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# Modeling and particular application of ASM2d model for describing organic matter and nutrient removal in a novel anaerobic-anoxic/oxic eight-phased system

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## ABSTRACT

An eight-phased AA/O process has advantages of saving energy power, cost, and enhancing nitrogen and phosphorus removal; it does not need equipment for sludge and mixed liquor recycle and also it required small land for construction. A computer program was built based on activated sludge model No. 2d (ASM2d) for simulating the performance of multi-tank AA/O activated sludge process in Wuxi campus, southeast university. The difficulty of simulation is the system operation with unsteadily state condition. The results indicated that the growth rate constant of ammonia oxidizing bacteria was 1.4 day<sup>-1</sup> and yield coefficient was 0.14. According to simulation, heterotrophic organism  $X_{H}$  phosphate accumulating organism  $X_{PAO}$ , and ammonia oxidizing bacteria X<sub>AOB</sub> decreased in the anaerobic tanks because of the lysis reaction. Then the  $X_{H_{c}} X_{PAO}$ , and  $X_{A}$  increased in the aerobic tanks due to aerobic growth. The heterotrophic microorganism; phosphorus accumulating organism; and autotrophic bacteria concentrations increased in quantities by about 56, 36, and 74% in tank one due to changes in the environmental state condition from anaerobic to aerobic and decreased in quantities by about 20, 44, and 0.14% in the tank three due to changes in the environmental state condition from aerobic to anoxic. The ratio of total nitrifying species to total active biomass varied between 1 and 12% in multi-tank AA/O process. The multi-tank AA/O system achieved  $89 \pm 1.3\%$ ,  $87.7 \pm 1.1\%$ , 73.6  $\pm 2.1\%$ , and  $83.7 \pm 0.9\%$  of chemical oxygen demand, NH<sub>4</sub><sup>+</sup> -N, TN, and total phosphorus (TP) removal efficiencies, respectively, during a six-month operation with the effluent meeting Chinese sewage discharge standard GB18918-Grade A.

Keywords: Wastewater; Multi-tank; AA/O; ASM2d; Modeling; Biomass

# 1. Introduction

Over the last 10 years, a number of biological nitrogen and phosphorus removal processes have been used to remove phosphorus with simultaneous nitrification and denitrification process. Most of the phosphorus developed biological nitrogen and removal processes consist of a sequential anaerobic and aerobic stage for biological phosphorus removal

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and recycle mixed liquor into anoxic zones to prop up the removal efficiency of total nitrogen. This approach required more energy for mixed liquid recirculation or addition of additional carbon substrate for denitrification process in anoxic zones accordingly, increasing the operational cost of these processes. Phosphorus and nitrogen removal enhanced via reconfiguring biological nutrient removal processes through canceling internal mixed liquor recirculation. This was done by configuring the process into anaerobic, oxic, anoxic, oxic zones in sequence in southeast university of China. A flow was fed into the anaerobic/anoxic zone by changing intake location. Many types of micro-organisms involved in the complex biological transformation processes, such as heterotrophic organisms, phosphate accumulating organisms, and autotrophic organisms. In order to understand bacterial reactions in biological nutrient removal processes, many different types of mathematical models have been proposed [1,2] and applied in the biological nutrient removal processes [3-6]. Some of them two-stage nitrification models [7,8] and other multi-stage denitrification models [9,10] were proposed in the biological nutrient removal processes. Although these models could predict nitrification or denitrification successfully, the application of these models were merely related to nitrogen removal, that is, the behaviors of heterotrophic organisms, phosphate accumulating organisms, and autotrophic organisms in both nitrogen and phosphorus removal process were not taken into account simultaneously. Activated sludge model No. 2d represents a model for biological phosphorus removal with simultaneous nitrification-denitrification in activated sludge systems. ASM2d is the extension of ASM2 model where it expanded to include the denitrifying activity of the phosphorus accumulating organism ( $X_{PAOs}$ ). Since ASM2d model can be described as multi-stage denitrification and phosphorus removal simultaneously, the objectives of this study are listed as follows: (1) to establish a model (Activated Sludge model No. 2d) in which multi-stage denitrification and phosphorus removal were taken into account simultaneously, (2) to validate the model by exploring the consistency between simulated and observed values of different components including soluble COD S<sub>5</sub>; NH<sub>4</sub>-N; NO<sub>3</sub>-N; and PO<sub>4</sub>-P in multi-tank AA/O process, and (3) to analyze the kinetics of different microorganisms including heterotrophic organisms, phosphate accumulating organisms, and autotrophic organisms in the multi-tank AA/O process.

# 2. Materials and methods

## 2.1. Experimental equipment

The main parts of a pilot plant utilized in this study are the main body which are rectangular box  $750 \times 630 \times 900$  mm, air compressor, pre-static pumps, mechanical agitation mixers, PLC programmable logic control, LCD display screen, inlet wastewater electromagnetic valves, outlet water electromagnetic valves, aeration electromagnetic valves, sludge discharge electromagnetic valves PVC pipes, and others. The principle diagram of pilot plant is shown in Fig. 1. The effective water depth in the five-step continuous flow activated sludge system is 650 mm while the total depth is 900 mm. The plane dimensions of tank two, tank three, and tank four are square planes while tank one and tank five are rectangular planes whereas the effective volumes of tank two, tank three, and tank four are  $250 \times 250 \times 650$  mm, while for tank one and tank five are  $380 \times 290 \times 650$  mm which make volume ratio between rectangular and square tanks,  $v_{tank one}/$ v<sub>tank two</sub>, equal 1.75. An operation cycle is composed of two half cycles with same running schemes, in which the raw wastewater flows from tank one to tank five during the first half cycle, and from tank five to tank one during the second; the first half cycle is similar to second half cycle. The scheme of first half cycle is included in Fig. 1 as bar diagram; it is divided into four phases named as phase I, II, III, and IV, respectively. In this scheme, tank one, tank two, tank three, and tank four operated as reactors and tank five as settler. The direction of flow was changed automatically via changing of intake location so that the system achieved automatic recirculation without equipment to return sludge and mixed liquor. Therefore, this system is effective for reducing energy consumption. Time and environmental state condition were controlled during each phase to achieve the function of AA/O process in the multi-tank system. An optimized removal efficiency of pollutant was achieved at a HRT of 16 h, SRT of 21 day, and air/water ratio of 35% at a temperature range of 19–23°C. The optimized running time was 1.5, 1, 1, and 0.5 h for phase I, II, III, and IV, respectively.

#### 2.2. Data collection and model algorithms

This study was conducted in Wuxi campus, southeast university in four different runs for calibration and parameter estimation and also four different runs for simulation. The raw wastewater was collected from a main manhole every day in a storage tank so it is steady-state simulation. The equations for implementing the calculation of ASM2d were described as



Fig. 1. Layout and algorithms of multi-tank AA/O process during a first half cycle.

follows. First, the basic equation for a mass balance within any defined system boundary was:

Input – Output t + Reaction = Accumulation (1)

Therefore, the summary of the mathematical model equations for the reaction rate of each component could be described as in the following equation:

$$C(t) \times (dC/dt) = (I_{\rm Ki} - O_{\rm Ki} + D_{\rm Ki} - D_{\rm Ki})/(V_{\rm Ki}C_{\rm Ki})$$
(2)

where  $I_{ki}$  and  $O_{ki}$  are input (influent) and output transport terms of the *i*th component in the *k*th tank;  $P_{ki}$  and  $D_{ki}$  are production and degradation terms of the *i*th component in the *k*th tank;  $V_{ki}$  is the volume of the *k*th tank. The reaction term for the *i*th component; and  $r_i$  is obtained by summing the product of the stoichiometric coefficients  $m_{ij}$  (Table 1) and the process rate expression  $e_j$  (Table 2) for the component *i* being considered in the mass balance:

$$r_i = \sum_j v_{ij} \rho_j \tag{3}$$

## 2.3. Sensitivity analysis

The effects of usually large uncertainties parameters in the multi-tank AA/O should be taken into account before starting the simulation of the system via sensitivity analysis. Interval analysis or stochastic techniques could be applied in steady- and transient-state condition [11,12]. In this study, the sensitivity of effluent components for some important parameters was analyzed based on a 5% increased rate in the standard values. All stoichiometrics are four parameters and kinetic parameters include forty-two parameters of ASM2d model. The component concentrations in the influent are sixteen parameters.

The sensitivity analyses of the above parameters (*p*) with respect to effluent components (*E*) were calculated by the following equation;

Sensitivity 
$$= \frac{dE/E}{dp/p}$$
 (4)

Tab. Stoi	le 1 chiometric matrix														
No.	Process	$S_{ m F}$	$S_{\mathrm{A}}$	S <sub>NH</sub>	SNO	$S_{\rm PO}$	S <sub>I</sub> S <sub>ALK</sub>	$X_{\rm S}$	$X_{\rm H}$	XPAO 2	K <sub>A</sub> X <sub>PP</sub>	X <sub>PH</sub>	IA X	$X_{\rm TSS}$	1
-	Aerobic growth on $S_{\rm F}$	$-\frac{1}{Y_{H}}$		$V_{1,\rm NH4}$		$V_{1,\rm PO4}$			-						1
0	Aerobic growth on $S_{\rm A}$		$-rac{\gamma_{\rm H}}{\gamma_{\rm H}}$	$V_{2,\rm NH4}$		$V_{2,PO4}$			1						
б	Anoxic growth on S., denitrification (S.,o)	$-rac{1}{Y_{ m H}}$	1	$V_{3,\rm NH4}$	$rac{1-Y_H}{2.85Y_H}$	$V_{3,PO4}$			1						
4	Anoxic growthon S <sub>A</sub> , denitrification (S <sub>NO</sub> )		$-\frac{1}{Y_{\rm H}}$	$V_{4,\rm NH4}$	$rac{1-Y_H}{2.85Y_H}$	$V_{4,\rm PO4}$			1						
Ŋ	Fermentation	-1		$V_{5,\rm NH4}$		$V_{5,\rm PO4}$									
9	Lysis			$V_{6,\rm NH4}$		$V_{6,\rm PO4}$		1- f <sub>v1</sub>	-1				f <sub>x</sub>	_	
	Aerobic arowth of X.	$-\frac{3.43-Y_{\rm AOB}}{Y_{\rm AOB}}$		$V_{7,{ m NH4}}$		$-i_{PBM}$		Ŕ							
×	brown or AA Lysis	YNOB		$V_{8,\rm NH4}$		$V_{8,PO4}$		<u>'</u>			-1		fx	_	
		•		11111/0		<b>EO 1</b> /0		f <sub>XI</sub>					<		
6	Aerobic hydrolysis	l-t <sub>SI</sub>		V9,NH4			tsi V <sub>9,Alk</sub>							$V_{9,\mathrm{Ts}}$	~
10	Anoxic	$1-f_{SI}$		$V_{10,}$			$f_{\rm SI}$ $V_{10,}$	-1						$V_{10,}$	
	hydrolysis			NH4			Alk							$T_{\rm SS}$	
11	Anaerobic	$1-f_{\rm SI}$		$V_{11,}$			$f_{\rm SI} V_{11,}$	1						$V_{11,}$	
12	nyurolysis Storage of X <sub>PHA</sub>		-1	NH4		$\gamma_{\rm PO4}$	AIk				1	1		Tss	
13	Aerobic					-  -					1 Y <sub>PC</sub>	)4 			
	storage of X <sub>PP</sub>											$Y_{\rm PH}$	Γ		
14	Anoxic storage of X <sub>PP</sub> , denitrification (S <sub>NO</sub> )				$V_{15,NO3}$	-1						-	P		
15	Aerobic growth of $X_{\rm PAO}$			$V_{16,}$		$-\mathrm{i}_{\mathrm{PBM}}$				_		$-\frac{1}{Y_{\rm F}}$	1 =		
16	Anoxic growth $X_{PAO}$ , denitrification			$V_{17,}$	$-V_{17,}$	$-i_{PBM}$				_		$-\frac{1}{Y_F}$			
17	Lysis of X <sub>PAO</sub>			$V_{18,}$	NO3	$V_{18,}$		, <del>',</del>		-1			$f_X$	_	
18	Lysis of X <sub>PP</sub>			NH4		P04 1		$\mathbf{f}_{\mathrm{XI}}$							
19	Lysis of X <sub>PHA</sub>		1									-1			

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Table 2		
Process	rate	equations

j	Process	Process rate equation $\rho_{j'}\rho_j \ge 0 \ (M_1 L^{-3} T^{-1})$
He	terotrophic organisms: X <sub>H</sub>	
1	Aerobic growth on $S_{\rm F}$	$\mu_{\rm H} \frac{S_{02}}{K_{\rm O2H}+S_{\rm O2}} \frac{S_F}{K_{\rm FH}+S_F} \frac{S_F}{S_{\rm S}+S_F} \frac{S_{\rm NH}}{K_{\rm NH4H}+S_{\rm NH}} \frac{S_{\rm PO}}{K_{\rm FH}+S_{\rm PO}} \frac{S_{\rm ALK}}{K_{\rm ALK}+S_{\rm ALK}} X_{\rm H}$
2	Aerobic growth on $S_A$	$\mu_{H} \frac{S_{02}}{K_{02H}+S_{02}} \frac{S_{A}}{K_{AH}+S_{A}} \frac{S_{A}}{S_{A}+S_{F}} \frac{S_{NH}}{K_{NH4H}+S_{NH}} \frac{S_{PO}}{K_{PH}+S_{PO}} \frac{S_{ALK}}{K_{ALK+S_{ALK}}} X_{H}$
3	Anoxic growth on $S_{\rm F}$ , denitrification ( $S_{\rm NO}$ )	$\mu_H \eta_{NO3H} \frac{K_{02H}}{K_{02H} + S_{02}} \frac{S_{NO}}{K_{NO3H} + S_{NO}} \frac{S_F}{K_{FH} + S_H} \frac{S_A}{S_A + S_F} \frac{S_{NH}}{K_{NH4H} + S_{NH}} \frac{S_{PO}}{K_{PH} + S_{PO}} \frac{S_{ALK}}{K_{ALK} + S_{ALL}} X_H$
4	Anoxic growth on $S_A$ , denitrification ( $S_{NO}$ )	$\mu_H \eta_{NO3H} \frac{K_{02H}}{K_{02H} + S_{02}} \frac{S_{NO}}{K_{NO3H} + S_{NO}} \frac{S_A}{K_{FH} + S_F} \frac{S_A}{S_A + S_F} \frac{S_{NH}}{K_{NH4H} + S_{NH}} \frac{S_{PO}}{K_{PH} + S_{PO}} \frac{S_{ALK}}{K_{ALK} + S_{ALL}} X_H$
5	Fermentation	$q_{\text{fe}} \frac{K_{\text{O2H}}}{K_{\text{O2H}} + S_{\text{O2}}} \frac{K_{\text{NO3H}}}{K_{\text{NO3H}} + S_{\text{NO}}} \frac{S_{\text{F}}}{K_{\text{fe}} + S_{\text{F}}} \frac{S_{\text{ALK}}}{K_{\text{ALK}} + S_{\text{ALK}}} X_{\text{H}}$
6	Lysis	$b_{\rm H}X_{\rm H}$
Am	monia oxidizers (nitrifying or	ganisms, autotrophic): $X_A$
7	Aerobic growth of $X_{AOB}$	$\mu_{AOB} \frac{S_{O2}}{K_{COLOR} + S_{CO}} \frac{S_{NH}}{K_{VIIIIOR} + S_{PO}} \frac{S_{ALK}}{K_{VIIIIOR} + S_{AIK}} X_{AOB}$
8	Lysis	$b_{AOB}X_{AOB}$
Hy	drolysis process	
9	Aerobic hydrolysis	$K_k \frac{S_{\text{O2S}}}{K_{\text{O2S}}+S_{\text{O2}}} \frac{X_S/X_H}{K_{\text{XS}}+X_S/X_H} X_H$
10	Anoxic hydrolysis	$K_{ m h}\eta_{ m NO3S}rac{K_{ m O2S}}{K_{ m O3S}+S_{ m O2}}rac{S_{ m NO}}{K_{ m NO3S}+S_{ m NO}}rac{X_{ m S}/X_{ m H}}{K_{ m XS}+X_{ m S}/X_{ m H}}X_{ m H}$
11	Anaerobic hydrolysis	$K_h\eta_{fe} \frac{K_{NO2S}}{K_{O2S}+S_{O2}} \frac{K_{NO3S}}{K_{NO3S}+S_{NO}} \frac{X_S/X_H}{K_{XS}+X_S/X_H} X_H$
Pho	osphorus accumulating organis	sms (PAO): X <sub>PAO</sub>
12	Storage of X <sub>PHA</sub>	$q_{\text{PHA}} \frac{S_{\text{A}}}{K_{\text{APAO}} + S_{\text{A}}} \frac{S_{\text{ALK}}}{K_{\text{ALKPAO}} + S_{\text{ALK}}} \frac{X_{\text{PP}}/X_{\text{PAO}}}{K_{\text{PP}} + X_{\text{PP}}/X_{\text{PAO}}} X_{\text{PAO}}$
13	Aerobic storage of $X_{PP}$	$q_{\mathrm{PP}} \frac{S_{\mathrm{O2}}}{K_{\mathrm{O2PAO}} + S_{\mathrm{O2}}} \frac{S_{\mathrm{PO}}}{K_{\mathrm{PS}} + S_{\mathrm{PO}}} \frac{S_{\mathrm{ALK}}}{K_{\mathrm{ALKPAO}} + S_{\mathrm{ALK}}} \frac{X_{\mathrm{PHA}}/X_{\mathrm{PAO}}}{K_{\mathrm{PHA}}/X_{\mathrm{PAO}}} \frac{K_{\mathrm{MAX}} - X_{\mathrm{PP}}/X_{\mathrm{PAO}}}{K_{\mathrm{IPP}} + K_{\mathrm{MAX}} - X_{\mathrm{PP}}/X_{\mathrm{PAO}}} X_{\mathrm{PAO}}$
14	Anoxic storage of $X_{PP}$ , denitrification ( $S_{NO}$ )	$q_{\text{PP}}\eta_{\text{NO3PAO}} \frac{K_{\text{O2PAO}}}{S_{\text{O2}}} \frac{S_{\text{NO}}}{K_{\text{NO3PAO}} + S_{\text{NO}}} \frac{S_{\text{O2}}}{K_{\text{O2PAO}} + S_{\text{O2}}} \frac{S_{\text{PO}}}{K_{\text{PS}} + S_{\text{PO}}} \frac{S_{\text{ALK}}}{K_{\text{ALKPAO}} + S_{\text{ALK}}} \frac{X_{\text{PHA}}/X_{\text{PAO}}}{K_{\text{PHA}}/X_{\text{PAO}}} \frac{K_{\text{MAX}} - X_{\text{PP}}/X_{\text{PAO}}}{K_{\text{IPP}} + K_{\text{MAX}} - X_{\text{PP}}/X_{\text{PAO}}} X_{\text{PAO}}$
15	Aerobic growth of $X_{PAO}$	$\mu_{\text{PAO}} \frac{S_{\text{O2}}}{K_{\text{O2}\text{PAO}} + S_{\text{O2}}} \frac{S_{\text{NH}}}{K_{\text{NH}\text{PAO}} + S_{\text{NH}}} \frac{S_{\text{PO}}}{K_{\text{PA}\text{PA}} + S_{\text{PA}\text{O}}} \frac{S_{\text{ALK}}}{K_{\text{PA}\text{A}} + S_{\text{ALK}}} \frac{X_{\text{PA}\text{A}}/X_{\text{PAO}}}{K_{\text{PA}\text{A}}/X_{\text{PAO}}} X_{\text{PAO}}$
16	Anoxic growth of $X_{PAO}$ , denitrification ( $S_{NO}$ )	$\mu_{PAO}\eta_{NO3PAO} \frac{K_{O2PAO}}{S_{O2}} \frac{S_{NO}}{K_{NO3PAO} + S_{NO}} \frac{S_{NO}}{K_{O2PAO} + S_{O2}} \frac{S_{NH}}{K_{NH4PAO} + S_{NH}} \frac{S_{PO}}{K_{PPAO} + S_{PO}} \frac{S_{ALK}}{K_{ALKPAO} + S_{ALK}} \frac{X_{PHA}/X_{PAO}}{K_{PHA} + X_{PHA}/X_{PAO}} X_{PAO}$
17	Lysis of X <sub>PAO</sub>	b <sub>PAO</sub> X <sub>PAO</sub>
18	Lysis of X <sub>PP</sub>	b <sub>PP</sub> X <sub>PP</sub>
19	Lysis of X <sub>PHA</sub>	D <sub>PHA</sub> X <sub>PHA</sub>

where dp is the change in the parameter value p and dE is the change in the output E.

The effluent component concentrations (*E*) have different sensitivities towards different parameters (*P*) according to sensitivity analysis via above equation. This study showed that the effluent ammonia-nitrogen and nitrate-nitrogen had a sensitivity of more than one towards five parameters, influentNH<sub>4</sub>-N,  $\mu_A$ ,  $Y_{PO4}$ ,  $q_{pp}$  and  $Y_{PO4}$ ; the effluent nitrate-nitrogen had sensitivity of more than one towards four parameters, influent flow-rate,  $\mu_A$ ,  $Y_H$ ,  $Y_{PO4}$ . The effluent PO<sub>4</sub>-P has more sensitivity towards PO<sub>4</sub>-P,  $q_{PHA}$ ,  $q_{PP}$ ,  $\mu_{PAO}$ ,  $Y_H$ ,  $K_{MAX}$ ,  $Y_{PO4}$ .

#### 2.4. Model calibration

There are many parameters in ASM2d model. For those parameters that are known to be approximately constant in domestic wastewater, the default values from previous research studies [3,13] were used as shown in Table 3.

Model calibration procedure is a process of adjusting coefficient values of the model as shown in Fig. 2, therefore the results simulated by the ASM2d model with these coefficients closely agree with the observed data. The model parameters are highly dependent on environmental state conditions. The parameter values are estimated by minimizing the sum of squares of

Table 3

Raw wastewater characteristics of Wuxi campus, Southeast University

Item	Symbol no.	Concentration (mg/L)				
Case study		1	2	3	4	
Total chemical oxygen demand	COD in-filtrated	805	688	458	513	
Particulate inert organic material	$X_{\mathrm{I}}$	63	61	55	59	
Slowly biodegradable substrate	$X_{\rm S}$	340	297	201	222	
Readily biodegradable substrate	Ss	306	261.5	174	195	
Active heterotrophic biomass	$X_{\mathrm{H}}$	5	4	4	1	
Active autotrophic biomass	$X_{\mathbf{A}}$	0.1	0.7	0.3	0.0	
Volatile fatty acids	$S_{\mathbf{A}}$	88	73	61	67	
Inert soluble organic material	$S_{\mathrm{I}}$	7	5	4	4	
Oxygen	So	0	0	0	0	
Nitrate nitrogen	S <sub>NO</sub>	2.23	1.23	1.26	2.8	
Ammonia nitrogen	$S_{\rm NH}$	18	27	32	19.4	
Total nitrogen	TN	31.7	39.6	43.2	33.1	
PO <sub>4</sub> -P	S <sub>PO</sub>	2.59	3.25	3.41	1.01	
Total nitrogen	TP	3.07	3.71	4.32	1.79	
Alkalinity	$S_{ALK}$	4.97	5.01	4.99	5.00	
Mixed liquor suspended solid	MLSS	87	73	71	67	

the deviations between the observed data and the model predictions data with the objective function given in the following equation [14]:

$$R^{2} = \frac{\sum (\text{Sim} - \text{aobs})^{2}}{\sum (\text{Sim} - \text{aobs})^{2} + \sum (\text{Sim} - \text{obs})^{2}}$$
(5)

where  $R^2$  is the coefficient of determination, sim is the model simulated value, obs is the observed value, and aobs is the average observed value.

The standard deviation for parameter determination was required to be lower than 50% to ensure the validity of the values of the parameters obtained. To make the first move of the calibration procedure, an initial guess of the parameters is essential. Such initial values are obtained with the values in the literature as shown in Table 3. To make simpler calibration process, it is preferred to change little constants as possible, due to the limited changeability of some parameters. The choice of the parameters for calibration is mostly based on the result of sensitivity analysis.

## 2.5. Analytical methods

COD, NH<sub>4</sub>-N, NO<sub>3</sub>-N, PO<sub>4</sub>-P, TP, and TN were analyzed according to standard methods [16]. NO<sub>3</sub>-N were analyzed by the IC method (Metrohm 761 compact IC equipped with metrosep asupp 5 column) and TN was analyzed by analytikjena AG multi N/C 3000.

# 2.5.1. Biomass batch tests

The procedures were fully or partially adopted from Standard Methods [17] or previous studies [18-21]. In order to determine the kinetic parameters of X<sub>AOB</sub>, we determined oxygen uptake rate of different microbial functional group for calculation [22,23]. Batch experimental tests were performed for four different runs for determining the kinetic parameters of X<sub>AOB</sub> and X<sub>NOB</sub>. The oxygen uptake rate measuring system consisted of four airtight, cylindrical chambers, with same height and volume, four magnetic stirrers for stirring, and an aeration stone in each chamber. DO was monitored by four oxygen meters of high stability connected to a data acquisition system. Since this oxygen uptake rate measurer was airtight, the actual respiration rate of the tested biomass at any time during the batch test did not depend on oxygen input. Therefore, the dissolved oxygen concentration represented the actual oxygen uptake rate. A certain amount of activated sludge sample was taken from the pilot plants and added into oxygen uptake rate chambers. Distilled water containing organic carbon source and nutrient including glucose, NH<sub>4</sub>SO<sub>4</sub>, and KH<sub>2</sub>PO<sub>4</sub> were added resulting in total volume of 800 mL in chamber. The measuring system was periodically aerated, then the difference between the measured OUR and baseline oxygen respiration was calculated and compared. The pH value was maintained at seven during batch test. In order to evaluate the kinetic parameters and active biomass of  $X_{H\nu}$ 



Fig. 2. Illustration of parameter estimation routine [15].

 $X_{AOB}$ , and  $X_{NOB}$  different types of oxygen uptake rate values should be considered: total oxygen uptake rate  $(OUR_T)$ , oxygen uptake rate of  $X_H$   $(OUR_H)$ , and oxygen uptake rate of  $X_{AOB}$  (OUR<sub>AOB</sub>). The determination of oxygen uptake rates of  $X_{H}$ ,  $X_{AOB}$ , and  $X_{NOB}$  was based on the subsequent addition of allylthiourea (ATU) and NaN<sub>3</sub>. Allylthiourea (86 µM) was added to the chambers to keep the NH<sub>4</sub>-N concentration constant during the incubation by selectively inhibiting  $X_{AOB}$  activity without affecting the activity of  $X_{NOB}$ while Azide (86 µM) was added to the chambers to keep the NO<sub>2</sub>-N concentration constant during the incubation by selectively inhibiting X<sub>NOB</sub> activity without affecting the activity of X<sub>AOB</sub> [24]. When determining  $OUR_{T}$ , no inhibitor was added. When determining  $OUR_{H_{\ell}}$  both allylthiourea (86 µM) and NaN<sub>3</sub> (24 µM) were added. If only NaN<sub>3</sub> (24 µM) was added, the determined oxygen uptake rate was the sum of OUR<sub>H</sub> and  $OUR_{AOB}$ , then  $OUR_{NOB} = (OUR_{H} + OUR_{AOB}) - OUR_{H} + OUR_{AOB}$ OUR<sub>H</sub>.

# 2.5.2. PHA test

The initial concentration of PHA in each zone of a new system was analyzed according to the method that is described in Ref. [25] for estimating initial concentration of PHA in each zone. In the initial step, duplicate 20 mL samples of MLSS was obtained and immediately centrifuged at 4°C. Then, the cold sludge pellet was lyophilized. After that, the pellet was added to the tube closed with a Teflon-lined screw cap for drying. About 2 mL of sulfuric acid, 3% methanol, and 2 mL of chloroform were added to the tube. This was digested for 1,200 min in an oven at 104°C. At the second step, once the sample had cooled at 25°C, 1 mL of water was added and the tube contents were shaken for 600 s. The chloroform content remained at the bottom of the tube, and this was drawn off for GC examination. The digested product was exposed on a Varian 3400 GC fitted with a 1.8-m Alltech 0.2% Carbowax 1500 on Graphpac-GC 80/100 mesh stainless steel column. The column temperature was 170°C and the



Fig. 3. Diagram depicting the retention/passage of influent wastewater COD components [26].

inoculation temperature was 180°C. PHA was measured by comparison to a standard consisting of a copolymer of the above-described alkanoates.

#### 2.5.3. Wastewater characterization

Activated sludge models (ASM) distinguish between the mechanisms acting on different components in the influent wastewater stream. The term wastewater characteristic refers to the partitioning of influent organic material into biodegradable and unbiodegradable (inert) portions, the ammonia portion of the total nitrogen, and so on. The influent wastewater is often varied from one municipal wastewater to another. Wastewater characteristics have a very significant impact on system performance, particularly for nutrient removal systems.

Characterization of the carbonaceous material in municipal wastewater for modeling purposes was usually in terms of the chemical oxygen demand (COD). The division of the total influent COD ( $COD_T$ ) into the various fractions used in nutrient removal system design and modeling is shown in Fig. 3. In ASM2d model, the  $COD_{tot}$  of the wastewater consisted of inert soluble organic matter (S<sub>I</sub>), readily and slowly biodegradable substrate (S<sub>S</sub> and X<sub>S</sub>, respectively), and inert suspended organic matter (X<sub>I</sub>), whereas biomass in the wastewater is considered to be insignificant.

# 2.6. Wastewater quality

The raw wastewater used in the experiment was collected from a main manhole of southeast university in Wuxi city and the characteristic of wastewater quality is listed in Table 3. In this study, four testing runs with different operations were implemented in Wuxi campus, southeast university. The raw wastewater is typical in Wuxi city-southeast university, China. COD infiltrated was between 150 and 850 mg/L with average of 650 mg/L, of which S<sub>5</sub>, S<sub>1</sub>, X<sub>5</sub>, and X<sub>I</sub> accounted for about 38, 2, 43, and 11%, respectively. MLSS was between 45 and 93 mg/L with average of 76 mg/L. NH<sub>4</sub>-N was between 10 and 40 mg/L with average of 22 mg/L. TP was between 1.7 and 4.5 mg/L with average of 2.6 mg/L, of which PO<sub>4</sub>-P accounted for about 70–90%.

#### 2.7. Model structure of the system

The model structure was built using stoichiometric matrix Table 1, process rate Table 2, algorithms, and multi-tank AA/O environmental state conditions during each phase. The algorithms of multi-tank AA/O

are shown in Fig. 2. The model structure has taken the environmental state condition changing of every tank and phase time into consideration.

The equations that described the transformation of the wastewater quality in the model formed an ordinary differential equations (ODEs) system. The set of equations in this model then was integrated simultaneously by the fourth-order range Kutta numerical analysis integration method [27]. According to the program structure of multi-tank AA/O, the entire model was implemented by means of a computer program that was coded with MATLAB<sup>®</sup>2010 language. When all the vectors  $\frac{1}{C_{ti}} \left( \frac{dC}{dt} \right)$  were nearly equal to zero, a steady state was reached. The integration was most accurate when time step is very small but the computing time increased inversely with the size of time step. Conversely, too large time step would result in large errors and other numerical problems. Thus, one criterion for an upper limit on time step is:

$$\Delta t < -C(t) \times \left(\frac{\mathrm{d}C}{ct}\right)^{-1} \tag{6}$$

where  $\Delta t$  is time step. By combining Eqs. (2) and (4), and neglecting the  $F_{ki}$  and  $P_{ki}$  terms in the mass balance, resulted in an equation for the maximum step size:

$$\Delta t < \frac{V_k C_{ki}}{O_{ki} + K_{ki}} = \theta_{ki} \tag{7}$$

The term  $\theta_{ki}$  is the mean residence time of component i in reactor component *k* at steady state.

## 3. Results and discussion

#### 3.1. Removal efficiency

According to investigation results, this system achieved  $89 \pm 1.3\%$ ,  $87.7 \pm 1.1\%$ ,  $73.6 \pm 2.1\%$ , and  $83.7 \pm 0.9\%$  of S<sub>S</sub>, NH<sup>+</sup><sub>4</sub>-N, TN, and TP removal efficiencies, respectively, during a six-month operation with the effluent meeting Chinese sewage discharge standard GB18918-Grade A. The results showed that this system operates with SND and denitrifying phosphorus removal phenomena which are benefits for enhancing nitrogen and phosphorus removal and also reducing energy power because it needs low dissolved oxygen concentration.

## 3.2. Model evaluation

The model evaluation is performed from the comparison between the predicated and observed values.



Fig. 4. Simulated and observed COD, NH<sub>4</sub>-N, NO<sub>3</sub>-N, and PO<sub>4</sub>-P in tank one of multi-tank A2/O process.

The experimental data of four related runs in southeast university -Wuxi campus are used for model evaluation. The influent raw wastewater characteristics are shown in Table 3. The predicated and observed are shown in Figs. 4-7 for all related runs. Figs. 4-7 shows the simulated and observed COD, NH<sub>4</sub>-N, NO<sub>3</sub>-N, and PO<sub>4</sub>-P in tank one, tank two, tank three, and tank four, respectively, of multi-tank AA/O activated sludge process. Fig. 4 depicts the observed and predicated data of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N concentration of tank one under four runs, This figure shows a good consistency between the observed and predicated data whereas the sum of squares of the deviations  $R^2$  of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N were 0.95, 0.96, 0.93, and 0.98, respectively, at run 1; 0.98, 0.95, 0.91, and 0.97, respectively, at run 2; 0.99, 0.95, 0.87, and 0.99, respectively, at run 3; and 0.95, 0.97, 0.87 and 0.92, respectively, at run 4. Fig. 5 depicts the observed and predicated data of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N concentration of tank two under four runs. This figure shows a good consistency between the observed and predicated data whereas the sum of squares of the deviations  $R^2$  of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N were 0.95, 0.73, 0.94, and 0.99, respectively, at run 1; 0.99, 0.89, 0.95, and 0.99, respectively, at run 2; 0.99, 0.89, 0.97, and 0.98, respectively, at run 3; and 0.97, 0.86, 0.97, and 0.98, respectively at run 4. Fig. 6 depicts the observed and predicated data of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N concentration of tank three under four runs. This figure shows good consistency between the observed and predicated data whereas the sum of squares of the deviations  $R^2$  of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N were 0.95, 0.66, 0.95, and 0.95, respectively, at run 1; 0.96, 0.77, 0.95, and 0.95, respectively, at run 2; 0.98, 0.63, 0.95, and 0.99, respectively, at run 3; and 0.97, 0.74, 0.95, and 0.997, respectively, at run 4. Fig. 7 depicts the observed and predicated data of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N concentration of tank four under four runs. This figure shows a good consistency between the observed and predicated data whereas the sum of squares of the deviations  $R^2$ of NH<sub>4</sub>-N, PO<sub>4</sub>-P, COD, and NO<sub>3</sub>-N were 0.96, 0.56, 0.96, and 0.98, respectively, at run 1; 0.97, 0.61, 0.93, and 0.96, respectively, at run 2; 0.99, 0.60, 0.95, and 0.94, respectively, at run 3; and 0.95, 0.59, 0.96, and 0.99, respectively, at run 4.



Fig. 5. Simulated and observed COD, NH<sub>4</sub>-N, NO<sub>3</sub>-N, and PO<sub>4</sub>-P in tank two of multi-tank A2/O process.



Fig. 6. Simulated and observed COD, NH<sub>4</sub>-N, NO<sub>3</sub>-N, and PO<sub>4</sub>-P in tank three of multi-tank A2/O process.



Fig. 7. Simulated and observed COD, NH<sub>4</sub>-N, NO<sub>3</sub>-N, and PO<sub>4</sub>-P in tank four of multi-tank A2/O process.



Fig. 8. Variations of biomass in each tank of multi-tank AA/O process.

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Table 4 Definition and typical values for kinetic parameters

Heterotrophic organisms: $X_{H}$ III6.00g $X_{9}$ g $^{-1}$ $X_{H}$ d $^{-1}$ $\mu_{0}$ Maximum relate of rementationModified3.3g $X_{9}$ g $^{-1}$ $X_{H}$ d $^{-1}$ $\eta_{0,CH}$ Reduction factor for denitrification ( $S_{NO}$ )Modified0.6- $h_{1}$ Reduction factor for denitrification ( $S_{NO}$ )Modified0.6- $h_{1}$ Rate constant for system and decayII0.4d $^{-1}$ $K_{20}$ Saturation coefficient for rementation on $S_{5}$ II4g COD m $^{-3}$ $K_{41}$ Saturation coefficient for growth on scattle $S_{5}$ III4g COD m $^{-3}$ $K_{41}$ Saturation coefficient for growth on acetate $S_{5}$ III4g COD m $^{-3}$ $K_{41}$ Saturation coefficient for phosphate (nutrient)III0.01g N m $^{-3}$ $K_{41}$ Saturation coefficient for ankalinity (HCOs)III0.01g N m $^{-3}$ $K_{41}$ Saturation coefficient for akalinity (HCOs)III0.1mode HCO $^{-3}$ m $^{-3}$ $K_{42}$ Maximum growth rate of $X_{A06}$ Modified1.4d $^{-1}$ $K_{64}$ Maximum growth rate of prosphorus (nutrient)III0.01g N m $^{-3}$ $K_{44}$ Gaturation coefficient for any growt (nutrient)III0.01g N m $^{-3}$ $K_{64}$ Gaturation coefficient for prosygenIII0.5g O m $^{-3}$ $K_{64}$ Hydrolysis reduction factorII0.01g P m $^{-2}$ $K_{64}$ Hydrolysis reduction fac	Item	Description	Ref.	20°c	Units
$\mu_{\rm H}$ Maximum growth rate on substrate[1]6.00g X <sub>0</sub> g s <sup>-1</sup> X <sub>H</sub> d <sup>-1</sup> $\mu_{\rm e}$ Maximum rate for fermentationModified3.0g X <sub>0</sub> g s <sup>-1</sup> X <sub>H</sub> d <sup>-1</sup> $N_{\rm NOHI}$ Reduction factor for denitrification (S <sub>NO</sub> )Modified0.6- $h_{\rm H}$ Rate constant for lysis and decay[1]0.4d <sup>-1</sup> $K_{\rm CD1}$ Saturation inhibition coefficient for growth on $S_{N}$ [1]4.4g COD m <sup>-3</sup> $K_{\rm RL}$ Saturation coefficient for growth on $S_{N}$ [1]4.g COD m <sup>-3</sup> $K_{\rm AL}$ Saturation coefficient for growth on acetate $S_{\Lambda}$ [1]4.g COD m <sup>-3</sup> $K_{\rm SOHI}$ Saturation coefficient for nitrate[1]0.01g N m <sup>-2</sup> $K_{\rm SOHI}$ Saturation coefficient for phosphate (nutrient)[1]0.01g N m <sup>-3</sup> $K_{\rm SOHI}$ Saturation coefficient for Alachinity (HCO <sub>2</sub> )[1]0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{\rm AL}$ Saturation coefficient for axonsModified1.4d <sup>-1</sup> $K_{\rm COD}$ Decay rate of $X_{\rm AOB}$ Modified1.4d <sup>-1</sup> $K_{\rm COD}$ Decay rate of $X_{\rm AOB}$ Modified1.4d <sup>-1</sup> $K_{\rm COD}$ Decay rate of $X_{\rm AOB}$ Modified1.4d <sup>-1</sup> $K_{\rm COD}$ Saturation coefficient for phosphares (nutrient)[1]0.5g O 2 m <sup>-3</sup> $K_{\rm ALL}$ Saturation coefficient for physice Nutrient)[1]0.5g O 2 m <sup>-3</sup> $K_{\rm ALL}$ Saturation coefficient for physice Nutrient)[1]		Heterotrophic organisms: $X_{H}$			
Animum PROSHMaximum rate for fermentationModified3.3g X_g S g g g s hReduction factor for denirification (Syo)Modified3.3g X_g S g g g g hReduction factor for denirification (Syo)Modified3.3g X_g g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g X_g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g g h3.3g g g g g h3.3g g g g g h3.3g g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3g g g g h3.3 <th< td=""><td><math>\mu_{\mathrm{H}}</math></td><td>Maximum growth rate on substrate</td><td>[1]</td><td>6.00</td><td><math>g X_{S} g^{-1} X_{H} d^{-1}</math></td></th<>	$\mu_{\mathrm{H}}$	Maximum growth rate on substrate	[1]	6.00	$g X_{S} g^{-1} X_{H} d^{-1}$
Moduli ProtocolReduction factor for denitrification (SNO)Modified 0.60.60.70.7 $b_{H}$ Rate constant for lysis and decay[1]0.2g O2 m <sup>-3</sup> $K_{H1}$ Saturation coefficient for oxygen[1]4g COD m <sup>-3</sup> $K_{Ri}$ Saturation coefficient for growth on $S_{F}$ [1]4g COD m <sup>-3</sup> $K_{Ki}$ Saturation coefficient for annonium (nutrient)110.05g N m <sup>-3</sup> $K_{Ki}$ Saturation coefficient for annonium (nutrient)110.01g N m <sup>-3</sup> $K_{Ki}$ Saturation coefficient for phosphate (nutrient)110.01g N m <sup>-3</sup> $K_{Ki}$ Saturation coefficient for annonium (nutrient)110.01g N m <sup>-3</sup> $K_{AL}$ Saturation coefficient for AgainModified1.4d <sup>-1</sup> $K_{AL}$ Saturation coefficient for annonium (nutrient)110.01g N m <sup>-3</sup> $K_{AL}$ Saturation coefficient for annonium (nutrient)110.5g Q 2 m <sup>-3</sup> $K_{AL}$ Saturation coefficient for annonium (nutrient)110.5g Q 2 m <sup>-3</sup> $K_{AL}$ Saturation coefficient for phospharus (nutrient)110.5g Q 2 m <sup>-3</sup> $K_{AL}$ Saturation coefficient for phospharus (nutrient)110.01g P m <sup>-3</sup> $K_{AL}$ Hydrolysis rate constant110.01g P m <sup>-3</sup> $K_{AL}$ Hydrolysis rate constant110.6- $K_{AL}$ Hydrolysis rate constant110.6- $K_{AL}$ Hydrolysis r	9fe	Maximum rate for fermentation	Modified	3.3	$g X_{S} g^{-1} X_{H} d^{-1}$
NoteIntervalIntervalIntervalIntervalKorntSaturation /inhibition coefficient for oxygenII0.4d <sup>-1</sup> KorntSaturation coefficient for growth on SpII4g COD m <sup>-3</sup> KatSaturation coefficient for growth on SpIII4g COD m <sup>-3</sup> KatSaturation coefficient for growth on SpIII4g COD m <sup>-3</sup> KAtHSaturation coefficient for antrateIII0.5g N m <sup>-3</sup> KAtHSaturation coefficient for alkalinity (HCO)III0.01g N m <sup>-3</sup> KALSaturation coefficient for alkalinity (HCO)III0.1mole HCO <sup>-3</sup> m <sup>-3</sup> KALSaturation coefficient for alkalinity (HCO)III0.1mole HCO <sup>-3</sup> m <sup>-3</sup> KALSaturation coefficient for ammonium (nutrient)III0.5g O2 m <sup>-3</sup> KALSaturation coefficient for ammonium (nutrient)III0.5g N m <sup>-3</sup> KoboDecay rate of XAOBModified0.08d <sup>-1</sup> KotaconSaturation coefficient for ammonium (nutrient)III0.5g N m <sup>-3</sup> KataconSaturation coefficient for alkalinity (HCO <sup>-3</sup> )III0.5g N m <sup>-3</sup> KataconSaturation coefficient for alkalinity (HCO <sup>-3</sup> )III0.5g N m <sup>-3</sup> KataconSaturation coefficient for alkalinity (HCO <sup>-3</sup> )III0.5g N m <sup>-3</sup> KataconsSaturation coefficient for alkalinity (HCO <sup>-3</sup> )III0.6-KataconsSaturation coefficient for phospheres (nutrient)III	MNO2H	Reduction factor for denitrification $(S_{NO})$	Modified	0.6	-
$\tilde{X}_{O2H}$ Saturation/inhibition coefficient for oxygen[1]0.2g O2 m^{-3} $K_{H}$ Saturation coefficient for growth on $S_{F}$ [1]4g COD m^{-3} $K_{AH}$ Saturation coefficient for growth on acetate $S_{A}$ [1]4g COD m^{-3} $K_{AH}$ Saturation coefficient for growth on acetate $S_{A}$ [1]4g COD m^{-3} $K_{NHH}$ Saturation coefficient for ammonium (nutrient)[1]0.05g N m^{-3} $K_{NHH}$ Saturation coefficient for phosphate (nutrient)[1]0.01g N m^{-3} $K_{AL}$ Saturation coefficient for alkalinity (HCO <sub>3</sub> )[1]0.1mole HCO <sup>-3</sup> m^{-3} $K_{AL}$ Saturation coefficient for oxygen[1]0.5g O2 m^{-3} $K_{AL}$ Saturation coefficient for alkalinity (HCO <sub>3</sub> )[1]0.5g O2 m^{-3} $K_{AL}$ Saturation coefficient for argo (NT)[1]0.01g N m^{-3} $K_{AL}$ Saturation coefficient for oxygen[1]0.5g O2 m^{-3} $K_{AL}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.01g P m^{-3} $K_{AL}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.01g P m^{-3} $K_{AL}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.6- $K_{AL}$ Saturation coefficient for oxygen[1]0.6- $K_{AL}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.6- $K_{AL}$ Saturation coefficient for oxygen[1]0.6-<	b <sub>H</sub>	Rate constant for lysis and decay	[1]	0.4	$d^{-1}$
KmSaturation coefficient for growth on $S_{P}$ [1]4g COD m <sup>-3</sup> $K_{e}$ Saturation coefficient for fermentation on $S_{A}$ [1]4g COD m <sup>-3</sup> $K_{AM}$ Saturation coefficient for growth on celtale $S_{A}$ [1]4g COD m <sup>-3</sup> $K_{NM}$ Saturation coefficient for nitrate[1]0.5g N m <sup>-3</sup> $K_{NH}$ Saturation coefficient for alkalinity (HCO <sub>3</sub> )[1]0.01g N m <sup>-3</sup> $K_{ML}$ Saturation coefficient for alkalinity (HCO <sub>3</sub> )[1]0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{AL}$ Saturation coefficient for alkalinity (HCO <sub>3</sub> )[1]0.1mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{AL}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5g O2 m <sup>-3</sup> $K_{02AOB}$ Saturation coefficient for anklonity (HCO <sup>-3</sup> )[1]0.5g O2 m <sup>-3</sup> $K_{02AOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.01g N m <sup>-3</sup> $K_{14AOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m <sup>-3</sup> $K_{14AOB}$ Saturation coefficient for phale nutritient)[1]0.01g P m <sup>-3</sup> $K_{14AOB}$ Saturation coefficient for phale nutritient)[1]0.01g P m <sup>-3</sup> $K_{14AOB}$ Saturation coefficient for phale nutritient)[1]0.01g P m <sup>-3</sup> $K_{14AOB}$ Saturation coefficient for phale nutritient)[1]0.01g P m <sup>-3</sup> $K_{24AOB}$ Saturation coefficient for phale nutritient)[1]0.01g P m <sup>-3</sup> $K_{14A}$ G <sup>-1</sup> <td>Kooh</td> <td>Saturation/inhibition coefficient for oxygen</td> <td>[1]</td> <td>0.2</td> <td><math>g O2 m^{-3}</math></td>	Kooh	Saturation/inhibition coefficient for oxygen	[1]	0.2	$g O2 m^{-3}$
$X_{at}^{in}$ Saturation coefficient for fermentation on $S_A$ [1]4g COD m^{-3} $K_{At}$ Saturation coefficient for growth on acetate $S_A$ [1]4g COD m^{-3} $K_{SCOH}$ Saturation coefficient for ammonium (nutrient)[1]0.05g N m^{-3} $K_{WHH}$ Saturation coefficient for ammonium (nutrient)[1]0.01g N m^{-3} $K_{HL}$ Saturation coefficient for ankalninity (HCO <sub>3</sub> )[1]0.1mole HCO <sup>-3</sup> m^{-3} $K_{AL}$ Saturation coefficient for akalninity (HCO <sub>3</sub> )[1]0.1mole HCO <sup>-3</sup> m^{-3} $M_{Ammonia}$ oxidizers bacteria (nitrifying organisms, autorophic: $X_{AOB}$ Modified0.8d^{-1} $K_{AL}$ Saturation coefficient for axygen[1]0.5g O2 m^{-3} $k_{ALAOB}$ Saturation coefficient for ammonium (nutrient)[1]0.1g N m^{-2} $K_{ALAOB}$ Saturation coefficient for ammonium (nutrient)[1]0.01g P m^{-3} $K_{ALAOB}$ Saturation coefficient for akalaninity (HCO <sup>-3</sup> )[1]0.01g P m^{-3} $K_{ALAOB}$ Saturation coefficient for akalaninity (HCO <sup>-3</sup> )[1]0.01g P m^{-3} $K_{ALAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3} $K_{ALAOB}$ Saturation (notificient for oxygen[1]0.4- $K_{ALAOB}$ Saturation (nihibition coefficient for oxygen[1]0.4- $N_{AOS}$ Saturation coefficient for oxygen[1]0.2g O_2n^{-1} $N_{A$	K <sub>FH</sub>	Saturation coefficient for growth on $S_{\rm F}$	[1]	4	g COD m <sup>-3</sup>
$K_{AH}$ Saturation coefficient for growth on acetate $S_A$ [1]4g COD m <sup>-3</sup> $K_{NOAH}$ Saturation/inhibition coefficient for nitrate[1]0.5g N m <sup>-3</sup> $K_{NHAH}$ Saturation coefficient for annonium (nutrient)[1]0.01g N m <sup>-3</sup> $K_{FH}$ Saturation coefficient for phosphate (nutrient)[1]0.01g N m <sup>-3</sup> $K_{AL}$ Saturation coefficient for adapting in a constraint of the phosphate (nutrient)[1]0.01g N m <sup>-3</sup> $M_{AL}$ Saturation coefficient for adapting in a constraint of the phosphate (nutrient)[1]0.01g N m <sup>-3</sup> $\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ Modified1.4d <sup>-1</sup> $h_{COA}$ Decay rate of $X_{AOB}$ Modified1.4d <sup>-1</sup> $h_{COA}$ Saturation coefficient for annonium (nutrient)[1]0.5g CD m <sup>-3</sup> $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{NALAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.01g P m <sup>-3</sup> $K_{NALAB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.01g P m <sup>-3</sup> $K_{NALAB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.6- $K_{NALAB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.1g N m <sup>-3</sup> $K_{NALAB}$ Saturation coefficient for oxygen[1]0.2g O_2 m <sup>-3</sup> $K_{NALAB}$ Anarotic hydrolysis reduction factor[1]0.4- $K_{NOS}$ <td>K<sub>fe</sub></td> <td>Saturation coefficient for fermentation on <math>S_{A}</math></td> <td>[1]</td> <td>4</td> <td><math>g \text{ COD } m^{-3}</math></td>	K <sub>fe</sub>	Saturation coefficient for fermentation on $S_{A}$	[1]	4	$g \text{ COD } m^{-3}$
XoomSaturation /inhibition coefficient for nitrateII0.5g N m^{-3}KSHHSaturation coefficient for ammonium (nutrient)0.05g N m^{-3}g N m^{-3}KALSaturation coefficient for phosphate (nutrient)0.01g N m^{-3}g N m^{-3}KALSaturation coefficient for alkalinity (HCO <sub>3</sub> )110.01g N m^{-3}Maximum growth rate of XAOBModified1.4d^{-1}BAOBDecay rate of XAOBModified0.06d^{-1}KORAOBSaturation coefficient for annonium (nutrient)110.5g O2 m^{-3}KNHAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )110.5mole HCO <sup>-3</sup> m^{-3}KALAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )110.5mole HCO <sup>-3</sup> m^{-3}KALAOBSaturation coefficient for phosphorus (nutrient)110.5mole HCO <sup>-3</sup> m^{-3}KALAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )110.6-KAAOBSaturation coefficient for crygen110.6-KAAHydrolysis reduction factor110.4-KASSaturation/inhibition coefficient for nitrite and110.5g N m <sup>-3</sup> KNOSAnoxic hydrolysis reduction factor110.4-KozsSaturation/inhibition coefficient for nitrite and110.5g N m <sup>-3</sup> KNOSSaturation/inhibition coefficient for nitrite and110.5g N m <sup>-3</sup> KNOSSaturation coefficient for anxic activityModified <td>K<sub>AH</sub></td> <td>Saturation coefficient for growth on acetate <math>S_{A}</math></td> <td>[1]</td> <td>4</td> <td><math>g \text{ COD } m^{-3}</math></td>	K <sub>AH</sub>	Saturation coefficient for growth on acetate $S_{A}$	[1]	4	$g \text{ COD } m^{-3}$
KNHAHSaturation coefficient for ammonium (nutrient)[1]0.05g N m^{-3} $K_{PH}$ Saturation coefficient for pakhaity (HCO)0.1g N m^{-3} $K_{AL}$ Saturation coefficient for alkalinity (HCO)110.1mole HCO <sup>-3</sup> m^{-3} $A_{AOB}$ Maximum growth rate of $X_{AOB}$ Modified1.4d^{-1} $AOB$ Decay rate of $X_{AOB}$ Modified0.08d^{-1} $B_{OB}$ Saturation coefficient for axmonium (nutrient)110.5g O2 m^{-3} $K_{NHAOB}$ Saturation coefficient for ammonium (nutrient)110.01g P m^{-3} $K_{ALCOB}$ Saturation coefficient for ammonium (nutrient)110.01g P m^{-3} $K_{ALCOB}$ Saturation coefficient for phosphorus (nutrient)110.01g P m^{-3} $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)110.01g P m^{-3} $NCOB$ Saturation coefficient for phosphorus (nutrient)110.01g P m^{-3} $N_{NCOB}$ Anaerobic hydrolysis reduction factor110.4- $K_{NS}$ Saturation /inhibition coefficient for oxygen110.2g Q m^{-3} $K_{NOB}$ Saturation /inhibition coefficient for nitrite and110.5g N m^{-3} $N_{NOB}$ Saturation /inhibition coefficient for nitrite and110.5g N m^{-3} $K_{NOB}$ Saturation /inhibition coefficient for nitrite and110.5g N m^{-3} $N_{NOB}$ Saturation /inhibition coefficient for nitrite and11 <td< td=""><td>KNO3H</td><td>Saturation/inhibition coefficient for nitrate</td><td>[1]</td><td>0.5</td><td><math>g N m^{-3}</math></td></td<>	KNO3H	Saturation/inhibition coefficient for nitrate	[1]	0.5	$g N m^{-3}$
XintSaturation coefficient for phosphate (nutrient)[1]0.01g N m^{-3}KALSaturation coefficient for alkalinity (HCOs)[1]0.1mole HCO^{-3} m^{-3}MARDMaximum growth rate of XAOBModified1.4d^{-1}bAOBDecay rate of XAOBModified0.08d^{-1}KQ2AOBSaturation coefficient for ammonium (nutrient)110.5g O2 m^{-3}KNHAOBSaturation coefficient for ammonium (nutrient)110.01g P m^{-3}KALKAOBSaturation coefficient for alkalinity (HCO <sup>-1</sup> )110.01g P m^{-3}KALKAOBSaturation coefficient for phosphorus (nutrient)110.01g P m^{-3}KhHydrolysis rate constant113d^{-1}Hydrolysis rate constant110.6-NOSSAnoxic hydrolysis reduction factor110.4-NOSSSaturation/inhibition coefficient for nyargen110.5g N m^{-3}KNGSSaturation/inhibition coefficient for oxygen110.1g X <sub>5</sub> g <sup>-1</sup> X <sub>H</sub> Phosphorus-accumulatingorganisms: X <sub>PAO</sub> 110.5g X <sub>THA</sub> g <sup>-1</sup> X <sub>PAO</sub> qIPARate constant for storage of X <sub>PHA</sub> (base X <sub>PP</sub> )Modified3.3g X <sub>PHA</sub> g <sup>-1</sup> X <sub>PAO</sub> qIPARate constant for storage of X <sub>PP</sub> 111.5g X <sub>PHA</sub> g <sup>-1</sup> X <sub>PAO</sub> qIPARate constant for storage of X <sub>PP</sub> 110.2d^{-1}qIPARate constant for storage of X <sub>PP</sub> 110.2d^{-1}qIPA	K <sub>NH4H</sub>	Saturation coefficient for ammonium (nutrient)	[1]	0.05	$g N m^{-3}$
SALSaturation coefficient for alkalinity (HCO3)[1]0.1mole HCO <sup>-3</sup> m <sup>-3</sup> Ammonia oxidizers bacteria (nitrifying organisms, autotrophic) $X_{AOB}$ Modified1.4d <sup>-1</sup> $\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ Modified0.08d <sup>-1</sup> $\mu_{AOB}$ Saturation/inhibitio coefficient for oxygen[1]0.5gO 2m <sup>-3</sup> $K_{Q2AOB}$ Saturation coefficient for alkalinity (HCO-3)[1]0.5gO 2m <sup>-3</sup> $K_{ALXAOB}$ Saturation coefficient for alkalinity (HCO-3)[1]0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{PAOB}$ Saturation coefficient for alkalinity (HCO-3)[1]0.01g P m <sup>-3</sup> $K_{PAOB}$ Saturation coefficient for physiphorus (nutrient)[1]0.1g P m <sup>-3</sup> $K_{PAOB}$ Saturation coefficient for alkalinity (HCO-3)[1]0.01g P m <sup>-3</sup> $K_{PAOB}$ Saturation coefficient for physiphorus (nutrient)[1]0.1g P m <sup>-3</sup> $R_{PAOB}$ Anoxic hydrolysis reduction factor[1]0.6- $R_{KS}$ Saturation/inhibition coefficient for oxygen[1]0.5g N m <sup>-3</sup> $K_{NOSS}$ Saturation/inhibition coefficient for oxygen[1]0.1g X s g <sup>-1</sup> X HPhosphorus-accumulating organisms: X <sub>PAO</sub> G <sup>-1</sup> 10.1g X s g <sup>-1</sup> X A d $q_{PHA}$ Rate constant for storage of X <sub>PP</sub> [1]1.5g X <sub>PHA</sub> g <sup>-1</sup> X <sub>PAO</sub> $q_{PHA}$ Rate constant for storage of X <sub>PP</sub> [1]0.2d <sup>-1</sup> $q_{PPA}$ Rate constant for storage of X <sub>PP</sub> <td>Крн</td> <td>Saturation coefficient for phosphate (nutrient)</td> <td>[1]</td> <td>0.01</td> <td><math>g N m^{-3}</math></td>	Крн	Saturation coefficient for phosphate (nutrient)	[1]	0.01	$g N m^{-3}$
Ammonia oxidizers bacteria (nitrifying organisms, autotrophic): $X_{AOB}$ Motified1.4d^{-1} $\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ Modified0.08d^{-1} $\mu_{AOB}$ Decay rate of $X_{AOB}$ Modified0.08d^{-1} $\mu_{AOB}$ Saturation /inhibition coefficient for oxygen[1]0.5g C m^{-3} $K_{CLAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5mole HCO <sup>-3</sup> m^{-3} $K_{ALEAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3} $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3} $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3} $K_{PAOB}$ Anoxic hydrolysis reduction factor[1]0.6- $\eta_{NOSS}$ Anoxic hydrolysis reduction factor[1]0.4- $K_{CSS}$ Saturation/inhibition coefficient for nitrite and[1]0.5g N m^{-3} $K_{NOSS}$ Saturation coefficient for particulate COD[1]0.1g X_s g^{-1} X_HPhosphorus-accumulating organisms: X <sub>PAO</sub> Maximum growth rate of PAOModified3.3g X_{PHA} g^{-1} X_{PAO} $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g X_{PHA} g^{-1} X_{PAO} $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]0.2d^{-1} $\eta_{PO}$ Maximum growth rate of PAOModified0.8- $\eta_{PD}$ Rate for lysis of $X_{PAO}$ [1	KAI	Saturation coefficient for alkalinity ( $HCO_3$ )	[1]	0.1	mole $HCO^{-3}$ m <sup>-3</sup>
organisms, autotrophic): $X_{AOB}$ $\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ Modified 1.4 d <sup>-1</sup> $K_{OZAOB}$ Saturation/inhibition coefficient for axygen [1] 0.5 g O2 m <sup>-3</sup> $K_{NIAAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) [1] 0.5 mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALKAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) [1] 0.5 mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{ALCAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) [1] 0.01 g P m <sup>-3</sup> $K_{ALCAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) [1] 0.6 - $\eta_{Ie}$ Anaerobic hydrolysis reduction factor [1] 0.6 - $\eta_{Ie}$ Anaerobic hydrolysis reduction factor [1] 0.4 - $K_{COS}$ Saturation/inhibition coefficient for anitrate for anitrate $K_S$ $K_{NO3S}$ Saturation coefficient for particulate COD [1] 0.1 g X <sub>5</sub> g <sup>-1</sup> X <sub>H</sub> Phosphorus-accumulating organisms: X <sub>PAO</sub> [1] 0.5 g N m <sup>-3</sup> nitrate $K_{XS}$ Saturation coefficient for storage of $X_{PHA}$ (base $X_{PP}$ ) Modified 3.3 g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> d <sup>-1</sup> $\eta_{VOSPAO}$ Reduction factor for anoxic activity Modified 0.8 - $\mu_{PAO}$ Maximum growth rate of PAO Modified 1.2 d <sup>-1</sup> $\eta_{VOSPAO}$ Reduction factor for anoxic activity Modified 0.8 - $\mu_{PAO}$ Maximum growth rate of PAO [1] 0.2 d <sup>-1</sup> $\eta_{VOSPAO}$ Reduction factor for anoxic activity Modified 0.8 - $\mu_{PAO}$ Maximum growth rate of PAO [1] 0.2 d <sup>-1</sup> $\eta_{VOSPAO}$ Saturation coefficient for oxygen [1] 0.2 d <sup>-1</sup> $\eta_{VOSPAO}$ Reduction factor for anoxic activity Modified 0.8 - $\mu_{PAO}$ Maximum growth rate of PAO [1] 0.2 d <sup>-1</sup> $\eta_{VOSPAO}$ Saturation coefficient for axycen [1] 0.2 d <sup>-1</sup> $\eta_{VOSPAO}$ Saturation coefficient for axycen [1] 0.2 g $\Omega_{2}$ m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for axycen [1] 0.2 g $\Omega_{2}$ m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for axycen [1] 0.2 g $\Omega_{2}$ m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for axycen [1] 0.2 g $\Omega_{2}$ m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for axycen [1] 0.2 g $P$ m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for amonium (nutrient) $K_{APAO}$ Saturation coefficient for amonium (nutrient)		Ammonia oxidizers bacteria (nitrifying			
$\mu_{AOB}$ Maximum growth rate of $X_{AOB}$ Modified1.4 $d^{-1}$ $h_{AOB}$ Decay rate of $X_{AOB}$ Modified0.08 $d^{-1}$ $K_{O2AOB}$ Saturation coefficient for anyonium (nutrient)110.5g O2 m^{-3} $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )110.5mol HCO <sup>-3</sup> m^{-3} $K_{ALKAOB}$ Saturation coefficient for phosphorus (nutrient)110.01g P m^{-3} $K_{ALKAOB}$ Saturation coefficient for phosphorus (nutrient)110.01g P m^{-3} $K_{AOB}$ Saturation coefficient for phosphorus (nutrient)110.6 $ R_{NOSS}$ Anoxic hydrolysis reduction factor110.6 $ N_{NOSS}$ Anoxic hydrolysis reduction factor110.4 $ K_{NOSS}$ Saturation/inhibition coefficient for oxygen110.2g O2 m^{-3} $R_{NOSS}$ Saturation coefficient for particulate COD110.1g Xs g^{-1} XHPhosphorus-accumulating organisms: XPAO $q^{-1}$ $R_{AE}$ constant for storage of $X_{PP}$ 111.5g XPHA g^{-1} XPAO $q_{PHA}$ Rate constant for storage of $X_{PP}$ 111.5g XPHA g^{-1} XPAO $q_{PTA}$ Rate constant for storage of $X_{PP}$ 110.2 $d^{-1}$ $P_{PO}$ Maximum growth rate of PAOModified8 $ P_{PO}$ Rate for lysis of $X_{PAO}$ 110.2 $d^{-1}$ $P_{PO}$ Rate for lysis of $X_{PAO}$ 110.2 $d^{-1}$ </td <td></td> <td>organisms, autotrophic): <math>X_{AOB}</math></td> <td></td> <td></td> <td></td>		organisms, autotrophic): $X_{AOB}$			
DecayDecay rate of $X_{AOB}$ Modified0.08 $d^{-1}$ $K_{02AOB}$ Saturation /inhibition coefficient for oxygen[1]0.5g O2 m^{-3} $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5mole HCO <sup>-3</sup> m^{-3} $K_{ALKAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.01g P m^{-3} $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3} $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.6 $ Hydrolysis of particulate substrate: X_SX_SA noxic hydrolysis reduction factor[1]0.6 \eta_{Re}Anaerobic hydrolysis reduction factor[1]0.6  \eta_{Re}Anaerobic hydrolysis reduction factor[1]0.5g O2 m^{-3}K_{O2S}Saturation/inhibition coefficient for oxygen[1]0.5g N m^{-3}K_{NOS}Saturation coefficient for particulate COD[1]0.1g XS g-1 XHPhosphorus-accumulatingorganisms: X_{PAO}ARate constant for storage of X_{PP}[1]1.5g X_{PHA} g^{-1} X_{PAO}d^{PHA}Rate constant for storage of X_{PP}[1]0.2d^{-1}\mu_{PAO}Maximum growth rate of PAOModified0.8-\mu_{PAO}Rate for lysis of X_{PP}[1]0.2d^{-1}\mu_{PAO}Rate for lysis of X_{PPO}[1]0.2d^{-1}\mu_{PAO}Rate for lysis$	$\mu_{AOB}$	Maximum growth rate of $X_{AOB}$	Modified	1.4	$d^{-1}$
$K_{0200B}$ Saturation/inhibition coefficient for oxygen[1]0.5g 02 m^{-3} $K_{NHAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]1g N m^{-3} $K_{ALKAOB}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5mole HCO <sup>-3</sup> m^{-3} $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3} $Hydrolysis$ of particulate substrate: $X_S$ III0.6- $K_N$ Hydrolysis reduction factor[1]0.6- $\eta_{NOSS}$ Anoarobic hydrolysis reduction factor[1]0.4- $K_{O2S}$ Saturation/inhibition coefficient for oxygen[1]0.2g O_2 m^{-3} $K_{NOSS}$ Saturation/inhibition coefficient for oxygen[1]0.5g N m^{-3} $K_{NOSS}$ Saturation/inhibition coefficient for nitrite and[1]0.5g N m^{-3} $K_{NOSS}$ Saturation coefficient for particulate COD[1]0.1g X <sub>5</sub> g - <sup>1</sup> X <sub>H</sub> Phosphorus-accumulating organisms: X <sub>PAO</sub> $M_{11}$ $R_{4}$ constant for storage of $X_{PF}$ [1]1.5g X <sub>PHA</sub> g - <sup>1</sup> X <sub>PAO</sub> $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g X <sub>PHA</sub> g - <sup>1</sup> X <sub>PAO</sub> $d_{NOSPAO}$ Reduction factor for anoxic activityModified1.2d - <sup>1</sup> $M_{NOSPAO}$ Rate for lysis of X <sub>PAO</sub> [1]0.2d - <sup>1</sup> $h_{PAO}$ Rate for lysis of X <sub>PAO</sub> [1]0.2g O_2 m - <sup>3</sup> $h_{NOSPAO}$ Saturation coefficient for nitrate, $S_{N$	b <sub>AOB</sub>	Decay rate of $X_{AOB}$	Modified	0.08	$d^{-1}$
K_NHAOB K_NHAOBSaturation coefficient for ammonium (nutrient)[1]1g N m^{-3}K_ALKAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5mole HCO <sup>-3</sup> m <sup>-3</sup> K_PAOBSaturation coefficient for phosphorus (nutrient)[1]0.01g P m <sup>-3</sup> K_hHydrolysis of particulate substrate: X <sub>5</sub> KK_hHydrolysis reduction factor[1]0.6- $\eta_{NOSS}$ Anoxic hydrolysis reduction factor[1]0.4- $\eta_{Re}$ Anaerobic hydrolysis reduction factor[1]0.4-Ko2SSaturation /inhibition coefficient for oxygen[1]0.5g N m <sup>-3</sup> KNO3SSaturation /inhibition coefficient for nitrite and[1]0.5g N m <sup>-3</sup> KNO3SSaturation coefficient for particulate COD[1]0.1g X <sub>5</sub> g <sup>-1</sup> X <sub>H</sub> Phosphorus-accumulating organisms: X <sub>PAO</sub> $q_{PHA}$ Rate constant for storage of X <sub>PHA</sub> (base X <sub>PP</sub> )Modified3.3g X <sub>PHA</sub> g <sup>-1</sup> X <sub>PAO</sub> qPPRate constant for storage of X <sub>PP</sub> [1]1.5g X <sub>PHA</sub> g <sup>-1</sup> X <sub>PAO</sub> $d^{-1}$ $\eta_{NOSPAO}$ Maximum growth rate of PAOModified1.2d <sup>-1</sup> $\eta_{NOSPAO}$ Reduction factor for anoxic activityModified0.8- $p_{PAO}$ Rate for lysis of X <sub>PAO</sub> [1]0.2d <sup>-1</sup> $\eta_{NOSPAO}$ Rate for lysis of X <sub>PP</sub> [1]0.2d <sup>-1</sup> $h_{FAO}$ Saturation coefficient for oxygen[1]0.2g <sup>-1</sup> $h_{FAO}$ Saturation co	K <sub>O2AOB</sub>	Saturation/inhibition coefficient for oxygen	[1]	0.5	$g O2 m^{-3}$
XALKAOB KALKAOBSaturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.5mole HCO <sup>-3</sup> m <sup>-3</sup> $K_{PAOB}$ Saturation coefficient for phosphorus (nutrient)[1]0.01g P m <sup>-3</sup> $K_{PAOB}$ Hydrolysis of particulate substrate: $X_S$ $X_S$ $K_h$ Hydrolysis rate constant[1]0.6 $ \eta_{NOSS}$ Anoxic hydrolysis reduction factor[1]0.6 $ \eta_e$ Anaerobic hydrolysis reduction factor[1]0.4 $ K_{O2S}$ Saturation/inhibition coefficient for nitrite and nitrate[1]0.5g N m <sup>-3</sup> $K_{NO3S}$ Saturation/inhibition coefficient for nitrite and nitrate[1]0.1g X_S g <sup>-1</sup> X_HPhosphorus-accumulating organisms: $X_{PAO}$ Fate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified3.3g $X_{PHA} g^{-1} X_{PAO}$ d <sup>-1</sup> $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA} g^{-1} X_{PAO}$ d <sup>-1</sup> $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA} g^{-1} X_{PAO}$ d <sup>-1</sup> $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA} g^{-1} X_{PAO}$ d <sup>-1</sup> $q_{PAO}$ Maximum growth rate of PAOModified1.2d <sup>-1</sup> $q_{PAO}$ Reduction factor for anoxic activityModified0.8- $q_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2g $O_2$ m <sup>-3</sup> $k_{NOSPAO}$ Saturation coefficient for origen for oxygen[1]0.2g $O_2$ m <sup>-3</sup> <tr< td=""><td>K<sub>NH4AOB</sub></td><td>Saturation coefficient for ammonium (nutrient)</td><td>[1]</td><td>1</td><td><math>g N m^{-3}</math></td></tr<>	K <sub>NH4AOB</sub>	Saturation coefficient for ammonium (nutrient)	[1]	1	$g N m^{-3}$
KrAOBSaturation coefficient for phosphorus (nutrient)[1]0.01g P m^{-3}Hydrolysis of particulate substrate: $X_5$ Hydrolysis of particulate substrate: $X_5$ II3d^{-1}NNOBSAnoxic hydrolysis reduction factor[1]0.6- $\eta_{le}$ Anaerobic hydrolysis reduction factor[1]0.4- $K_{O2S}$ Saturation/inhibition coefficient for oxygen[1]0.2g O <sub>2</sub> m^{-3} $K_{NOBS}$ Saturation /inhibition coefficient for nitrite and[1]0.5g N m^{-3}nitratenitrateII0.1g X <sub>S</sub> g^{-1} X <sub>H</sub> Phosphorus-accumulating organisms: X <sub>PAO</sub> Rate constant for storage of X <sub>PHA</sub> (base X <sub>PP</sub> )Modified3.3g X <sub>PHA</sub> g^{-1} X <sub>PAO</sub> qPHARate constant for storage of X <sub>PP</sub> [1]1.5g X <sub>PHA</sub> g^{-1} X <sub>PAO</sub> qPAOMaximum growth rate of PAOModified0.8- $\eta_{NOSPAO}$ Reduction factor for anoxic activityModified0.8- $h_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2g O <sub>1</sub> $h_{PAO}$ Rate for lysis of $X_{PP}$ [1]0.2g O <sub>2</sub> m^{-3} $K_{OSPAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.2g O <sub>2</sub> m^{-3} $K_{PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.2g O <sub>1</sub> $h_{PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.2g O <sub>2</sub> m^{-3} $K_{NOSPAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.5g N m^{-3} <td>KALKAOB</td> <td>Saturation coefficient for alkalinity <math>(HCO^{-3})</math></td> <td>[1]</td> <td>0.5</td> <td>mole HCO<sup>-3</sup> m<sup>-3</sup></td>	KALKAOB	Saturation coefficient for alkalinity $(HCO^{-3})$	[1]	0.5	mole HCO <sup>-3</sup> m <sup>-3</sup>
Hydrolysis of particulate substrate: $X_S$ O $K_h$ Hydrolysis of particulate substrate: $X_S$ O $X_{NO35}$ Anoxic hydrolysis reduction factor[1]3d^{-1} $\eta_{NO35}$ Anoxic hydrolysis reduction factor[1]0.6- $\eta_{te}$ Anaerobic hydrolysis reduction factor[1]0.4- $X_{O25}$ Saturation/inhibition coefficient for oxygen[1]0.2g O_2 m^{-3} $K_{NO35}$ Saturation/inhibition coefficient for nitrite and nitrate[1]0.1g X_S g^{-1} X_HPhosphorus-accumulating organisms: $X_{PAO}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified3.3g $X_{PHA}$ g^{-1} $X_{PAO}$ d^{-1} $q_{PHA}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g^{-1} $X_{PAO}$ d^{-1} $q_{PAO}$ Maximum growth rate of PAOModified0.8- $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $p_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d^{-1} $p_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d^{-1} $p_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2g O_2 m^{-3} $p_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2g O_2 $p_{PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.2g O_2 $p_{PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.2g O_2 $p_{PAO}$ Saturation coef	KPAOB	Saturation coefficient for phosphorus (nutrient)	[1]	0.01	$g P m^{-3}$
$K_h$ Hydrolysis rate constant[1]3 $d^{-1}$ $\eta_{NOOS}$ Anoxic hydrolysis reduction factor[1]0.6- $\eta_{le}$ Anaerobic hydrolysis reduction factor[1]0.4- $K_{O2S}$ Saturation/inhibition coefficient for oxygen[1]0.2 $g O_2 m^{-3}$ $K_{NOOS}$ Saturation/inhibition coefficient for nitrite and[1]0.5 $g N m^{-3}$ $nitrate$ saturation/inhibition coefficient for nitrite and[1]0.1 $g X_5 g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified3.3 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PPA}$ Rate constant for storage of $X_{PP}$ [1]1.5 $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $\eta_{NOSPAO}$ Reduction factor for anoxic activityModified0.8- $p_{PAO}$ Maximum growth rate of PAOModified0.8- $p_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2 $d^{-1}$ $h_{NOSPAO}$ Rate for lysis of $X_{PAO}$ [1]0.2 $d^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2 $d^{-1}$ $b_{PAO}$ Saturation coefficient for intrate, $S_{NO}$ [1]0.2 $d^{-1}$ $h_{NOSPAO}$ Saturation coefficient for oxygen[1]0.2 $d^{-1}$ $b_{PAO}$ Saturation coefficient for intrate, $S_{NO}$ [1]0.2 $g^{-1}$ $k_{PAO}$ Saturation coefficient for acteate $S_A$ [1]		Hydrolysis of particulate substrate: $X_{\rm S}$			0
$n_{NO35}$ Anoxic hydrolysis reduction factor[1] $0.6$ $ \eta_{le}$ Anaerobic hydrolysis reduction factor[1] $0.4$ $ K_{O25}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{NO35}$ Saturation/inhibition coefficient for nitrite and nitrate[1] $0.5$ $g N m^{-3}$ $K_{NO35}$ Saturation coefficient for particulate COD[1] $0.1$ $g X_5 g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified $3.3$ $g X_{PHA} g^{-1} X_{PAO}$ $d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ [1] $1.5$ $g X_{PHA} g^{-1} X_{PAO}$ $d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAOModified $0.8$ $ \mu_{PAO}$ Reduction factor for anoxic activityModified $0.8$ $ b_{PAO}$ Rate for lysis of $X_{PPO}$ [1] $0.2$ $d^{-1}$ $b_{PAO}$ Saturation coefficient for oxygen[1] $0.2$ $d^{-1}$ $k_{NO3PAO}$ Saturation inhibition coefficient for oxygen[1] $0.2$ $d^{-1}$ $k_{PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1] $0.2$ $g CD m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for actexte $S_A$ [1] $4$ $g COD m^{-3}$ $K_{APAO}$ Saturation coefficient for phosphorus in storage[1] $0.2$ $g P m^{-3}$ $K_{PAO}$ Saturation coefficient for phosphorus in storage[1] <td>K<sub>b</sub></td> <td>Hydrolysis rate constant</td> <td>[1]</td> <td>3</td> <td><math>d^{-1}</math></td>	K <sub>b</sub>	Hydrolysis rate constant	[1]	3	$d^{-1}$
Incom IpeAnaerobic hydrolysis reduction factor[1] $0.4$ $ K_{O2S}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{NO3S}$ Saturation/inhibition coefficient for nitrite and nitrate[1] $0.5$ $g N m^{-3}$ $K_{NS}$ Saturation coefficient for particulate COD[1] $0.1$ $g X_5 g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ $q_{PHA}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified $3.3$ $g X_{PHA} g^{-1} X_{PAO}$ $d^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ [1] $1.5$ $g X_{PHA} g^{-1} X_{PAO}$ $d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAOModified $1.2$ $d^{-1}$ $\mu_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $\mu_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $h_{PAO}$ Saturation factor for anoxic activityModified $0.8$ $ b_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g C m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1] $0.2$ $g C m^{-3}$ $K_{PAO}$ Saturation coefficient for acteate $S_A$ [1] $4$ $g COD m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for phosphorus in storage[1] $0.2$ $g P m^{$	n	Anoxic hydrolysis reduction factor	[1]	0.6	_
NormSaturation/inhibition coefficient for oxygen[1]0.2 $g O_2 m^{-3}$ $K_{NO35}$ Saturation/inhibition coefficient for nitrite and nitrate[1]0.5 $g N m^{-3}$ $K_{XS}$ Saturation coefficient for particulate COD[1]0.1 $g X_S g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ [1]0.1 $g X_{S} g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified $3.3$ $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PHA}$ Rate constant for storage of $X_{PP}$ [1] $1.5$ $g X_{PHA} g^{-1} X_{PAO} d^{-1}$ $q_{PAO}$ Maximum growth rate of PAOModified $1.2$ $d^{-1}$ $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified $0.8$ - $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $k_{O3PAO}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for actate $S_A$ [1] $0.5$ $g N m^{-3}$ $K_{NAPAO}$ Saturation coefficient for amonium (nutrient)[1] $0.05$ $g N m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for phosphate (nutrient)[1] $0.2$ $g COD m^{-3}$ $K_{PFAO}$ Saturation coefficient for phosphate (nutrient)[1] $0.2$ $g P m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for phosphate (nutrient)[1] <td><math>n_{f_{\Theta}}</math></td> <td>Anaerobic hydrolysis reduction factor</td> <td>[1]</td> <td>0.4</td> <td>_</td>	$n_{f_{\Theta}}$	Anaerobic hydrolysis reduction factor	[1]	0.4	_
KNO35Saturation/inhibition coefficient for nitrite and nitrate[1]0.5g N m^{-3} $K_{\rm NO35}$ Saturation coefficient for particulate COD[1]0.1g X_{\rm s} g^{-1} X_{\rm H}Phosphorus-accumulating organisms: X <sub>PAO</sub> Rate constant for storage of X <sub>PHA</sub> (base X <sub>PP</sub> )Modified3.3g X <sub>PHA</sub> g^{-1} X <sub>PAO</sub> $q_{\rm PHA}$ Rate constant for storage of X <sub>PP</sub> [1]1.5g X <sub>PHA</sub> g^{-1} X <sub>PAO</sub> $q_{\rm PP}$ Rate constant for storage of X <sub>PP</sub> [1]1.5g X <sub>PHA</sub> g^{-1} X <sub>PAO</sub> $d^{-1}$ $d^{-1}$ $d^{-1}$ $d^{-1}$ $d^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAOModified1.2 $d^{-1}$ $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8 $ b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2 $d^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2 $d^{-1}$ $k_{O3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.5g N m^{-3} $K_{NO3PAO}$ Saturation coefficient for acetate $S_A$ [1]4g COD m^{-3} $k_{NO3PAO}$ Saturation coefficient for amonium (nutrient)[1]0.01g P m^{-3} $k_{NO3PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m^{-3} $k_{NO3PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m^{-3} $k_{NO3PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m^{-3} $k_{PAO}$	Kors	Saturation/inhibition coefficient for oxygen	[1]	0.2	$g O_2 m^{-3}$
nitratenitrate0 $K_{XS}$ Saturation coefficient for particulate COD[1]0.1g $X_S g^{-1} X_H$ Phosphorus-accumulating organisms: $X_{PAO}$ </td <td>KNO3S</td> <td>Saturation/inhibition coefficient for nitrite and</td> <td>[1]</td> <td>0.5</td> <td><math>g N m^{-3}</math></td>	KNO3S	Saturation/inhibition coefficient for nitrite and	[1]	0.5	$g N m^{-3}$
$K_{XS}$ Saturation coefficient for particulate COD[1]0.1g X_S g^{-1} X_HPhosphorus-accumulating organisms: $X_{PAO}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified3.3g $X_{PHA}$ g^{-1} $X_{PAO}$ d^{-1} $q_{PHA}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g^{-1} $X_{PAO}$ d^{-1} $\mu_{PAO}$ Maximum growth rate of PAOModified1.2d^{-1} $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d^{-1} $b_{PP}$ Rate for lysis of $X_{PP}$ [1]0.2d^{-1} $b_{PHA}$ Rate for lysis of $X_{PHA}$ [1]0.2d^{-1} $k_{O2PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2g O2 m^{-3} $K_{NO3PAO}$ Saturation coefficient for acteate $S_A$ [1]4g COD m^{-3} $K_{PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m^{-3} $K_{PFAO}$ Saturation coefficient for phosphorus in storage[1]0.01g P m^{-3} $K_{PFAO}$ Saturation coefficient for phosphate (nutrient)[1]0.1g P m^{-3} $K_{PFAO}$ Saturation coefficient for alkalinity (HCO^{-3})[1]0.1mole HCO^{-3} m^{-3}	NOOD	nitrate			0
Phosphorus-accumulating organisms: $X_{PAO}$ Rate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified3.3g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> $\mu_{PAO}$ Maximum growth rate of PAOModified1.2d <sup>-1</sup> $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d <sup>-1</sup> $b_{PP}$ Rate for lysis of $X_{PP}$ [1]0.2d <sup>-1</sup> $b_{PHA}$ Rate for lysis of $X_{PHA}$ [1]0.2d <sup>-1</sup> $K_{O2PAO}$ Saturation coefficient for oxygen[1]0.2gO <sub>2</sub> m <sup>-3</sup> $K_{NAPAO}$ Saturation coefficient for acteate $S_A$ [1]4g COD m <sup>-3</sup> $K_{NH4PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m <sup>-3</sup> $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01g P m <sup>-3</sup> $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01g P m <sup>-3</sup>	K <sub>XS</sub>	Saturation coefficient for particulate COD	[1]	0.1	g $X_{\rm S}$ g <sup>-1</sup> $X_{\rm H}$
Organisms. XPAORate constant for storage of $X_{PHA}$ (base $X_{PP}$ )Modified3.3g $X_{PHA}$ g $^{-1}$ $X_{PAO}$ d $^{-1}$ $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g $^{-1}$ $X_{PAO}$ d $^{-1}$ $\mu_{PAO}$ Maximum growth rate of PAOModified1.2d $^{-1}$ $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d $^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d $^{-1}$ $b_{PAO}$ Rate for lysis of $X_{PP}$ [1]0.2d $^{-1}$ $b_{PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2g $O_2$ m $^{-3}$ $K_{O2PAO}$ Saturation coefficient for acetate $S_A$ [1]4g COD m $^{-3}$ $K_{NO3PAO}$ Saturation coefficient for ammonium (nutrient)[1]0.05g N m $^{-3}$ $K_{NH4PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m $^{-3}$ $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01g P m $^{-3}$ $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.1mole HCO $^{-3}$ m $^{-3}$	Phosphorus-accumulating				
Image: definition of storage of XpHA (base Xpp)Modulied5.5g ApHA gApAO $q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ $\mu_{PAO}$ Maximum growth rate of PAOModified1.2d <sup>-1</sup> $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d <sup>-1</sup> $b_{PAO}$ Rate for lysis of $X_{PP}$ [1]0.2d <sup>-1</sup> $b_{PP}$ Rate for lysis of $X_{PP}$ [1]0.2d <sup>-1</sup> $b_{PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2g O_2 m^{-3} $K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.5g N m^{-3} $K_{NO3PAO}$ Saturation coefficient for acetate $S_A$ [1]4g COD m^{-3} $K_{NH4PAO}$ Saturation coefficient for phosphorus in storage[1]0.2g P m^{-3} $K_{PFAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01g P m^{-3} $K_{PFAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.1mole HCO <sup>-3</sup> m^{-3}		Pate constant for storage of $Y_{\text{cons}}$ (base $Y_{\text{cons}}$ )	Modified	33	$\alpha X = \alpha^{-1} X$
$q_{PP}$ Rate constant for storage of $X_{PP}$ [1]1.5g $X_{PHA}$ g <sup>-1</sup> $X_{PAO}$ d <sup>-1</sup> $\mu_{PAO}$ Maximum growth rate of PAOModified1.2d <sup>-1</sup> $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2d <sup>-1</sup> $b_{PP}$ Rate for lysis of $X_{PP}$ [1]0.2d <sup>-1</sup> $b_{PHA}$ Rate for lysis of $X_{PPAO}$ [1]0.2d <sup>-1</sup> $b_{PHA}$ Rate for lysis of $X_{PHA}$ [1]0.2d <sup>-1</sup> $k_{O2PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2g $O_2$ m <sup>-3</sup> $K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1]0.5g N m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for acetate $S_A$ [1]4g COD m <sup>-3</sup> $K_{PFAO}$ Saturation coefficient for phosphorus in storage of PP0.1g P m <sup>-3</sup> $K_{ALKPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01g P m <sup>-3</sup>	ЧРНА	Kate constant for storage of ApHA (base App)	Moumeu	5.5	$d^{-1}$
$\mu_{PAO}$ Maximum growth rate of PAOModified1.2 $d^{-1}$ $\eta_{NO3PAO}$ Reduction factor for anoxic activityModified0.8- $b_{PAO}$ Rate for lysis of $X_{PAO}$ [1]0.2 $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PP}$ [1]0.2 $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ [1]0.2 $d^{-1}$ $b_{CO2PAO}$ Saturation/inhibition coefficient for oxygen[1]0.2 $g O_2 m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for acetate $S_A$ [1]0.5 $g N m^{-3}$ $K_{NPAO}$ Saturation coefficient for acetate $S_A$ [1]4 $g COD m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP[1]0.01 $g P m^{-3}$ $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.1mole HCO <sup>-3</sup> m <sup>-3</sup>	<i>q</i> <sub>PP</sub>	Rate constant for storage of $X_{PP}$	[1]	1.5	$g X_{PHA} g^{-1} X_{PAO}$ $d^{-1}$
$\eta_{\text{NO3PAO}}$ Reduction factor for anoxic activityModified $0.8$ $ b_{\text{PAO}}$ Rate for lysis of $X_{\text{PAO}}$ [1] $0.2$ $d^{-1}$ $b_{\text{PP}}$ Rate for lysis of $X_{\text{PP}}$ [1] $0.2$ $d^{-1}$ $b_{\text{PHA}}$ Rate for lysis of $X_{\text{PHA}}$ [1] $0.2$ $d^{-1}$ $k_{\text{O2PAO}}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{\text{NO3PAO}}$ Saturation coefficient for nitrate, $S_{\text{NO}}$ [1] $0.5$ $g N m^{-3}$ $K_{\text{NO3PAO}}$ Saturation coefficient for acetate $S_A$ [1] $4$ $g \text{ COD } m^{-3}$ $K_{\text{NH4PAO}}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ $g N m^{-3}$ $K_{\text{PS}}$ Saturation coefficient for phosphorus in storage of PP[1] $0.2$ $g P m^{-3}$ $K_{\text{ALKPAO}}$ Saturation coefficient for phosphate (nutrient)[1] $0.01$ $g P m^{-3}$ $K_{\text{ALKPAO}}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m^{-3}	$\mu_{\rm PAO}$	Maximum growth rate of PAO	Modified	1.2	$d^{-1}$
$b_{PAO}$ Rate for lysis of $X_{PAO}$ [1] $0.2$ $d^{-1}$ $b_{PP}$ Rate for lysis of $X_{PP}$ [1] $0.2$ $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ [1] $0.2$ $d^{-1}$ $k_{O2PAO}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1] $0.5$ $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ [1] $4$ $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP[1] $0.01$ $g P m^{-3}$ $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m <sup>-3</sup>	$\eta_{\rm NO3PAO}$	Reduction factor for anoxic activity	Modified	0.8	-
$b_{PP}$ Rate for lysis of $X_{PP}$ [1] $0.2$ $d^{-1}$ $b_{PHA}$ Rate for lysis of $X_{PHA}$ [1] $0.2$ $d^{-1}$ $K_{O2PAO}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1] $0.5$ $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ [1] $4$ $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage of PP[1] $0.2$ $g P m^{-3}$ $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.01$ $g P m^{-3}$	b <sub>PAO</sub>	Rate for lysis of X <sub>PAO</sub>	[1]	0.2	$d^{-1}$
$b_{\text{PHA}}$ Rate for lysis of $X_{\text{PHA}}$ [1] $0.2$ $d^{-1}$ $K_{\text{O2PAO}}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{\text{NO3PAO}}$ Saturation coefficient for nitrate, $S_{\text{NO}}$ [1] $0.5$ $g N m^{-3}$ $K_{\text{APAO}}$ Saturation coefficient for acetate $S_A$ [1] $4$ $g \text{ COD } m^{-3}$ $K_{\text{NH4PAO}}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ $g N m^{-3}$ $K_{\text{PS}}$ Saturation coefficient for phosphorus in storage[1] $0.2$ $g P m^{-3}$ $K_{\text{PPAO}}$ Saturation coefficient for phosphate (nutrient)[1] $0.01$ $g P m^{-3}$ $K_{\text{ALKPAO}}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m <sup>-3</sup>	$b_{\mathrm{PP}}$	Rate for lysis of $X_{\rm PP}$	[1]	0.2	$d^{-1}$
$K_{O2PAO}$ Saturation/inhibition coefficient for oxygen[1] $0.2$ $g O_2 m^{-3}$ $K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1] $0.5$ $g N m^{-3}$ $K_{APAO}$ Saturation coefficient for acetate $S_A$ [1]4 $g COD m^{-3}$ $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ $g N m^{-3}$ $K_{PS}$ Saturation coefficient for phosphorus in storage[1] $0.2$ $g P m^{-3}$ $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1] $0.01$ $g P m^{-3}$ $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m <sup>-3</sup>	$b_{\mathrm{PHA}}$	Rate for lysis of $X_{PHA}$	[1]	0.2	$d^{-1}$
$K_{NO3PAO}$ Saturation coefficient for nitrate, $S_{NO}$ [1] $0.5$ g N m <sup>-3</sup> $K_{APAO}$ Saturation coefficient for acetate $S_A$ [1]4g COD m <sup>-3</sup> $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ g N m <sup>-3</sup> $K_{PS}$ Saturation coefficient for phosphorus in storage[1] $0.2$ g P m <sup>-3</sup> $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1] $0.01$ g P m <sup>-3</sup> $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m <sup>-3</sup>	K <sub>O2PAO</sub>	Saturation/inhibition coefficient for oxygen	[1]	0.2	$g O_2 m^{-3}$
$K_{APAO}$ Saturation coefficient for acetate $S_A$ [1]4g COD m^{-3} $K_{NH4PAO}$ Saturation coefficient for ammonium (nutrient)[1]0.05g N m^{-3} $K_{PS}$ Saturation coefficient for phosphorus in storage of PP[1]0.2g P m^{-3} $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01g P m^{-3} $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.1mole HCO <sup>-3</sup> m^{-3}	K <sub>NO3PAO</sub>	Saturation coefficient for nitrate, $S_{\rm NO}$	[1]	0.5	$g N m^{-3}$
$K_{\rm NH4PAO}$ Saturation coefficient for ammonium (nutrient)[1] $0.05$ g N m <sup>-3</sup> $K_{\rm PS}$ Saturation coefficient for phosphorus in storage[1] $0.2$ g P m <sup>-3</sup> $K_{\rm PPAO}$ Saturation coefficient for phosphate (nutrient)[1] $0.01$ g P m <sup>-3</sup> $K_{\rm ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m <sup>-3</sup>	K <sub>APAO</sub>	Saturation coefficient for acetate $S_A$	[1]	4	$g \text{ COD } m^{-3}$
$K_{PS}$ Saturation coefficient for phosphorus in storage[1] $0.2$ $g$ P m^{-3} $K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1] $0.01$ $g$ P m^{-3} $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1] $0.1$ mole HCO <sup>-3</sup> m^{-3}	K <sub>NH4PAO</sub>	Saturation coefficient for ammonium (nutrient)	[1]	0.05	$\tilde{g} N m^{-3}$
$K_{PPAO}$ Saturation coefficient for phosphate (nutrient)[1]0.01 g P m^{-3} $K_{ALKPAO}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> )[1]0.1 mole HCO <sup>-3</sup> m^{-3}	K <sub>PS</sub>	Saturation coefficient for phosphorus in storage of PP	[1]	0.2	$g P m^{-3}$
$K_{\text{ALKPAO}}$ Saturation coefficient for alkalinity (HCO <sup>-3</sup> ) [1] 0.1 mole HCO <sup>-3</sup> m <sup>-3</sup>	KPPAO	Saturation coefficient for phosphate (nutrient)	[1]	0.01	$g P m^{-3}$
	KALKPAO	Saturation coefficient for alkalinity ( $HCO^{-3}$ )	[1]	0.1	mole $HCO^{-3}$ m <sup>-3</sup>

(Continued)

Item	Description	Ref.	20°c	Units
K <sub>PP</sub>	Saturation coefficient for poly-phosphate	[1]	0.01	$g X_{PP} g^{-1} X_{PAO}$
K <sub>MAX</sub>	Maximum ratio of $X_{PP}/X_{PAO}$	[1]	0.34	$g X_{PP} g^{-1} X_{PAO}$
$K_{\rm IPP}$	Inhibition coefficient for PP storage	[1]	0.02	$g X_{PP} g^{-1} X_{PAO}$
$K_{\rm PHA}$	Saturation coefficient for PHA	[1]	0.01	$g X_{PHA} g^{-1} X_{PAO}$

Table 4 (continued)

## 3.3. Model simulation of the biomass

The particulate component concentrations could be also calculated from model simulation as shown in Fig. 8 whereas the heterotrophic organism  $X_{H}$ ; phosphate accumulating organism  $X_{PAO}$ , and autotrophic microorganism X<sub>A</sub> concentrations in multi-tank AA/O activated sludge process were 638-1,204, 58.4-275, and 90-200.12 mg/L at run 1; 594.9-1321.4, 58.43-337.76, and 35-203.88 mg/L at run 2; 514.22-1,160, 58.42-271.13, and 95.5-208.6 mg/L at run 3; 534.26-1174.5, 58.42-272.5, and 89.72-185.36 mg/L at run 4. As result, The X<sub>H</sub>; X<sub>PAO</sub>; and X<sub>A</sub> decreased in the anaerobic tank because of the lysis reaction. Then the heterotrophic organism X<sub>H</sub>; phosphate accumulating organism X<sub>PAO</sub>; and autotrophic microorganism X<sub>A</sub> increased in the aerobic tanks due to aerobic growth. The heterotrophic organism X<sub>H</sub>; phosphate accumulating organism X<sub>PAO;</sub> and autotrophic microorganism X<sub>A</sub> increased in quantities by about 56, 36, and 74% in tank one due to change the environmental state condition from anaerobic to aerobic and decreased in quantities by about 20, 44, and 0.14% in tank three due to change the environmental state condition from aerobic to anoxic. The ratio of total nitrifying species to total active biomass was between 1 and 12% in multi-tank AA/O process. In this study, the disadvantages of the developed BNR processes were improved by reconfiguring the process without mixed liquor and sludge recirculation. This was done by configuring the process into five-tank with variable environmental state conditions, anaerobic/anoxic, aerobic, and settling conditions, in each tank to achieve optimum removal of phosphorus and nitrogen. In multi-tank AA/O process, the intake location changing of raw wastewater was also used to direct the influent into the anoxic zone as an external carbon source for denitrification process. So, the heterotrophic organism  $X_{H}$ ; phosphate accumulating organism  $X_{PAO}$ ; and autotrophic microorganism  $X_A$ decreased in the anoxic tank due to the dilution effect of the flow. In addition to the dilution effect of the influent, the X<sub>A</sub> also decreased due to the negative growth rate that resulted from lysis reaction in the anoxic tank. In full-scale wastewater treatment plant, the transient system behavior is of high practical importance since variations of composition, influent flow-rate as well as changes of operation prevent each real-world wastewater treatment plant from reaching the steady-state condition. Although the application of this ASM2d under steady state was validated in this study; the application in transient state can be implemented in the future study. In addition, the practical applications of the ASM2d model including plant optimization, controller layout, mathematical verification of the purification performance, and model-based state and parameter estimation should be taken into account in the future study.

# 4. Conclusions

The variation of pollutants COD,  $NH_4$ -N,  $NO_3$ -N, and  $PO_4$ -P in multi-tank AA/O activated sludge process could be modeled successfully using the activated sludge model No. 2d. The microbial kinetic behaviors in these testing four runs were analyzed based on ASM2d model. The results obtained in this study can be summarized as follows:

- (1) The effective removal efficiency of COD, NH<sub>4</sub>-N, TN, and TP at 89, 87.7, 73.6, and 83.7% were achieved, respectively, in multi-tank AA/O activated sludge process.
- (2) In this study, the growth rate constant of autotrophic organisms  $X_A$  and its yield coefficient value were 1.4 day<sup>-1</sup> and 0.14, respectively.
- (3) According to model simulation, the X<sub>H</sub>; X<sub>PAO</sub>; and X<sub>A</sub> concentrations 638–1,204, 58.4–275, and 90–200.12 mg/L at run 1, 594.9–1321.4, 58.43–337.76, and 35–203.88 mg/L at run 2, 514.22–1,160, 58.42–271.13, and 95.5–208.6 mg/L at run 3, 534.26–1174.5, 58.42–272.5, and 89.72–185.36 mg/L at run four in multi-tank AA/O activated sludge process.
- (4) According to simulation,  $X_{H}$ ;  $X_{PAO}$ ; and  $X_{A}$  decreased in the anaerobic tanks because of the lysis reaction. Then the  $X_{H}$ ;  $X_{PAO}$ ; and  $X_{A}$  increased in the aerobic tanks due to aerobic growth. The  $X_{H}$ ;  $X_{PAO}$ ; and  $X_{A}$  increased in quantities by about 56, 36, and 74% in tank one due to change in the environmental state condition from anaerobic to aerobic and decreased in quantities

by about 20, 44, and 0.14% in the tank three due to change in the environmental state condition from aerobic to anoxic. The ratio of total nitrifying species to total active biomass was between 1 and 12% in multi-tank AA/O process.

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