>PO4</sub> -1 -1			Y <sub>PO4</sub> 1 1 1	1 -Y <sub>PHA</sub> -Y <sub>PHA</sub>	
19	Anoxic storage of $X_{PP}$ denitrification			NO2	$V_{19,}$	-1			- 1	$-Y_{\rm PHA}$	
20 21	Aerobic growth of X <sub>PAO</sub> Anoxic growth of X <sub>PAO</sub>		$V_{20,N} V_{21,N}$	$^{ m IH4}_{ m IH4}$ $V_{21,}$	NO3	— <sup>1</sup> PBM — <sup>1</sup> PBM		1		$-rac{1}{Y_H}$	
22	denitrification (S <sub>NO2</sub> ) Anoxic growth of X <sub>PAO</sub> Amitrification (S )		$V_{22,N}$	NO2 IH4	$V_{22,}$	$-i_{\rm PBM}$		1	I	$-rac{1}{Y_H}$	
23	Lysis of X <sub>PAO</sub>		$V_{23,N}$	IH4	NO3	$V_{23,PO4}$		$1-f_{XI}$	-1		
24 25	Lysis of $X_{\rm PP}$ Lysis of $X_{\rm PHA}$					1			-1	$f_{\chi I}$	

# 4. Results and discussion

# 4.1. Investigation results

In this study, certain information regarding the raw wastewater characteristics was provided from a main manhole of southeast university in Wuxi city (China). Four testing runs with different operations were used for model calibration and parameter estimation and also four different runs for model simulation. Their values are shown in Table (4). According to OUR experiments, the values of the maximum growth rates of  $X_{\rm H}$ ,  $X_{\rm AOB}$ , and  $X_{\rm NOB}$  were 6.0, 1.4, and 0.4 day<sup>-1</sup>, respectively. Their rate constants for lysis and decay were 0.4, 0.08, and 0.04 day<sup>-1</sup>, respectively.

## 4.2. Sensitivity analysis (SN) and model calibration

The effects of frequently large uncertainties parameters in PITSF-SU process should be taken into account before starting in the simulation of this system via sensitivity analysis. The sensitivity (SN) of effluent components for some important parameters was analyzed based on 8% change of the standard values. All stoichiometric are five parameters and kinetic parameters are 52 parameters of the extension model. The influent components are 16 parameters including the influent flow rate, external flow of sludge recycles (two parameters). The sensitivity analysis of the above parameters ( $\zeta$ ) according to output components ( $\beta$ ) was calculated by the following formula [18].

$$(SN) = (d\beta/\beta)/(d\xi/\xi)$$
(19)

where  $(d\xi)$  is the change in the parameter value  $\xi$  and  $d\beta$  the change in the output  $\beta$ . According to sensitivity analysis, the output concentrations  $(\beta)$  have different sensitivities toward different parameters. This study showed that the effluent  $S_S$  of COD fraction observed to have a sensitivity of more than one (SN > 1) toward three parameters of  $\mu_{\rm H\prime}$ ,  $b_{\rm H\prime}$ ,  $Y_{\rm H}$ . It was also revealed that the effluent concentration of  $S_{\rm NH4}$ ,  $S_{\rm NO2}$ , and  $S_{\rm NO3}$ had a sensitivity of more than one (SN > 1) towards five (input  $S_{\text{NH4}}$ ,  $\mu_{\text{AOB}}$ ,  $q_{\text{pp}}$ ,  $Y_{\text{AOB}}$ ,  $Y_{\text{PO4}}$ ), eight parameters ( $\mu_{AOB}$ ,  $\mu_{NOB}$ ,  $\mu_{PAO}$ ,  $q_{pp}$ ,  $Y_H$ ,  $Y_{AOB}$ ,  $Y_{NOB}$ ,  $Y_{PO4}$ ), and four parameters influent flow rate ( $\mu_{AOB}$ ,  $Y_{H}$ ,  $Y_{PO4}$ ), respectively. The effluent phosphate  $(S_{PO4})$  was mainly sensitive toward seven parameters ( $S_{PO4}$ ,  $q_{PHA}$ ,  $q_{pp}$ ,  $\mu_{PA0}$ , K<sub>MAX</sub>, Y<sub>H</sub>, and Y<sub>PO4</sub>. The internal concentrations of  $S_{\rm S'},\,S_{\rm NH4'},\,S_{\rm NO2'},\,S_{\rm NO3'}$  and  $S_{\rm PO4}$  were also sensitive for the stoichiometric and kinetic parameters at the end of the anaerobic tank. Additionally, this work showed that 59 kinetic parameters gave a sensitivity

of more than one (SN > 1) according to the internal concentrations. According to the sensitivity analysis, the main parameters in activated sludge models are known to be approximately constant in domestic wastewater, the default values from previous studies [2] were used as shown in Table 3.

After analysis, the parameters of the model, the simulation data were calibrated to adjust coefficient values of the extension model, and thus, the simulation result by this model with these coefficients closely agree with the measured data. The model parameters are greatly dependent on environmental state conditions. The parameter values are estimated by minimizing the sum of squares  $(R^2)$  of the deviations between the experimental data and the model predictions with the objective function. The standard deviation for parameter calculation was required to be lower than 50% to ensure the validity of the parameters value obtained. An initial guess of these parameters is necessary to initiate the calibration procedure. To simplify the calibration process, it is desired to change as few constants as possible, because of the limited variability of some parameters. The selection of the parameters for calibration is mainly based on the result of sensitivity analysis.

## 4.3. Model validation

#### 4.3.1. Simulation of soluble components

The model evaluation is performed from the comparison between the measured and predicated values. The experimental data of four related runs real domestic wastewater are used for extension model evaluation. The simulated and experimental NH<sub>4</sub><sup>+</sup>-N, NO<sub>3</sub><sup>-</sup>-N, and PO<sub>4</sub>-P values of tank one, tank two, tank three, tank four, and tank five under different runs with a *C*/*N* ratio of (5.4, 6.7, 3.4, and 9.1) and *C*/*P* ratio of (45.2, 130.4, 27.63, and 52.23), respectively, as shown below:

4.3.1.1. Model validation of tank one. Fig. 6 shows the observed and predicated data of ammonia–N nitrate–N, and  $PO_4^-$ –P concentration of tank one under different runs. It has a good agreement between the observed and predicated data, whereas the sum of squares of the deviations ( $R_2$ ) of NH<sub>4</sub><sup>-</sup>-N, PO<sub>4</sub>–P, and NO<sub>3</sub><sup>-</sup>–N were 0.98, 0.99, and 0.97, respectively, at run 1, 0.98, 0.99, and 0.98, respectively, at run 2, 0.99, 0.98, and 0.97, respectively, at run 3 and 0.99, 0.99, and 0.97, respectively, at run 4.

Under anoxic condition, it was found from Fig. 6 that  $NH_4^-$ -N concentration was increased to 9.08, 9.6, 11.1, and 4.9 mg/L in runs 1, 2, 3, and 4, respectively,

Table 3 Definition and typical values for kinetic parameters

Heterotrophic organisms: X <sub>H</sub> $\mu_{\rm H}$ Maximum growth rate on substrate6.00g X, g $^{-1}$ X <sub>H</sub> d $^{-1}$ $\mu_{\rm GCB}$ Reduction factor for denitrification (S <sub>NG2</sub> )0.5- $\eta_{\rm SCBH}$ Reduction factor for denitrification (S <sub>NG3</sub> )0.6- $\eta_{\rm SCBH}$ Reduction factor for denitrification (S <sub>NG3</sub> )0.6- $\eta_{\rm SCBH}$ Rate constant for lysis and decay0.4d $^{-1}$ $\kappa_{\rm SCB}$ Saturation coefficient for oxygen0.2g O m $^{-3}$ $\kappa_{\rm K}$ Saturation coefficient for growth on $s_{\rm Sc}$ 4g COD m $^{-3}$ $\kappa_{\rm K}$ Saturation, coefficient for growth on acetate $S_{\rm N}$ 4g COD m $^{-3}$ $\kappa_{\rm NOH}$ Saturation, inhibition coefficient for $s_{\rm SCD}$ 0.5g N m $^{-3}$ $\kappa_{\rm SOH}$ Saturation, inhibition coefficient for $s_{\rm SCD}$ 0.5g N m $^{-3}$ $\kappa_{\rm SOH}$ Saturation, coefficient for sheaphate (nutrient)0.01g p m $^{-3}$ $\kappa_{\rm NH}$ Saturation coefficient for animonium (nutrient)0.01g p m $^{-3}$ $\kappa_{\rm AL}$ Saturation coefficient for animonium (nutrient)1g N m $^{-3}$ $\kappa_{\rm AL}$ Saturation coefficient for animonium (nutrient)0.01g N m $^{-1}$ $\kappa_{\rm AL}$ Saturation coefficient for animonium (nutrient)0.1g N m $^{-1}$ $\kappa_{\rm AL}$ Saturation coefficient for animonium (nutrient)0.01g N m $^{-1}$ $\kappa_{\rm AL}$ Saturation coefficient for animonium (nutrient)0.01g N m $^{-3}$ $\kappa_{\rm AL}$	Item	Description	20°C	Units
$\mu_{\rm th}$ Maximum growth rate on substrate6.00g X g $^{-1}$ X <sub>H</sub> d $^{-1}$ $\eta_{\rm GOH}$ Reduction factor for denitrification (S <sub>NO2</sub> )0.5- $\eta_{\rm OOH}$ Reduction factor for denitrification (S <sub>NO2</sub> )0.6- $\eta_{\rm OOH}$ Reduction factor for denitrification (S <sub>NO2</sub> )0.4d $^{-1}$ $K_{\rm CH}$ Saturation coefficient for growth on Sp4g COD m $^{-3}$ $K_{\rm H}$ Saturation coefficient for growth on Sp4g COD m $^{-3}$ $K_{\rm Ai}$ Saturation coefficient for growth on scalets S <sub>A</sub> 4g COD m $^{-3}$ $K_{\rm Aii}$ Saturation coefficient for Spoot0.5g N m $^{-3}$ KoosaSaturation /inhibition coefficient for Spoot0.5g N m $^{-3}$ KoosaSaturation coefficient for Spoot0.5g N m $^{-3}$ KousaSaturation coefficient for spoot0.5g N m $^{-3}$ KousaSaturation coefficient for spoot0.01g p m $^{-3}$ KautaSaturation coefficient for spoot0.01g p m $^{-3}$ KautaSaturation coefficient for aNone0.01g p m $^{-3}$ KautaSaturation coefficient for aNone0.01g N m $^{-3}$ KautaSaturation coefficient for anomonium (nutrient)0.5g O m $^{-3}$ <td>Heterotrophic organi</td> <td>isms: X<sub>H</sub></td> <td></td> <td></td>	Heterotrophic organi	isms: X <sub>H</sub>		
$q_{00}$ Maximum rate for fermentation3.3 $q_{X} \ge q^{-1} X_{H} d^{-1}$ $h_{NOM}$ Reduction factor for denitrification ( $S_{NOD}$ )0.5 $ h_{NOM}$ Rate constant for lysis and decay0.4 $d^{-1}$ $K_{O21}$ Saturation coefficient for growth on $S_{P}$ 4 $g \ COD \ m^{-3}$ $K_{R1}$ Saturation coefficient for formentation on $S_{A}$ 4 $g \ COD \ m^{-3}$ $K_{K1}$ Saturation coefficient for formentation on $S_{A}$ 4 $g \ COD \ m^{-3}$ $K_{NO1}$ Saturation inhibition coefficient for $S_{NO2}$ 0.5 $g \ N \ m^{-3}$ $K_{NO1}$ Saturation inhibition coefficient for $S_{NO2}$ 0.5 $g \ N \ m^{-3}$ $K_{NO1}$ Saturation coefficient for phosphate (nutrient)0.05 $g \ N \ m^{-3}$ $K_{NO1}$ Saturation coefficient for akalinity (HCO <sup>-1</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NL}$ Saturation coefficient for akalinity (HCO <sup>-1</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $N_{NO1}$ Maximum growth rate of $X_{AO0}$ 1.4 $d^{-1}$ $K_{O200}$ Saturation coefficient for akalinity (HCO <sup>-1</sup> )0.5 $g \ O m^{-3}$ $K_{NLA}$ Saturation coefficient for amonium (nutrient)0.01 $g \ P \ m^{-3}$ $N_{NO2}$ Saturation coefficient for akalinity (HCO <sup>-1</sup> )1 $g \ O m^{-3}$ $K_{NLA}$ Saturation coefficient for akalinity (HCO <sup>-1</sup> )0.5 $g \ O m^{-3}$ $K_{NLA}$ Saturation coefficient for amonium (nutrient)0.01 $g \ P \ m^{-3}$ $N_{NO2}$ Saturation coefficient for amonium (nutrien	$\mu_{ m H}$	Maximum growth rate on substrate	6.00	$g X_{\rm S} g^{-1} X_{\rm H} d^{-1}$
$\eta_{\text{NOM}}$ Reduction factor for denitrification ( $S_{\text{NO}2}$ )0.5- $\eta_{\text{NOM}}$ Rate constant for lysis and decay0.4d <sup>-1</sup> $K_{\text{DM}}$ Saturation, inhibition coefficient for oxygen0.2g C p m <sup>-3</sup> $K_{\text{H}}$ Saturation coefficient for growth on $S_{\text{T}}$ 4g COD m <sup>-3</sup> $K_{\text{R}}$ Saturation coefficient for growth on scatter $S_{\text{A}}$ 4g COD m <sup>-3</sup> $K_{\text{R}}$ Saturation inhibition coefficient for $S_{\text{NO2}}$ 0.5g N m <sup>-3</sup> $K_{\text{NO1}}$ Saturation, inhibition coefficient for $S_{\text{NO2}}$ 0.5g N m <sup>-3</sup> $K_{\text{NO1}}$ Saturation, inhibition coefficient for $S_{\text{NO2}}$ 0.5g N m <sup>-3</sup> $K_{\text{NO1}}$ Saturation, coefficient for $S_{\text{NO2}}$ 0.5g N m <sup>-3</sup> $K_{\text{NO1}}$ Saturation coefficient for phosphate (nutrient)0.01g p m <sup>-3</sup> $K_{\text{RL}}$ Saturation coefficient for annonnium (nutrient)0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $N_{\text{NO3}}$ Saturation coefficient for annonnium (nutrient)0.1g N m <sup>-3</sup> $K_{\text{RL}}$ Saturation coefficient for annonnium (nutrient)0.5g Q m <sup>-3</sup> $K_{\text{NA4}}$ Saturation coefficient for annonnium (nutrient)0.01g N m <sup>-3</sup> $K_{\text{NA5}}$ Saturation coefficient for annonnium (nutrient)0.01g N m <sup>-3</sup> $K_{\text{NA6}}$ Saturation coefficient for annonnium (nutrient)0.01g N m <sup>-3</sup> $K_{\text{NA5}}$ Saturation coefficient for annonnium (nutrient)0.01g N m <sup>-3</sup> $K_{\text{NA6}}$ Saturation coefficient for annonnium (nut	q <sub>fe</sub>	Maximum rate for fermentation	3.3	$g X_S g^{-1} X_H d^{-1}$
$\eta_{0.05H}$ Reduction factor for denitrification ( $S_{NC3}$ )0.6- $b_{th}$ Rate constant for Jysis and decay0.4d <sup>-1</sup> $K_{02H}$ Saturation coefficient for growth on $S_{T}$ 4g COD m <sup>-3</sup> $K_{H}$ Saturation coefficient for growth on acetale $S_A$ 4g COD m <sup>-3</sup> $K_{AH}$ Saturation coefficient for synce0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation (nihibition coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation/ nihibition coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation/ nihibition coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation coefficient for aphosphate (nutrient)0.01g p m <sup>-3</sup> $K_{ALX}$ Saturation coefficient for aphosphate (nutrient)0.01g p m <sup>-3</sup> $K_{ALX}$ Saturation coefficient for $N_{NOB}$ 1.4d <sup>-1</sup> $R_{OD}$ Baturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O_2 m <sup>-3</sup> Nitrifying arganisms, autotrophic (Ammonia exidizing bacteria) $X_{AOB}$ 1.4d <sup>-1</sup> $R_{OD}$ Baturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALXAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALXAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALXAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALXAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O_2 m <sup>-3</sup>	$\eta_{ m NO2H}$	Reduction factor for denitrification $(S_{NO2})$	0.5	-
$b_{11}$ Rate constant for lysis and decay0.4d^{-1} $K_{CRH}$ Saturation (inhibition coefficient for growth on $S_{\mu}$ 4g COD m^{-3} $K_{R6}$ Saturation coefficient for growth on acetate $S_{\Lambda}$ 4g COD m^{-3} $K_{R0H}$ Saturation (inhibition coefficient for $S_{NO2}$ 0.5g N m^{-3} $K_{NOH}$ Saturation/inhibition coefficient for $S_{NO2}$ 0.5g N m^{-3} $K_{NOH}$ Saturation/inhibition coefficient for $S_{NO2}$ 0.5g N m^{-3} $K_{NOH}$ Saturation/inhibition coefficient for $S_{NO2}$ 0.5g N m^{-3} $K_{NOH}$ Saturation coefficient for ammonium (nutrient)0.01g p m^{-3} $K_{H1}$ Saturation coefficient for alkalinity (HCO <sup>3</sup> )0.1mole HCO <sup>3</sup> m^{-3} $Nitrifying organisms, autorphysic (Ammonia calkizing bacteria) X_{AOB}$ 1.4d^{-1} $\mu_{NOR}$ Maximum growth rate of $X_{AOB}$ 1.4d^{-1} $K_{02AOB}$ Saturation coefficient for alkalinity (HCO <sup>3</sup> )0.5mole HCO <sup>3</sup> m^{-3} $K_{02AOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{02AOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m^{-3} $K_{02AOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{02AOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{02AOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g N m^{-3} $K_{02AOB}$ Saturation coefficient for	$\eta_{ m NO3H}$	Reduction factor for denitrification $(S_{NO3})$	0.6	-
$K_{02H}$ Saturation /inhibition coefficient for growth on $S_{5}$ 4g COD m <sup>-3</sup> $K_{6}$ Saturation coefficient for growth on $S_{5}$ 4g COD m <sup>-3</sup> $K_{60H}$ Saturation coefficient for growth on acetate $S_{A}$ 4g COD m <sup>-3</sup> $K_{60H}$ Saturation/inhibition coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation/inhibition coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation/inhibition coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation coefficient for annonium (nutrient)0.01g p m <sup>-3</sup> $K_{HH}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $N_{HH}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $N_{AB}$ Maximum growth rate of $X_{AOB}$ 1.4d <sup>-1</sup> $K_{2AO0}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $N_{AB}$ Maximum growth rate of $X_{AOB}$ 0.5g O <sub>2</sub> m <sup>-3</sup> $K_{MLAO0}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $N_{MIT}$ Maximum growth rate of $X_{NOB}$ 0.4d <sup>-1</sup> $K_{ALXON}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.5g O <sub>2</sub> m <sup>-3</sup> $K_{MLAO0}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{MLAO0}$ Saturation coefficient for alkalnity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{MLAO0}$ Saturation coefficient for annonium (nutrient)0.01g P m <sup></sup>	$b_{ m H}$	Rate constant for lysis and decay	0.4	$d^{-1}$
$K_{\mu}$ Saturation coefficient for growth on $S_{P}$ 4g COD m <sup>-3</sup> $K_{AH}$ Saturation coefficient for growth on acetate $S_A$ 4g COD m <sup>-3</sup> $K_{AH}$ Saturation coefficient for $S_{NO2}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation /inhibition coefficient for $S_{NO3}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation /inhibition coefficient for $S_{NO3}$ 0.5g N m <sup>-3</sup> $K_{NOH}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{HL}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{PL}$ Maximum growth rate of $X_{AOB}$ 1.4d <sup>-1</sup> $h_{OO}$ Decay rate of $X_{AOB}$ 0.08d <sup>-1</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O <sub>2</sub> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O <sub>2</sub> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O <sub>2</sub> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O <sub>2</sub> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O <sub>2</sub> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for annonium (nutrient)0.01g N m <sup>-3</sup> $K_{NAOB}$ Saturation coefficient for annonium (nutrient)0.5g O <sub>2</sub> m <sup>-3</sup>	K <sub>O2H</sub>	Saturation/inhibition coefficient for oxygen	0.2	$g O_2 m^{-3}$
$K_{g}$ Saturation coefficient for growth on acetate $S_A$ 4g COD m^{-3} $K_{NG2H}$ Saturation coefficient for $S_{NG2}$ 0.5g N m^{-3} $K_{NO2H}$ Saturation /inhibition coefficient for $S_{NG3}$ 0.5g N m^{-3} $K_{NO4H}$ Saturation /inhibition coefficient for $S_{NG3}$ 0.5g N m^{-3} $K_{NO4H}$ Saturation coefficient for phosphate (nutrient)0.01g p m^{-3} $K_{NH4}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $Nitrifying organisms, autotrophic (Ammonia oxidizing bacteria) XAC081.4d^{-1}h_{O60}Maximum growth rate of X_{AO61}0.5g O2 m-3K_{ALAB}Saturation coefficient for alkalinity (HCO-3)0.5mole HCO-3 m-3K_{ALAB}Saturation coefficient for ammonium (nutrient)1g N m-3K_{AD30}Saturation coefficient for phosphorus (nutrient)0.01g P m-3Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) XAOB0.4d-1h_{O60}Decay rate of X_{NO8}0.04d-1h_{O60}Decay rate of X_{NO8}0.04d-1h_{O60}Decay rate of X_{NO8}0.04d-1h_{O60}Decay rate of X_{NO8}0.04d-1h_{O60}Decay rate of X_{NO8}0.4d-1h_{O60}Decay rate of X_{NO8}0.4d-1h_{O60}Decay rate of X_{NO8}0.4d-1h_{O60}Decay rate of X_{NO8}0.04<$	$K_{\rm FH}$	Saturation coefficient for growth on $S_{\rm F}$	4	$g \text{ COD } m^{-3}$
$K_{\rm HL}$ Saturation coefficient for ${\rm S}_{\rm NO2}$ 4g COD m^{-3} $K_{\rm NO3H}$ Saturation /inhibition coefficient for ${\rm S}_{\rm NO3}$ 0.5g N m^{-3} $K_{\rm NO4H}$ Saturation /inhibition coefficient for ${\rm S}_{\rm NO3}$ 0.5g N m^{-3} $K_{\rm NO4H}$ Saturation coefficient for annonium (nutrient)0.01g p m^{-3} $K_{\rm NH}$ Saturation coefficient for phosphate (nutrient)0.01g p m^{-3} $K_{\rm NH}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m^{-3} $K_{\rm NH}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLR}$ Decay rate of $X_{\rm AOB}$ 0.08d^{-1} $K_{\rm NLR}$ Saturation coefficient for anyonium (nutrient)1g N m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{\rm NLRAOB}$ Saturation coefficient for anyonium (nutrient)0.01 <td< td=""><td>K<sub>fe</sub></td><td>Saturation coefficient for fermentation on <math>S_A</math></td><td>4</td><td><math>g \text{ COD } m^{-3}</math></td></td<>	K <sub>fe</sub>	Saturation coefficient for fermentation on $S_A$	4	$g \text{ COD } m^{-3}$
Kuch Kuch	K <sub>AH</sub>	Saturation coefficient for growth on acetate $S_A$	4	g COD m <sup>-3</sup>
KuoniSaturation (inhibition coefficient for $5_{NO3}$ 0.5g N m^3KNOAHSaturation (inhibition coefficient for $5_{NO3}$ 0.5g N m^3KHSaturation coefficient for ammonium (nutrient)0.01g P m^3KHSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m^-3Nitrifying organisms, autotrophic (Ammonia oxidizing bacteria) $X_{AOB}$ 1.4d^{-1}NonMaximum growth rate of $X_{AOB}$ 0.08d^{-1}KOADDecay rate of $X_{AOB}$ 0.08d^{-1}KOADSaturation coefficient for oxygen0.5g O <sub>2</sub> m^-3KNHAOBSaturation coefficient for oxygen0.5mole HCO <sup>-3</sup> m^-3KNHAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^-3KNHAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^-3KNAAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.01g P m^-3Nitrifying organisms, autorophic (Nitrie toxidizing bacteria) XAOB4d^{-1}HNOBDecay rate of X <sub>NOB</sub> 0.04d^-1KouxoonSaturation coefficient for oxygen0.5g O <sub>2</sub> m <sup>-3</sup> KutstonSaturation coefficient for oxygen0.5mole HCO <sup>-3</sup> m^-3KutstonSaturation coefficient for oxygen0.5mole HCO <sup>-3</sup> m^-3KauxonSaturation coefficient for oxygen0.5mole HCO <sup>-3</sup> m^-3KauxonSaturation coefficient for oxygen0.5mole HCO <sup>-3</sup> m^-3KauxonSaturation coefficient for oxygen <td< td=""><td>K<sub>NO2H</sub></td><td>Saturation/inhibition coefficient for <math>S_{NO2}</math></td><td>0.5</td><td><math>g N m^{-3}</math></td></td<>	K <sub>NO2H</sub>	Saturation/inhibition coefficient for $S_{NO2}$	0.5	$g N m^{-3}$
Kyonh Kyuch KyuthiSaturation (inhibition coefficient for shxon kythick aturation coefficient for ammonium (nutrient)0.05g N m^{-3} g N m^{-3}Kyth Kyth Kattaration coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m^{-3}KALK Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m^{-3}Waon Maximum growth rate of XAOB0.08d <sup>-1</sup> Kozon Saturation (inhibition coefficient for oxygen0.08d <sup>-1</sup> Kozon Saturation coefficient for almonium (nutrient)1g N m^{-3}KatkAOB Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3}Nitrifying organisms, autotrophic (Numorosorus (nutrient)0.01g P m <sup>-3</sup> Nitrifying organisms, autotrophic (Numorosorus (nutrient)0.01g P m <sup>-3</sup> Nitrifying organisms, autotrophic (Numorosorus (nutrient)0.01g N m <sup>-3</sup> Kozons Saturation coefficient for asygen0.5g O_2 m <sup>-3</sup> Nobe Maximum growth rate of XNOB0.4d <sup>-1</sup> Kozons Saturation coefficient for oxygen0.5g O_2 m <sup>-3</sup> Kozons Saturation coefficient for ammonium (nutrient)0.5g N m <sup>-3</sup> Kozons Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> Kozons Saturation coefficient for phosphorus (nutrient)0.01g N m <sup>-3</sup> Kozons Saturation coefficient for oxygen0.5g O_2 m <sup>-3</sup> Kozons Saturation coefficient for particulate CDD0.1g N m <sup>-3</sup> Kozons Saturation coefficient for particulate CDD0.1g N m	K <sub>NO3H</sub>	Saturation/inhibition coefficient for $S_{NO3}$	0.5	$g N m^{-3}$
Keinth Kuith KuithSaturation coefficient for anonium (nutrient)0.05g N m^3 g p m^3 Katk Saturation coefficient for alkalinity (HCO <sup>3</sup> )0.01g p m^3 mole HCO <sup>-3</sup> m^-3Nthrifying organisms, autotrophic (Annunoia oxidizing bacteria) $X_{AOB}$ 1.4d^{-1} $h_{AOB}$ Maximum growth rate of $X_{AOB}$ 0.08d^{-1} $h_{AOB}$ Decay rate of $X_{AOB}$ 0.08d^{-1} $h_{AOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5g O_2 m^{-3}KSHADBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3}KNHADBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3}KNHADBSaturation coefficient for phosphorus (nutrient)0.01g P m <sup>-3</sup> Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) $X_{AOB}$ 0.4d^{-1} $h_{OOB}$ Decay rate of $X_{NOB}$ 0.04d^{-1} $h_{OOB}$ Saturation coefficient for oxygen0.5g O_2 m <sup>-3</sup> $K_{ALNOB}$ Saturation coefficient for annonium (nutrient)0.01g N m <sup>-3</sup> $K_{ALNOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALNOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALNOB}$ Saturation coefficient for oxygen0.2g O_2 m <sup>-3</sup> $K_{ALNOB}$ Saturation coefficient for oxygen0.2g O_2 m <sup>-3</sup> $K_{ALNOB}$ Saturation coefficient for oxygen0.2g O_2 m <sup>-3</sup> $K_{ALNOB}$ Saturation co	K <sub>NOxH</sub>	Saturation/inhibition coefficient for $S_{NO3}$	0.5	$g N m^{-3}$
$K_{\text{HL}}$ Saturation coefficient for phosphate (nutrient)0.01 $\stackrel{\circ}{\text{g}}$ p m <sup>-3</sup> $K_{\text{ALX}}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $Nitrifying organisms, autotrophic (Ammonia axidizing bacteria) X_{AOB}1.4d-1A_{\text{OAD}}Decay rate of X_{AOB}0.08d-1\delta_{\text{CACOB}}Saturation /inhibition coefficient for oxygen0.5g O2 m-3K_{\text{NLLAOB}}Saturation coefficient for ammonium (nutrient)1g N m-3K_{\text{NLLAOB}}Saturation coefficient for phosphorus (nutrient)0.01g P m-3Nitrifying organisms, autotrophic (Nitrite axidizing bacteria) X_{AOB}0.4d-1K_{\text{NLB}}Saturation coefficient for anomonium (nutrient)0.01g N m-3Nitrifying organisms, autotrophic (Nitrite axidizing bacteria) X_{AOB}0.4d-1K_{\text{NDB}}Saturation coefficient for anomonium (nutrient)0.5g O2 m-3K_{\text{NDB}}Saturation coefficient for ammonium (nutrient)0.01g N m-3K_{\text{NDB}}Saturation coefficient for ammonium (nutrient)0.01g N m-3K_{NIXKOB}Saturation coefficient for ammonium (nutrient)0.01g N m-3K_{NIXKOB}Saturation coefficient for anomonium (nutrient)0.01g N m-3K_{NIXKOB}Saturation coefficient for ammonium (nutrient)0.01g N m-3K_{NIXKOB}Saturation coefficient for anomonium (nutrient)0.01g N m-3K_{NIXKOB}Saturation coefficient for ang$	K <sub>NH4H</sub>	Saturation coefficient for ammonium (nutrient)	0.05	$g N m^{-3}$
$K_{\rm LLX}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.1mole HCO <sup>-3</sup> m <sup>-3</sup> Nitrifying organisms, autotrophic (Ammonia oxidizing bacteria) $X_{\rm AOB}$ 1.4d <sup>-1</sup> $h_{OB}$ Maximum growth rate of $X_{\rm AOB}$ 0.08d <sup>-1</sup> $h_{OB}$ Saturation coefficient for oxygen0.5g O <sub>2</sub> m <sup>-3</sup> $K_{SNHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NLAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NLAOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m <sup>-3</sup> $Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) X_{AOB}0.4d-1K_{O2NOB}Saturation /inhibition coefficient for oxygen0.5g O2 m-3K_{NILNOB}Saturation coefficient for ammonium (nutrient)0.01g N m-3K_{NILNOB}Saturation coefficient for ammonium (nutrient)0.5mole HCO-3 m-3K_{NILNOB}Saturation coefficient for alkalinity (HCO-3)0.5mole HCO-3 m-3K_{NILNOB}Saturation coefficient for alkalinity (HCO-3)0.5mole HCO-3 m-3K_{NILNOB}Saturation coefficient for phosphorus (nutrient)0.01g P m-3K_{NILNOB}Saturation coefficient for phosphorus (nutrient)0.5mole HCO-3 m-3K_{NILNOB}Saturation coefficient for oxygen0.2g O2 m-3K_{NILNOB}Saturation coefficient for notic for oxygen0.2g O2 m-3K_{NILNOB}Saturation coeff$	K <sub>PH</sub>	Saturation coefficient for phosphate (nutrient)	0.01	$g p m^{-3}$
Nitrifying organisms, autotrophic (Ammonia axidizing bacteria) $X_{AOB}$ 1.4 d <sup>-1</sup> $\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ 0.98 d <sup>-1</sup> $\mu_{AOB}$ Decay rate of $X_{AOB}$ 0.08 d <sup>-1</sup> $K_{02AOB}$ Saturation coefficient for oxygen 0.5 g $D_2$ m <sup>-3</sup> $K_{NIAAOB}$ Saturation coefficient for ammonium (nutrient) 1 g N m <sup>-3</sup> $K_{ALKAOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NADOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Maximum growth rate of $X_{NOB}$ 0.4 d <sup>-1</sup> $K_{O2XOB}$ Maximum growth rate of $X_{NOB}$ 0.4 d <sup>-1</sup> $K_{O2XOB}$ Saturation (nubibilion coefficient for oxygen 0.5 g $O_2$ m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for ammonium (nutrient) 0.01 g N m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for ammonium (nutrient) 0.01 g N m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for ammonium (nutrient) 0.5 g $O_2$ m <sup>-3</sup> $K_{NLNOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $K_{NOB}$ Saturation coefficient for antice for 0.6 - $M_R$ Anaerobic hydrolysis reduction factor 0.4 - $M_{NOS}$ Saturation/inhibition coefficient for nitrite and nitrate 0.5 g N m <sup>-3</sup> $K_{NOS}$ Saturation coefficient for particulate COD 0.1 g X <sub>S</sub> g <sup>-1</sup> X <sub>H</sub> $Phosphorus-accumulating organisms: XPAO 0-1 M_{PAO} Maximum growth rate of PAO 1.2 d-1M_{NOSNO} Reduction factor for anoxic activity 0.8 -M_{PAO} Maximum growth rate of PAO 1.2 d-1M_{NOSNO} Reluction factor for anoxic activity 0.8 -M_{PAO} Maximum growth rate of$	K <sub>ALK</sub>	Saturation coefficient for alkalinity $(HCO^{-3})$	0.1	mole HCO <sup>-3</sup> m <sup>-3</sup>
$\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ 1.4 $d^{-1}$ $\lambda_{AOB}$ Decay rate of $X_{AOB}$ 0.08 $d^{-1}$ $\lambda_{GAOB}$ Saturation (inhibition coefficient for oxygen0.5 $gO_2 m^{-3}$ $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{AOB}$ Saturation coefficient for phosphorus (nutrient)0.01 $gP m^{-3}$ Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) $X_{AOB}$ 0.4 $d^{-1}$ $NooB$ Maximum growth rate of $X_{NOB}$ 0.04 $d^{-1}$ $K_{ONOB}$ Saturation coefficient for oxygen0.5 $gO_2 m^{-3}$ $K_{NIRNOB}$ Saturation coefficient for ammonium (nutrient)0.01 $gN m^{-3}$ $K_{NONOB}$ Saturation coefficient for ammonium (nutrient)0.5 $gN m^{-3}$ $K_{NONOB}$ Saturation coefficient for ahkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALKNOB}$ Saturation coefficient for phosphorus (nutrient)0.01 $gP m^{-3}$ $K_{MLKNOB}$ Saturation coefficient for phosphorus (nutrient)0.01 $gP m^{-3}$ $K_{ML}$ Hydrolysis reduction factor0.4 $ K_{R}$ Hydrolysis reduction factor0.4 $ K_{RS}$ Saturation coefficient for oxygen0.2 $gO_2 m^{-3}$ $K_{NOS}$ Saturation (inhibition coefficient for oxygen0.2 $gO_2 m^{-3}$ $K_{NOS}$ Saturation (inhibition coefficient for oxygen0.2 $gO_2 m^{-3}$ $K_{NOS}$ Saturation (inhibition coefficient for oxygen <td>Nitrifying organism</td> <td>s, autotrophic (Ammonia oxidizing bacteria) X<sub>AOB</sub></td> <td></td> <td></td>	Nitrifying organism	s, autotrophic (Ammonia oxidizing bacteria) X <sub>AOB</sub>		
	$\mu_{AOB}$	Maximum growth rate of X <sub>AOB</sub>	1.4	$d^{-1}$
Ko2AOBSaturation/inhibition coefficient for axmonium (nutrient)0.5g O2 m^{-3}KNIEAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3}KALKAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.01g P m^{-3}Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) XAOB0.4d^{-1}NOBMaximum growth rate of XNOB0.4d^{-1}NOBDecay rate of XNOB0.04d^{-1}NOBSaturation coefficient for axmonium (nutrient)0.01g N m^{-3}KOZNOBSaturation coefficient for ammonium (nutrient)0.01g N m^{-3}KNIENOBSaturation coefficient for ammonium (nutrient)0.5g N m^{-3}KNIENOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> KNONOSaturation coefficient for phosphorus (nutrient)0.01g P m <sup>-3</sup> Hydrolysis rate constant3d <sup>-1</sup> HyosAnaerobic hydrolysis reduction factor0.6-NoASAnaerobic hydrolysis reduction factor0.4-KosSaturation/inhibition coefficient for oxygen0.2g N m <sup>-3</sup> KyosSaturation/inhibition coefficient for oxygen0.2<	b <sub>AOB</sub>	Decay rate of X <sub>AOB</sub>	0.08	$d^{-1}$
KNHAOBSaturation coefficient for ammonium (nutrient)1g N m <sup>-3</sup> KALKAOBSaturation coefficient for phosphorus (utrient)0.5mole HCO <sup>-3</sup> m <sup>-3</sup> Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) XAOB0.01g P m <sup>-3</sup> Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) XAOB0.4d <sup>-1</sup> NobDecay rate of XNOB0.04d <sup>-1</sup> KONBDecay rate of XNOB0.04d <sup>-1</sup> KONBSaturation /inhibition coefficient for oxygen0.5g O <sub>2</sub> m <sup>-3</sup> KNINNOBSaturation coefficient for ammonium (nutrient)0.01g N m <sup>-3</sup> KALKNOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> KALKNOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> K <sub>NALKNOB</sub> Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> K <sub>NALKNOB</sub> Saturation coefficient for phosphorus (nutrient)0.01g P m <sup>-3</sup> Hydrolysis rate constant3d <sup>-1</sup> -Hydrolysis rate constant3d <sup>-1</sup> NoxasAnoxic hydrolysis reduction factor0.6-N <sub>6</sub> Anaerobic hydrolysis reduction factor0.4-K <sub>025</sub> Saturation /inhibition coefficient for oxygen0.2g O <sub>2</sub> m <sup>-3</sup> K <sub>NOS5</sub> Saturation /inhibition coefficient for oxygen0.2g O <sub>2</sub> m <sup>-3</sup> K <sub>NOS5</sub> Saturation /inhibition coefficient for oxygen0.2g O <sub>2</sub> m <sup>-3</sup> K <sub>NOS5</sub> Saturation /inhibition coefficient for oxygen	K <sub>O2AOB</sub>	Saturation/inhibition coefficient for oxygen	0.5	$g O_2 m^{-3}$
$K_{ALKAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m <sup>-3</sup> Nitrifying organisms, autorophic (Nitrite oxidizing bacteria) $X_{AOB}$	K <sub>NH4AOB</sub>	Saturation coefficient for ammonium (nutrient)	1	$g N m^{-3}$
$K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m^{-3}Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) X <sub>AOB</sub> $V_{AOB}$ $0.4$ $d^{-1}$ $PNOB$ Decay rate of $X_{NOB}$ 0.04 $d^{-1}$ $P_{NOB}$ Decay rate of $X_{NOB}$ 0.04 $d^{-1}$ $K_{OZNOB}$ Saturation coefficient for oxygen0.5g O <sub>2</sub> m^{-3} $K_{NLNOB}$ Saturation coefficient for ammonium (nutrient)0.01g N m^{-3} $K_{NLNOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{ALKNOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m^{-3} $Hydrolysis of particulate substrate: X_SX_SX_SX_SK_{II}Hydrolysis reduction factor0.6-\eta_{Pa}Anaerobic hydrolysis reduction factor0.4-K_{OZS}Saturation coefficient for oxygen0.2g O2 m^{-3}K_{NOS}Saturation/inhibition coefficient for oxygen0.1g XB g s-1 XHPhosphorus-accumulating organisms: X_{PAO}0.1g XB g s-1 XHq_{PhA}Rate constant for storage of X_{PHA} (base X_{PP})3.3g XPHA g-1 XPAO d-1q_{PhA}Rate constant for storage of X_{PP}0.2d-1q_{PhA}Rate for lysis of X_{PAO}0.2d-1q_{PhA}Rate for lysis of X_{PP}0.2d-1q_{PhA}Rate constant for storage of X_{PP}0.2d-1q_{PhA}Rate fo$	K <sub>ALKAOB</sub>	Saturation coefficient for alkalinity (HCO <sup>-3</sup> )	0.5	mole HCO <sup>-3</sup> m <sup>-3</sup>
Nitrifying organisms, autotrophic (Nitrite oxidizing bacteria) $X_{AOB}$ $\mu_{NOB}$ Maximum growth rate of $X_{NOB}$ 0.4 d <sup>-1</sup> $K_{O2NOB}$ Decay rate of $X_{NOB}$ 0.004 d <sup>-1</sup> $K_{O2NOB}$ Saturation (inhibition coefficient for oxygen 0.5 g O <sub>2</sub> m <sup>-3</sup> $K_{NHANOB}$ Saturation coefficient for ammonium (nutrient) 0.011 g N m <sup>-3</sup> $K_{NO2NOB}$ Saturation coefficient for ammonium (nutrient) 0.5 g N m <sup>-3</sup> $K_{NO2NOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) 0.5 mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NENOB}$ Saturation coefficient for phosphorus (nutrient) 0.01 g P m <sup>-3</sup> $Hydrolysis of particulate substrate: X_s$ $K_h$ Hydrolysis rate constant 3 d <sup>-1</sup> $\eta_{NOAS}$ Anoxic hydrolysis reduction factor 0.6 - $\eta_k$ Anaerobic hydrolysis reduction factor 0.4 - $K_{NOXS}$ Saturation coefficient for particulate COD 0.1 g $X_s g^{-1} X_H$ $Phosphorus-accumulating organisms: X_{PAO}q_{PLA} Rate constant for storage of X_{PLA} (base X_{PP}) 3.3 g X_{PLA} g^{-1} X_{PAO} d^{-1}\eta_{NOAPAO} Reduction factor for anoxic activity 0.8 -p_{PAO} Maximum growth rate of PAO 1.2 d-1\eta_{NOAPAO} Reduction factor for anoxic activity 0.8 -p_{PAO} Maximum growth rate of PAO 2.2 d-1\eta_{NOAPAO} Reduction factor for anoxic activity 0.8 -p_{PAO} Saturation /inhibition coefficient for oxygen 0.2 d-1K_{D2D} Saturation factor for anoxic activity 0.8 -p_{PAO} Rate for lysis of X_{PAO} 0.2 d-1f_{PAO} Maximum growth rate of PAO 1.2 d-1f_{NOAPAO} Reduction factor for anoxic activity 0.8 -f_{PAO} Saturation coefficient for oxygen 0.2 g O2 m-3K_{NENO} Saturation coefficient for oxygen 0.2 g O2 m-3K_{PAO} Saturation coefficient for oxygen 0.2 d-1K_{D2PAO} Saturation coefficient for anoxic activity 0.8 -f_{PAO} Saturation coefficient for acteate S_A 4 g COD m-3K_{NENPAO} Saturation coefficient for acteate S_A 4 g COD m-3K_{NENPAO} Saturation coefficient for ammonium (nutrient) 0.05 g N m-3K_{PAO} Saturation coefficient for ammonium (nutrient) 0.05 g N$	K <sub>PAOB</sub>	Saturation coefficient for phosphorus (nutrient)	0.01	$g P m^{-3}$
$\mu_{NOB}$ Maximum growth rate of $\tilde{X}_{NOB}$ 0.4d^{-1} $b_{NOB}$ Decay rate of $X_{NOB}$ 0.04d^{-1} $K_{O2NOB}$ Saturation /inhibition coefficient for oxygen0.5g O_2 m^{-3} $K_{NHANOB}$ Saturation coefficient for ammonium (nutrient)0.01g N m^{-3} $K_{NENNOB}$ Saturation coefficient for ammonium (nutrient)0.5g N m^{-3} $K_{NLKNOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m^{-3} $Hydrolysis of particulate substrate: X_SX_SNoxsAnoxic hydrolysis reduction factor0.6H_RAnoxic hydrolysis reduction factor0.4-K_{O2SS}Saturation /inhibition coefficient for oxygen0.2g O_2 m^{-3}K_{NOAS}Saturation /inhibition coefficient for oxygen0.2g N m^{-3}K_{O2SS}Saturation /inhibition coefficient for oxygen0.1g X_S g^{-1} X_HPhosphorus-accumulating organisms: X_{PAO}X_{PAO}X_{PAO}X_{PAO}q_{PIA}Rate constant for storage of X_{PIA} (base X_{PP})3.3g X_{PIA} g^{-1} X_{PAO} d^{-1}q_{PAO}Maximum growth rate of PAO1.2d^{-1}\eta_{NOSPAO}Reduction factor for anoxic activity0.8-b_{PAO}Maximum growth rate of PAO0.2d^{-1}q_{PAO}Maximum growth rate of PAO0.2d^{-1}h_{PAO}Rate for lysis of X_{PPA}0.2d^{-1}b_{PAO}Saturation coefficient for oxygen0.2d^{-1}$	Nitrifying organism	s, autotrophic (Nitrite oxidizing bacteria) X <sub>AOB</sub>		0
$b_{NOB}$ Decay rate of $X_{NOB}$ 0.04 $d^{-1}$ $K_{O2NOB}$ Saturation /inhibition coefficient for oxygen0.5 $g O_2 m^{-3}$ $K_{N1HNOB}$ Saturation coefficient for ammonium (nutrient)0.01 $g N m^{-3}$ $K_{N02NOB}$ Saturation coefficient for ammonium (nutrient)0.5 $g N m^{-3}$ $K_{N02NOB}$ Saturation coefficient for ammonium (nutrient)0.5 $g N m^{-3}$ $K_{N02NOB}$ Saturation coefficient for phosphorus (nutrient)0.01 $g P m^{-3}$ $Hydrolysis of particulate substrate: X_SK_hHydrolysis reduction factor0.6 \eta_{NOXS}Anoxic hydrolysis reduction factor0.4 K_{O2S}Saturation /inhibition coefficient for oxygen0.2g O_2 m^{-3}K_{NOXS}Saturation /inhibition coefficient for nitrite and nitrate0.5g N m^{-3}K_{NOXS}Saturation /inhibition coefficient for nitrite and nitrate0.5g N m^{-3}K_{NOXS}Saturation coefficient for particulate COD0.1g X_S g^{-1} X_HPhosphorus-accumulating organisms: X_{PAO}q_{PP}1.5g X_{PHA} g^{-1} X_{PAO} d^{-1}\eta_{NOXPAO}Rate constant for storage of X_{PP}0.8 \mu_{PAO}Maximum growth rate of PAO1.2d^{-1}\eta_{NOXPAO}Rate for lysis of X_{PPA}0.2d^{-1}h_{PAO}Rate for lysis of X_{PPA}0.2d^{-1}h_{PAO}Saturation coefficient for oxygen0.2g O_2 m^{-3}K_{NAPAO}$	$\mu_{\rm NOB}$	Maximum growth rate of $X_{NOB}$	0.4	$d^{-1}$
$K_{02NOB}$ Saturation/inhibition coefficient for oxygen0.5g $O_2 m^{-3}$ $K_{NHANOB}$ Saturation coefficient for ammonium (nutrient)0.01g N m^{-3} $K_{NO2NOB}$ Saturation coefficient for ammonium (nutrient)0.5g N m^{-3} $K_{NLKNOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m^{-3} $K_{NENOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m^{-3}Hydrolysis of particulate substrate: $X_S$ $X_K$ $X_K$ $K_h$ Hydrolysis reduction factor0.6 $ \eta_{fe}$ Anaerobic hydrolysis reduction factor0.4 $ K_{O2S}$ Saturation coefficient for particulate COD0.1g N m^{-3} $K_{NOXS}$ Saturation coefficient for particulate COD0.1g X_S g^{-1} X_HPhosphorus-accumulating organisms: $X_{PAO}$ $X_{PHA}$ $X_{PAA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> $q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> $q_{NOXPAO}$ Reduction factor for anxiz activity0.8 $ h_{PAO}$ Maximum growth rate of PAO1.2d <sup>-1</sup> $\eta_{NOXPAO}$ Rate for lysis of $X_{PAO}$ 0.2d <sup>-1</sup> $h_{PAO}$ Saturation coefficient for oxygen0.2g C_1^{-1} $h_{PAO}$ Maximum growth rate of PAO1.2d <sup>-1</sup> $h_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2d <sup>-1</sup> $h_{PAO}$ Saturation coefficient for oxygen0.2g C_1^{-1} $h_{PAO}$ Saturation coefficient	$b_{\rm NOB}$	Decay rate of X <sub>NOB</sub>	0.04	$d^{-1}$
$K_{\rm NH4NOB}$ Saturation coefficient for ammonium (nutrient)0.01 $g~N~m^{-3}$ $K_{\rm NO2NOB}$ Saturation coefficient for anmonium (nutrient)0.5 $g~N~m^{-3}$ $K_{\rm ALKNOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{\rm PNOB}$ Saturation coefficient for phosphorus (nutrient)0.01 $g~P~m^{-3}$ $Hydrolysis of particulate substrate: X_5K_hHydrolysis rate constant3d^{-1}N_{\rm NOXS}Anoxic hydrolysis reduction factor0.6 \eta_{\rm fe}Anaerobic hydrolysis reduction factor0.4 K_{\rm O2S}Saturation/inhibition coefficient for nitrite and nitrate0.5g~N~m^{-3}K_{\rm NOXS}Saturation/inhibition coefficient for nitrite and nitrate0.5g~N~m^{-3}K_{\rm NOXS}Saturation coefficient for particulate COD0.1g~X_{\rm S}~g^{-1}~X_{\rm H}Phosphorus-accumulating organisms: X_{PAO}1.2d^{-1}q_{\rm PHA}Rate constant for storage of X_{\rm PHA} (base X_{\rm PP})3.3g~X_{\rm PHA}~g^{-1}~X_{\rm PAO}~d^{-1}q_{\rm PAO}Maximum growth rate of PAO1.2d^{-1}q_{\rm NORPAO}Reduction factor for anoxic activity0.8 b_{\rm PAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}h_{\rm NORPAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}f_{\rm PAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}h_{\rm PAO}Saturation coefficient for oxygen0.2g~0_2~m^{-3}$	K <sub>O2NOB</sub>	Saturation/inhibition coefficient for oxygen	0.5	$g O_2 m^{-3}$
KNO2NOBSaturation coefficient for ammonium (nutrient)0.5 $g$ N m <sup>-3</sup> KALKNOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> KPNOBSaturation coefficient for phosphorus (nutrient)0.01 $g$ P m <sup>-3</sup> Hydrolysis of particulate substrate: $X_S$ $X_h$ Hydrolysis rate constant3 $d^{-1}$ $\eta_{NOXS}$ Anoxic hydrolysis reduction factor0.6 $ \eta_{fe}$ $\Lambda_{nacrobic hydrolysis reduction factor0.4 K_{O2S}Saturation/inhibition coefficient for oxygen0.2g O2 m-3K_{NOxS}Saturation coefficient for particulate COD0.1g XS g^{-1} XHPhosphorus-accumulating organisms: X_{PAO}0.1g XS g^{-1} XHq_{PHA}Rate constant for storage of X_{PPA}1.5g XPHA g^{-1} XPAO d^{-1}q_{PAO}Maximum growth rate of PAO1.2d^{-1}\eta_{NOXPAO}Reduction factor for anoxic activity0.8 p_{PAO}Rate for lysis of X_{PAO}0.2d^{-1}h_{NOXPAO}Saturation coefficient for oxygen0.2d^{-1}h_{PAO}Maximum growth rate of PAO1.2d^{-1}h_{PAO}Rate for lysis of X_{PAO}0.2d^{-1}h_{PAO}Rate for lysis of X_{PAO}0.2d^{-1}h_{PAO}Saturation coefficient for oxygen0.2d^{-1}h_{PAO}Saturation coefficient for oxygen0.2d^{-1}h_{PAO}Saturation c$	K <sub>NH4NOB</sub>	Saturation coefficient for ammonium (nutrient)	0.01	$g N m^{-3}$
$K_{ALKNOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{PNOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m <sup>-3</sup> $Hydrolysis of particulate substrate: X_5$ $K_6$ $1^{-1}$ $K_h$ Hydrolysis rate constant3 $d^{-1}$ $\eta_{NOKS}$ Anoxic hydrolysis reduction factor0.6 $ \eta_{fe}$ Anaerobic hydrolysis reduction factor0.4 $ K_{O2S}$ Saturation/inhibition coefficient for oxygen0.2g O <sub>2</sub> m <sup>-3</sup> $K_{NOxS}$ Saturation coefficient for particulate COD0.1g X <sub>S</sub> g <sup>-1</sup> X <sub>H</sub> Phosphorus-accumulating organism: $X_{PAO}$ $  q_{PAA}$ Rate constant for storage of $X_{PPA}$ (base $X_{PP}$ )3.3g X <sub>PHA</sub> g <sup>-1</sup> X <sub>PAO</sub> d <sup>-1</sup> $q_{PAO}$ Maximum growth rate of PAO1.2d <sup>-1</sup> $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8 $ b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2d <sup>-1</sup> $b_{PAO}$ Saturation coefficient for oxygen0.2g O <sub>2</sub> m <sup>-3</sup> $K_{O2PAO}$ Saturation coefficient for oxygen0.2d <sup>-1</sup> $b_{PAO}$ Saturation factor for anoxic activity0.8- $b_{PAO}$ Saturation coefficient for oxygen0.2d <sup>-1</sup> $k_{O2PAO}$ Saturation coeffic	K <sub>NO2NOB</sub>	Saturation coefficient for ammonium (nutrient)	0.5	$g N m^{-3}$
$K_{\rm PNOB}$ Saturation coefficient for phosphorus (nutrient)0.01g P m^{-3}Hydrolysis of particulate substrate: $X_S$ $X_S$ $A$ $A$ $N_{\rm NOX}$ Anoxic hydrolysis reduction factor $0.6$ $ \eta_{\rm fe}$ Anaerobic hydrolysis reduction factor $0.4$ $ K_{\rm O2S}$ Saturation/inhibition coefficient for oxygen $0.2$ $g O_2 m^{-3}$ $K_{\rm NOX}$ Saturation coefficient for particulate COD $0.1$ $g X_S g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $0.1$ $g X_S g^{-1} X_H$ $Phasphorus-accumulating organisms: X_{PAO}3.3g X_{\rm PHA} g^{-1} X_{PAO} d^{-1}q_{\rm PA}Rate constant for storage of X_{\rm PHA} (base X_{\rm PP})3.3g X_{\rm PHA} g^{-1} X_{PAO} d^{-1}q_{\rm PAO}Maximum growth rate of PAO1.2d^{-1}\eta_{\rm NOXPAO}Reduction factor for anoxic activity0.8 b_{\rm PAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}b_{\rm PAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}b_{\rm PAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}b_{\rm PAO}Saturation coefficient for oxygen0.2d^{-1}b_{\rm PAO}Saturation coefficient for oxygen0.2d^{-1}b_{\rm PAO}Rate for lysis of X_{\rm PAO}0.2d^{-1}b_{\rm PAO}Saturation coefficient for oxygen0.2d^{-1}b_{\rm PAO}Saturation coefficient for oxygen0.2g O_2 m^{-3}<$	K <sub>ALKNOB</sub>	Saturation coefficient for alkalinity (HCO <sup>-3</sup> )	0.5	mole HCO <sup>-3</sup> m <sup>-3</sup>
Hydrolysis of particulate substrate: $X_s$ $K_h$ Hydrolysis rate constant3 $d^{-1}$ $\eta_{NOxS}$ Anoxic hydrolysis reduction factor0.6- $\eta_{fe}$ Anaerobic hydrolysis reduction factor0.4- $K_{O2S}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOxS}$ Saturation/inhibition coefficient for particulate COD0.1 $g X_s g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ 0.1 $g X_s g^{-1} X_{PAO} d^{-1}$ $q_{PHA}$ Rate constant for storage of $X_{PPA}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $\eta_{PP}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $\eta_{NOXPAO}$ Rete for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $\psi_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $\psi_{PAO}$ Saturation coefficient for oxygen0.2 $d^{-1}$ $\psi_{PAO}$ Saturation coefficient for oxygen0.5 $g N m^{-3}$ $K_{NOXPAO}$ <td>K<sub>PNOB</sub></td> <td>Saturation coefficient for phosphorus (nutrient)</td> <td>0.01</td> <td>g P m<sup>-3</sup></td>	K <sub>PNOB</sub>	Saturation coefficient for phosphorus (nutrient)	0.01	g P m <sup>-3</sup>
$K_h$ Hydrolysis rate constant3 $d^{-1}$ $\eta_{NOXS}$ Anoxic hydrolysis reduction factor0.6- $\eta_{fe}$ Anaerobic hydrolysis reduction factor0.4- $K_{O2S}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOXS}$ Saturation /inhibition coefficient for nitrite and nitrate0.5 $g N m^{-3}$ $K_{XS}$ Saturation coefficient for particulate COD0.1 $g X_5 g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )3.3 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Saturation /inhibition coefficient for oxygen0.2 $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PPAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PPAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Saturation /inhibition coefficient for oxygen0.2 $d^{-1}$ $k_{O2PAO}$ Saturation coefficient for intrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{NMAPAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{NHAPAO}$ Saturation coefficient for amonium (nutrient)0.05 $g P m^{-3}$ $K_{NM4PAO}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$	Hydrolysis of partici	ılate substrate: X <sub>S</sub>		0
$\eta_{\text{NOXS}}$ Anoxic hydrolysis reduction factor0.6- $\eta_{\text{fe}}$ Anaerobic hydrolysis reduction factor0.4- $K_{\text{O2S}}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{\text{NOXS}}$ Saturation/inhibition coefficient for nitrite and nitrate0.5 $g N m^{-3}$ $K_{\text{XS}}$ Saturation coefficient for particulate COD0.1 $g X_{\text{S}} g^{-1} X_{\text{H}}$ Phosphorus-accumulating organisms: $X_{PAO}$ - $q_{\text{PHA}}$ Rate constant for storage of $X_{\text{PHA}}$ (base $X_{\text{PP}}$ )3.3 $g X_{\text{PHA}} g^{-1} X_{\text{PAO}} d^{-1}$ $q_{\text{PAO}}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{\text{NOXPAO}}$ Reduction factor for anoxic activity0.8- $b_{\text{PAO}}$ Rate for lysis of $X_{\text{PAO}}$ 0.2 $d^{-1}$ $h_{\text{NOXPAO}}$ Rate for lysis of $X_{\text{PAO}}$ 0.2 $d^{-1}$ $b_{\text{PAO}}$ Rate for lysis of $X_{\text{PAO}}$ 0.2 $d^{-1}$ $k_{\text{O2PAO}}$ Saturation/inhibition coefficient for oxygen0.2 $d^{-1}$ $h_{\text{NOXPAO}}$ Rate for lysis of $X_{\text{PP}}$ 0.2 $d^{-1}$ $b_{\text{PAO}}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $k_{\text{O2PAO}}$ Saturation coefficient for nitrate, $S_{\text{NO3}}$ 0.5 $g N m^{-3}$ $k_{\text{PAO}}$ Saturation coefficient for acetate $S_A$ 4 $g \text{COD } m^{-3}$ $k_{\text{NAA}}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $k_{\text{PAO}}$ Saturation coefficient for	K <sub>h</sub>	Hydrolysis rate constant	3	$d^{-1}$
$\eta_{fe}$ Anaerobic hydrolysis reduction factor0.4- $K_{O2S}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NXS}$ Saturation/inhibition coefficient for nitrite and nitrate0.5 $g N m^{-3}$ $K_{XS}$ Saturation coefficient for particulate COD0.1 $g X_S g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )3.3 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Saturation /inhibition coefficient for oxygen0.2 $d^{-1}$ $k_{OXPAO}$ Saturation factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $k_{OXPAO}$ Saturation /inhibition coefficient for oxygen0.2 $d^{-1}$ $k_{NOXPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{NAPAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.01 $g P m^{-3}$ $K_{PNS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$	$\eta_{\rm NOxS}$	Anoxic hydrolysis reduction factor	0.6	-
$K_{O2S}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOXS}$ Saturation/inhibition coefficient for nitrite and nitrate0.5 $g N m^{-3}$ $K_{XS}$ Saturation coefficient for particulate COD0.1 $g X_S g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $u_{PAO}$ $a Xe constant for storage of X_{PHA} (base X_{PP})3.3g X_{PHA} g^{-1} X_{PAO} d^{-1}q_{PP}Rate constant for storage of X_{PP}1.5g X_{PHA} g^{-1} X_{PAO} d^{-1}\mu_{PAO}Maximum growth rate of PAO1.2d^{-1}\eta_{NOXPAO}Reduction factor for anoxic activity0.8 b_{PAO}Rate for lysis of X_{PP}0.2d^{-1}b_{PAO}Rate for lysis of X_{PP}0.2d^{-1}b_{PAO}Saturation/inhibition coefficient for oxygen0.2d^{-1}b_{PAO}Saturation factor for anoxic activity0.8 b_{PAO}Rate for lysis of X_{PP}0.2d^{-1}b_{PAO}Saturation factor for nitrate, S_{NO3}0.2d^{-1}b_{PAO}Saturation coefficient for oxygen0.2g O_2 m^{-3}K_{NOXPAO}Saturation coefficient for acetate S_A4g COD m^{-3}K_{NAPAO}Saturation coefficient for acetate S_A4g COD m^{-3}K_{NAPAO}Saturation coefficient for amonium (nutrient)0.05g N m^{-3}K_{PS}Saturation coefficient for phosphorus in storage of PP0.2g P m^$	$\eta_{\rm fe}$	Anaerobic hydrolysis reduction factor	0.4	-
$K_{NOXS}$ Saturation/inhibition coefficient for nitrite and nitrate0.5 $g N m^{-3}$ $K_{XS}$ Saturation coefficient for particulate COD0.1 $g X_S g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ 0.1 $g X_S g^{-1} X_H$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )3.3 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen0.2 $d^{-1}$ $k_{O2PAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{NOAPAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$	K <sub>O2S</sub>	Saturation/inhibition coefficient for oxygen	0.2	$g O_2 m^{-3}$
$K_{\rm XS}$ Saturation coefficient for particulate COD0.1 $g X_{\rm S} g^{-1} X_{\rm H}$ Phosphorus-accumulating organisms: $X_{PAO}$ $q_{\rm PHA}$ Rate constant for storage of $X_{\rm PHA}$ (base $X_{\rm PP}$ )3.3 $g X_{\rm PHA} g^{-1} X_{\rm PAO} d^{-1}$ $q_{\rm PP}$ Rate constant for storage of $X_{\rm PP}$ 1.5 $g X_{\rm PHA} g^{-1} X_{\rm PAO} d^{-1}$ $\mu_{\rm PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{\rm NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{\rm PAO}$ Rate for lysis of $X_{\rm PAO}$ 0.2 $d^{-1}$ $b_{\rm PAO}$ Rate for lysis of $X_{\rm PAO}$ 0.2 $d^{-1}$ $b_{\rm PAO}$ Rate for lysis of $X_{\rm PP}$ 0.2 $d^{-1}$ $b_{\rm PAO}$ Saturation coefficient for oxygen0.2 $d^{-1}$ $K_{O2PAO}$ Saturation coefficient for nitrate, $S_{\rm NO3}$ 0.5 $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{\rm NH4PAO}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$ $K_{\rm PP}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$	K <sub>NOxS</sub>	Saturation/inhibition coefficient for nitrite and nitrate	0.5	$g N m^{-3}$
Phosphorus-accumulating organisms: $X_{PAO}$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )3.3 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8 $ b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen0.2 $d^{-1}$ $K_{O2PAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{APAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$	K <sub>XS</sub>	Saturation coefficient for particulate COD	0.1	$g X_S g^{-1} X_H$
$q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )3.3 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{O2PAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{APAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$	Phosphorus-accumul	ating organisms: X <sub>PAO</sub>		
$q_{PP}$ Rate constant for storage of $X_{PP}$ 1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ 0.2 $d^{-1}$ $k_{O2PAO}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOXPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$ $K_{PY}$ Saturation coefficient for phosphorus in storage of PP0.01 $g P m^{-3}$	$q_{\rm PHA}$	Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )	3.3	$g X_{PHA} g^{-1} X_{PAO} d^{-1}$
$\mu_{PAO}$ Maximum growth rate of PAO1.2 $d^{-1}$ $\eta_{NOXPAO}$ Reduction factor for anoxic activity0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ 0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ 0.2 $d^{-1}$ $K_{O2PAO}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOXPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$ $K_{reve}$ Saturation coefficient for phosphorus in storage of PP0.01 $g P m^{-3}$	9 <sub>PP</sub>	Rate constant for storage of $X_{PP}$	1.5	$g X_{PHA} g^{-1} X_{PAO} d^{-1}$
$\eta_{NOXPAO}$ Reduction factor for anoxic activity $0.8$ $ b_{PAO}$ Rate for lysis of $X_{PAO}$ $0.2$ $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PP}$ $0.2$ $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ $0.2$ $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ $0.2$ $d^{-1}$ $K_{O2PAO}$ Saturation/inhibition coefficient for oxygen $0.2$ $g O_2 m^{-3}$ $K_{NOXPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ $0.5$ $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for phosphorus in storage of PP $0.2$ $g P m^{-3}$ $K_{PS}$ Saturation coefficient for phosphote (nutrient) $0.01$ $g R m^{-3}$	$\mu_{\mathrm{PAO}}$	Maximum growth rate of PAO	1.2	$d^{-1}$
$b_{PAO}$ Rate for lysis of $X_{PAO}$ 0.2 $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ 0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ 0.2 $d^{-1}$ $K_{O2PAO}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOxPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for accetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$ $K_{rnvic}$ Saturation coefficient for phosphorus (nutrient)0.01 $g R m^{-3}$	$\eta_{\rm NOxPAO}$	Reduction factor for anoxic activity	0.8	-
$b_{PP}$ Rate for lysis of $X_{PP}$ 0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ 0.2 $d^{-1}$ $K_{O2PAO}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOxPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for accetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$ $K_{revice}$ Saturation coefficient for phosphorus (nutrient)0.01 $g P m^{-3}$	$b_{\rm PAO}$	Rate for lysis of $X_{PAO}$	0.2	$d^{-1}$
$b_{\text{PHA}}$ Rate for lysis of $X_{\text{PHA}}$ 0.2 $d^{-1}$ $K_{02PAO}$ Saturation/inhibition coefficient for oxygen0.2 $g O_2 m^{-3}$ $K_{NOxPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5 $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g P m^{-3}$ $K_{revice}$ Saturation coefficient for phosphorus (nutrient)0.01 $g P m^{-3}$	$b_{\rm PP}$	Rate for lysis of $X_{\rm PP}$	0.2	$d^{-1}$
$K_{O2PAO}$ Saturation/inhibition coefficient for oxygen0.2g $O_2 m^{-3}$ $K_{NOxPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5g N m^{-3} $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4g COD m^{-3} $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05g N m^{-3} $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2g P m^{-3} $K_{revice}$ Saturation coefficient for phosphorus (nutrient)0.01g R m^{-3}	$b_{\mathrm{PHA}}$	Rate for lysis of $X_{\text{PHA}}$	0.2	$d^{-1}$
$K_{NOXPAO}$ Saturation coefficient for nitrate, $S_{NO3}$ 0.5g N m^{-3} $K_{APAO}$ Saturation coefficient for acetate $S_A$ 4g COD m^{-3} $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05g N m^{-3} $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2g P m^{-3} $K_{runco}$ Saturation coefficient for phosphate (nutrient)0.01g P m^{-3}	K <sub>O2PAO</sub>	Saturation/inhibition coefficient for oxygen	0.2	$g O_2 m^{-3}$
$K_{APAO}$ Saturation coefficient for acetate $S_A$ 4 $g \text{ COD m}^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g \text{ N m}^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g \text{ P m}^{-3}$ $K_{rrule}$ Saturation coefficient for phosphate (nutrient)0.01 $g \text{ P m}^{-3}$	K <sub>NOxPAO</sub>	Saturation coefficient for nitrate, S <sub>NO3</sub>	0.5	$g N m^{-3}$
$K_{\rm NH4PAO}$ Saturation coefficient for ammonium (nutrient)0.05 $g~N~m^{-3}$ $K_{\rm PS}$ Saturation coefficient for phosphorus in storage of PP0.2 $g~P~m^{-3}$ $K_{\rm PN}$ Saturation coefficient for phosphate (nutrient)0.01 $g~P~m^{-3}$	K <sub>APAO</sub>	Saturation coefficient for acetate $S_A$	4	g COD m <sup>-3</sup>
$K_{PS}$ Saturation coefficient for phosphorus in storage of PP0.2g P m^{-3} $K_{PS}$ Saturation coefficient for phosphate (nutrient)0.01g P m^{-3}	K <sub>NH4PAO</sub>	Saturation coefficient for ammonium (nutrient)	0.05	$g N m^{-3}$
$K_{\rm resc}$ Saturation coefficient for phosphate (nutrient) 0.01 g P m <sup>-3</sup>	K <sub>PS</sub>	Saturation coefficient for phosphorus in storage of PP	0.2	$g P m^{-3}$
Appao Saturation coefficient for phosphate (nument) 0.01 g r m	$K_{\rm PPAO}$	Saturation coefficient for phosphate (nutrient)	0.01	$g P m^{-3}$

(Continued)

Item	Description	20°C	Units
K <sub>ALKPAO</sub> K <sub>pp</sub>	Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) Saturation coefficient for poly-phosphate	0.1 0.01	mole HCO <sup>-3</sup> m <sup>-3</sup> g $\chi_{\rm PP}$ g <sup>-1</sup> $\chi_{\rm PAO}$
K <sub>MAX</sub>	Maximum ratio of $X_{PP}/X_{PAO}$	0.34	$g X_{PP} g^{-1} X_{PAO}$
K <sub>IPP</sub> K <sub>PHA</sub>	Saturation coefficient for PHA	0.02	$g \chi_{PP} g^{-1} \chi_{PAO}$ $g \chi_{PHA} g^{-1} \chi_{PAO}$

Table 3 (Continued)



Fig. 6. Experimental data (points) and model simulation (lines) of  $NH_4$ -N, nitrate–N, and  $PO_4^-$ –P in tank one (a) run 1 (b) run 2 (c) run 3, and (d) run 4.

because  $NH_4^+$ –N concentration is decreased tendency with the increasing of C/N ratio (C/N is 9.1 in run 4).  $NO_3^-$ –N was decreased approximately to 3.1 mg/L in all runs of C/N ratio larger than five while it was decreased in run 3 due to an inadequate carbon source which led to insufficient denitrification process.

Under anaerobic condition during phase II,  $NH_4^+$ -N was increased to 17.4 mg/L in run 3, while it was increased to 9.8 mg/L in run 4 due to the increasing of C/N ratio.

Under aerobic condition during phase III,  $NH_4^+$ –N concentration was decreased below 4 mg/L during runs 1, 2, and 4 while it was decreased to 6 mg/L in run 4 due to low organic matter (C/N < 3.5) which required a long time for completion the nitrification process.

It can be seen clearly from Fig. 6,  $NO_3^-$ –N concentration was significantly increased and its increase rate gradually decreases with the increasing of *C/N* ratio. In the end of the aeration, NO<sub>3</sub>–N concentration was 7.9 mg/L at low *C/N* ratio (run 3), while it was

decreased to 5.6 mg/L at C/N ratio of 5.4, 6.7, and 9.1 in runs 1, 2, and 3, respectively. As can be seen from Fig. 6, PO<sub>4</sub><sup>-</sup>–P concentration was released greatly to be 14.29 mg/L under anaerobic condition in run 1 and its releasing was decreased to be 7.99 mg/L in run 3. The proposed explanation for this observation is due to high VFA ( $S_A = 91$ ) in run 1 and low VFA ( $S_A = 59$ ) in run 4 which that effected significantly on phosphorus release. Under aerobic condition, phosphorus uptake in runs 1, 2, and 3 were better than run 4 owing to low C/P ratio in run 3 (C/P ratio was 27.6).

4.3.1.2. Model validation of tank two. Fig. 7 depicts the tested and predicated data of ammonia–N, nitrate–N, nitrite–N and  $PO_4^-$ –P concentrations of tank two under four investigated runs, This figure is shown a good consistency between the simulation values and test values, whereas the sum of squares of the deviations ( $R^2$ ) of NH<sub>4</sub><sup>+</sup>–N, PO<sub>4</sub><sup>-</sup>–P, NO<sub>2</sub><sup>-</sup>–N and NO<sub>2</sub><sup>-</sup>–N were 0.99, 0.98,0.94, and 0.95, respectively, of at run 1, 0.99, 0.99, 0.98, and 0.99,

Table 4

Short definition	of model com	ponent and t	ypical raw	wastewater	characteristics
			./ .		

Symbol	Item	Unit	Run no			
oymbol	nem	Ont	1	2	3	4
Dissolved compo	onent					
So	Oxygen	$g O2 m^{-3}$	0	0	0	0
Ss	Readily biodegradable substrate	g COD m <sup>-3</sup>	209	172	89	106
$S_{\rm A}$	Volatile fatty acids	g COD m <sup>-3</sup>	91	79	59	66
$S_{\mathrm{I}}$	Inert soluble organic material	g COD m <sup>-3</sup>	7.2	5.3	3.88	4.3
$S_{\rm NH4}$	Ammonia nitrogen	g N m <sup>-3</sup>	45.2	26.5	33	17.78
$S_{\rm NO2}$	Nitrite nitrogen	g N m <sup>-3</sup>	0.26	0.11	0.06	0.02
$S_{\rm NO3}$	Nitrate nitrogen	g N m <sup>-3</sup>	3.11	1.98	1.27	0.23
$S_{\rm ALK}$	Alkalinity	mol $HCO_3^- m^{-3}$	4.83	5.23	4.93	5.11
$S_{\rm PO4}$	Soluble orthophosphate	$g P m^{-3}$	5.83	1.49	4.26	3.55
Particulate comp	ponent		1	2	3	4
XI	Particulate inert organic material	g COD $m^{-3}$	61	59	53	57
Xs	Slowly biodegradable substrate	g COD m <sup>-3</sup>	337	260	197	209
$X_{\rm H}$	Active heterotrophic biomass	g COD m <sup>-3</sup>	6	3	5	1
X <sub>AOB</sub>	Ammonia oxidizing bacteria	g COD m <sup>-3</sup>	0.5	0.1	0.3	0.01
X <sub>NOB</sub>	Nitrite oxidizing bacteria	$\tilde{g}$ COD.m <sup>-3</sup>	0.08	0.01	0	0
MLSS ( $x_{TSS}$ )	Mixed liquor suspended solid	g TSS m <sup>-3</sup>	89	76	65	71



Fig. 7. Experimental data (points) and model simulation (lines) of different soluble components in tank two (a) run 1 (b) run 2 (c) run 3 and (d) run 4.

respectively, at run 2, 0.98, 0.98, 0.97, and 0.89, respectively, at run 3 and 0.98, 0.98, 9.99, and 0.92, respectively, at run 4. The analysis of biological reaction (denitrification and phosphorus release during phase I, nitrification and SND process during phase II and denitrification during phase III) were discussed previously. The main difference between the simulation result of the fourth runs were similar to the analysis to tank one, whereas  $NH_4^+$ -N was increased to 15.8 mg/L in run 3, while it was

increased to 7.08 mg/L in run 4 due to insufficient organic matter in run 3. Under aerobic condition, it was concluded that all runs of C/N > 4 are more appropriateness that can met Chinese national class I (Grade A) sewage discharge standard. In PITSF process, SND process was clearly observed in tank two, whereas it was operated under a companied effect of nitrification and denitrification. The extension model was able successfully to simulate NO<sub>3</sub>–N variation in tank two where the sum of squares of the deviations

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 $(R^2)$  of NO<sub>3</sub>–N was above 0.95 in all investigated runs.

It was notably from Fig. 7 that the indication of  $PO_4$ –P release and its uptake was similar to tank one. It was externally affected by VFA (Sa) variation in different runs. The simulation result showed that an extension model is a good development model to predicted NO<sub>2</sub>–N pathway, whereas the sum of squares of the deviations  $R^2$  of NO<sub>2</sub>–N was (0.97) between the observed and predicted values.

4.3.1.3. Model validation of tank three. Fig. 8 shows the tested and predicated data of ammonia-N, nitrate-N, nitrite-N, and PO<sub>4</sub>-P concentrations of tank three for four investigated runs. It showed a good reliability between the observed and predicated data, whereas the sum of squares of the deviations  $R^2$  of ammonia–N,  $PO_4^-$ –P nitrate-N, and nitrite–N concentrations were 0.99, 0.98, 0.96, and 0.88, respectively, at run 1, 0.99, 0.97, 0.95, and 0.87, respectively, at run 2, 0.96, 0.99, 0.99, and 0.87, respectively, at run 3, and 0.99, 0.99, 0.95, and 0.84, respectively, at run 4. The aerobic denitrification phenomena (SND) were observed clearly during phase I. Thus, both anoxic and aerobic biological reaction is considered for each simulated compound. This model showed a good agreement to simulate the variation of NO2-N and NO<sub>3</sub>-N where NO<sub>3</sub>-N concentration was decreased below 3 mg/L in run 4 (C/N > 7), while it was decreased slowly in run 3 due to low organic carbon which effected significantly on SND rate as shown previously [1].

4.3.1.4. Model validation of tank four. Fig. 9 depicts the observed and predicated data of ammonia-N, PO<sub>4</sub><sup>-</sup>-P, and nitrite-N concentrations of tank four under four runs. It showed a good fitness between simulation and experimental data, whereas the sum of squares of the deviations ( $R^2$ ) of NH<sub>4</sub><sup>+</sup>-N, PO<sub>4</sub><sup>-</sup>-P, and nitrite-N were 0.99, 0.94, and 0.97, respectively, at run 1, 0.98, 0.99, and 0.97, respectively, at run 2, 0.99, 0.99, and 0.98, respectively, at run 3, and 0.99, 0.98, and 0.98, respectively, at run 4. It was found from Fig. 9 that PO<sub>4</sub>-P was decreased below 0.3 mg/L in runs 1, 2, 4, but it was decreased to 3.4 mg/L in run 3 due to low C/P ratio in this run. In spite of PO<sub>4</sub>-P was consumed by X<sub>PAO</sub> organism which utilized both S<sub>NO2</sub> and S<sub>NO3</sub> concentrations as a donor electron accepter, extension model is succeeded to model the variation of PO4-P in phase I.

4.3.1.5. Model validation of tank five. Fig. 10 depicts the tested and predicated data of  $NH_4^+$ –N,  $PO_4$ –N, nitrate–N, and nitrite–N concentration of tank five under four investigated runs. This figure shows a good consistency between the observed and predicated data, whereas the sum of squares of the deviations ( $R^2$ )  $NH_4^+$ –N,  $PO_4$ –P, nitrate–N, and nitrite–N concentration of tank five were 0.91, 0.77, 0.99, and 0.77, respectively, at run 1, 0.92, 0.90, 0.99, and 0.71, respectively, at run 2, 0.99, 0.95, 0.77, and 0.68, respectively, at run 3, and 0.95, 0.73, 0.99, and 0.76, respectively, at run 4.



Fig. 8. Experimental data (points) and model simulation (lines) of different soluble components in tank three (a) run 1 (b) run 2 (c) run 3, and (d) run 4.



Fig. 9. Experimental data (points) and model simulation (lines) of different soluble components in tank four (a) run 1 (b) run 2 (c) run 3, and (d) run 4.



Fig. 10. Experimental data (points) and model simulation (lines) of different soluble components in tank five (a) run 1 (b) run 2 (c) run 3, and (d) run 4.

It can be seen readily from Fig. 10 that  $NH_4^+-N$  was approximately stabilized at 2.44, 1.2, 3.5, and 1.44 mg/L in runs 1, 2, 3, and 4, respectively. PO<sub>4</sub>-P concentration was below 0.07 mg/L in runs 1, 2, and 4 while it was 0.2 mg/L in run 3 due to low *C/P* ratio in this run. However, the simulation result showed a geed convergence with the observed result where it can be meet Chinese national class I (Grade A) sewage discharge standard.

## 4.4.2. Simulation of particulate components

In this study, the variations of micro-organisms were evaluated by extension model in each tank during the first half-cycle. Fig. 11a–e showed the simulation values of particulate component concentrations during the first half-cycle under different runs. It was depicted that, the  $X_{H}$ ,  $X_{PAO}$ ,  $X_{PP}$ ,  $X_{AOB}$ , and  $X_{NOB}$  concentrations were 687–2,108, 130–257, 158–227,



Fig. 11a. The biomass variations in tank one under different runs.



Fig. 11b. The biomass variations in tank one under different runs.

29–65, and 15–48 mg/L in PITSF-SEU process. According to Fig. 11a–e,  $X_{\rm H}$ ,  $X_{\rm PAO}$ ,  $X_{\rm AOB}$ , and  $X_{\rm NOB}$  were increased slowly with time in the anoxic tank, and then, it was decreased in the anaerobic tanks because of the lysis reaction.  $X_{\rm PHA}$  were increased with time under anaerobic state condition tank due to phosphorus released, and then, it was decreased in the aerobic tanks due to phosphors uptake. The

simulation result concluded that both  $X_{AOB}$  and  $X_{NOB}$  are utilized as an aerobic species that utilize free molecular oxygen as final electron accepter. Quantitatively, the particulate component of  $X_{AOB}$  was increased obviously to 66 mg/L in tank 1 under aerobic condition and  $X_{NOB}$  increased also to 36 mg/L in this tank due to aerobic growth. Although the particulate components of  $X_{AOB}$  and  $X_{NOB}$  varied in each



Fig. 11c. The biomass variations in tank three under different runs.



Fig. 11d. The biomass variations in tank four under different runs.

tank, the ratio of total nitrifying species to total active biomass was about 2–2.68% in each tank. Both  $X_{\rm H}$  and  $X_{\rm PAO}$  are facultative species that utilize free molecular oxygen or combined oxygen as final electron accepter for aerobic or anoxic growth. Quantitatively, the biomass of  $X_{\rm H}$  was decreased to 1,393 mg/L in tank 1 (anoxic tank) in which the step feeding influent flowed during phase I, and then, it was decreased to 501 mg/L in phase II where tank 1 operated under anaerobic condition. It was increased obviously in phase III to be 942 mg/L. The particulate components of  $X_{\rm H}$ ,  $X_{\rm PAO}$ ,  $X_{\rm PP}$ ,  $X_{\rm AOB}$ , and  $X_{\rm NOB}$  increased in quantities by about 49, 27, 151, 88, and 98% in tank two due to change the environmental state condition



Fig. 11e. The biomass variations in tank five under different runs.

from anaerobic to aerobic during phase II and decreased in quantities by about 55, 67, 45, 0.11, and 0.4% in phase III due to change the environmental state condition from aerobic to anoxic in which the step feed influent pumped from tank 2 during this phase. The particulate components of  $X_{H}$ ,  $X_{PAO}$ ,  $X_{PP}$ ,  $X_{AOB}$ , and  $X_{NOB}$  increased slowly in quantities by about 41, 38, 37, 70.3, and 81% in whole phases of tank five because of the aerobic reaction as shown in Fig. 11a–e, while X<sub>PHA</sub> was decreased in quantities by about 41%. In this study, the disadvantages of the developed biological nutrient removal processes were enhanced by reconfiguring the process without internal mixed liquor recirculation. This was done by configuring the process into five tanks with changeable environmental state condition into anaerobic/anoxic, aerobic zones in each tank to achieve optimum nutrient removal. In PITSF-SEU process, a step feed influent was also used to direct the influent into the anoxic tank as an external organic source for denitrification. Thus, the particulate components of  $X_{H_{\ell}}$   $X_{PAO_{\ell}}$  and X<sub>PP</sub> decreased in this tank due to the dilution effect of the second flow. The particulate components of  $X_{AOB}$ and  $X_{\text{NOB}}$  were also decreased due to the negative growth rate resulted from lysis reaction in the anoxic tank. In full-scale wastewater treatment plant, the transient system behavior is of high practical importance since variations of composition, influent flowrate as well as changes of operation prevents each realworld wastewater treatment plant from reaching the steady-state condition. Although the application of extension model under steady state was validated in this study, the application in transient state can be implemented in the future study. In addition, the practical applications of the extension model including plant controller layout, optimization, mathematical verification of the purification performance, and model-based state and parameter estimation should be taken into account in the future study.

## 5. Conclusions

The variation of soluble components of  $S_{\text{NO2}}$ ,  $S_{\text{NO3}}$ ,  $S_{\text{NH4}}$ , and  $S_{\text{PO4}}$  in PITSF-SEU process could be modeled successfully using an extension model. The results obtained in this work can be summarized as follows:

- The effective removal efficiency of ammonia–N, TN, and TP at 94%, 89.2%, 90.6%, respectively, were achieved effectively in PITSF-SEU process.
- (2) In this study,  $\mu_{AOB}$  and  $\mu_{NOB}$  were 0.8 and 0.4 day<sup>-1</sup>, respectively.  $Y_{AOB}$  was 0.18 and  $Y_{NOB}$  was 0.06. The values of ( $\eta_{NO2H}$ ) and ( $\eta_{NO3H}$ ) were chosen as 1.0 and 0.8, respectively.
- (3) The simulation result showed a good agreement between the observed and predicated data, whereas the sum of squares deviations ( $R_2$ ) of soluble components  $S_{NH4}$ ,  $S_{PO4}$ ,  $S_{NO3}$  and  $S_{NO2}$ were more than 0.95 in all investigated runs. High NH<sub>4</sub><sup>+</sup>-N and PO<sub>4</sub>–P removal rate were achieved successfully in runs 1, 2, 4 of *C*/*N*

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ratio > 5 and C/P ratio > 40.

- (4) In this work, SND process was modified successfully in the first aerobic tanks during a main phase where both anoxic and aerobic biological reaction was considered for each compound.
- (5)According to model simulation,  $X_{H}$ ,  $X_{PAO}$ ,  $X_{PP}$ ,  $X_{AOB}$ , and  $X_{NOB}$  concentrations were 898–2,308, 104-244, 158-227, 22-69, and 13-48 in four test runs, respectively. The results concluded that the particulate components of  $X_{H}$ ;  $X_{PAO}$ ,  $X_{PP}$ ,  $X_{AOB}$ , and  $X_{NOB}$  decreased in the anaerobic tanks because of the lysis reaction. Then,  $X_{\rm H}$ ;  $X_{PAO}$ ,  $X_{PP}$ ,  $X_{AOB}$ , and  $X_{NOB}$  increased in the aerobic tanks due to aerobic growth. They were increased in quantities by about 49, 27, 151, 88, and 98% in tank two due to change the environmental state condition from anaerobic to aerobic during phase II and decreased in quantities by about 55, 67, 45, 0.11, and 0.4% in phase III due to change the environmental state condition from aerobic to anoxic in which the step feed influent pumped from tank 2 during this phase.

# Abbreviations

PITSF-SEU	<ul> <li>phased isolation tank step</li> </ul>	
	feed-southeast university	
A2/O	— anaerobic–anoxic/oxic	
SBR	<ul> <li>sequence batch reactor</li> </ul>	
SND	<ul> <li>— simultaneous nitrification and</li> </ul>	
	denitrification	
X <sub>AOB</sub>	<ul> <li>ammonia-oxidizing bacteria</li> </ul>	
X <sub>NOB</sub>	<ul> <li>nitrite oxidize bacteria</li> </ul>	
X <sub>PAOS</sub>	<ul> <li>phosphate-accumulating organisms</li> </ul>	
$X_{\rm H}, X_{\rm PP}$	<ul> <li>poly phosphate organism heterotroph</li> </ul>	ιic
	organisms	
PLC	— programmable logic control	
$X_{\rm PHA}$	<ul> <li>poly-hydroxylalkonates</li> </ul>	
OUR	<ul> <li>oxygen uptake rate</li> </ul>	

#### References

- N. Rusul, A. Saad, X.W. Lu, Biological nutrient removal with limited organic matter using a novel anaerobic–anoxic/oxic multi-phased activated sludge process, Saudi J. Biol. Sci. 20(1) (2013) 1–21.
- [2] M. Henze, W. Gujer, T. Mino, M.C.M. van Loosdrecht, Activated Sludge Models: ASM1, ASM2, ASM2d and ASM3, International Water Association, London, 2000.

- [3] WEF, Biological and Chemical Systems for Nutrient Removal, Water Environment Federation, Alexandria, VA, 1999.
- [4] J. Oles, P.A. Wilderer, Computer aided design of sequencing batch reactor based on IAWPRC activated sludge model, Water Sci. Technol. 23(6) (1999) 1087–1095.
- [5] M. Henze, W. Gujer, Activated Sludge Model No. 2 IAWQ, Scientific and Technical Report No. 3 IAWQ, 1995, London, ISBN 9022200.
- [6] M. Henze, W. Gujer, Activated Sludge Model No. 1 IAWPRC, Scientific and Technical Report No. 1 IAWQ, 1987, London, ISBN 1010-707X.
- [7] M. Henze, W. Gujer, T. Mino, T. Matsuo, M.T. Wentzel, G.V.R. Marais, Activated Sludge Model No. 2 IAWQ, Scientific and Technical Report No. 3, IAWQ, 1995.
- [8] M. Henze, W. Gujer, T. Mino, T. Matsuo, M.C. Wentzel, G.V.R. Marais, M.C. van Loosdrecht, Outline activated sludge model No. 2d, Water Sci. Technol. 39(1) (1999) 165–182.
- [9] W. Gujer, M. Henze, T. Mino, M.C.M. van Loosdrecht, Activated sludge model no. 3, Water Sci. Technol. 39 (1) (1999) 183–193.
- [10] G. Didem, K. Ozlem, B. Hanife, S. Seval, Storage phenomena in relation to carbon sources for denitrification, J. Desalin. Water Treat. 8(3) (2009) 171–176.
- [11] J. Kappeler, R. Brodmann, Low F/M bulking and scumming: Towards a better understanding by modeling, Water Sci. Technol. 31(2) (1995) 225–339.
- [12] S. Marsili-Libelli, F. Tabani, Accuracy analysis of a respirometer for activated sludge dynamic 351 modeling, Water Res. 36(11) (2002) 81–92.
- [13] S.E.P.A. Chinese, Water and Wastewater Monitoring Methods, 4th ed., Chinese Environmental Science, Beijing, 2000.
- [14] D. Mamais, D. Jenkins, P. Pitt, A rapid physico-chemical method for the determination of readily biodegradable soluble COD in municipal wastewater, Water Res. 27(1) (1993) 195–197.
- [15] G. Philippe, A. Jean-Mark, U. Vincent, B. Jean-Claude, Estimation of nitrifying bacterial activities by measuring oxygen uptake in the presence of the metabolic inhibitors allylthiourea and azide, Appl. Environ. Microbiol. 64(3) (1998) 2266–2268.
- [16] T. Mino, Activated Sludge Model: Microbiological Basis, in: G. Bitton (Ed.), Encyclopedia of Environmental Microbiology, 323(1), New York, NY, Wiley, 2002, pp. 14–26.
- [17] D. Wild, R. Von Schulthess, W. Gujer, Structure modeling of denitrification intermediates, Water Sci. Technol. 31(2) (1995) 69–76.
- [18] T.Y. Pai, S.H. Chuang, Y.P. Tsai, C.F. Ouyang, Modeling a combined A2O and RBC process under DO variation by using an activated sludge bio-film hybrid model, Environ. Eng. 130(12) (2004) 1433–1441.