



Parametric study of an integrated organic Rankine/reverse Brayton refrigeration cycle and multiple-effect desalination unit

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ABSTRACT

This study explores the opportunity of a combined cooling, desalination, and power (CCDP) unit that is thermally driven using low- to mid-grade heat input of 1,940 kW_{th} (enthalpy of vaporization of steam at 200°C and mass flow rate of 1 kg/s). The proposed CCDP system is comprised of a Rankine cycle that partially drives a gas refrigeration cycle by means of shaft work and thermally drives a multiple-effect distillation (MED) unit by harnessing the rejected heat of condenser. Based on our thermodynamic model, the proposed CCDP system is more efficient from an energy-saving viewpoint compared with stand-alone systems that deliver the same services provided if there are ≥8 MED effects (units). Furthermore, the proposed polygeneration system is able to produce nearly 188 kW_e of electrical power output, 116 kW_{th} of cooling capacity, and 25.6 m³/h of freshwater capacity when water is employed as a working fluid and air as a refrigerant. In addition, the CCDP system attains an exergy efficiency of ≈42% and a primary energy-saving ratio of 28%. Because an organic Rankine cycle is promising for the conversion of low- and mid-grade heat to electricity, various organic working fluids are investigated. The results show that when propane is used instead of water, the freshwater capacity rises by 3.4%.

Keywords: Tri-generation; Polygeneration; Combined cooling and power; Combined cooling, heating, and power; Combined cooling; Desalination; Power

1. Introduction

A polygeneration system is an improved version of a cogeneration system in which more than two products are attained such as electricity, refrigeration, or freshwater. Combinations of different types of conventional and renewable energy sources such as fossil fuels or solar thermal energy can be leveraged together into one cycle that provides various services such as electricity, refrigeration, desalinated water, etc. Such systems are capable of ensuring high overall energy conversion efficiency with less environmental impact compared with conventional systems. Furthermore,

polygeneration systems are more effective than stand-alone systems in facing energy price demand fluctuations, which is mutually beneficial to both owners and end-users.

Freshwater demand has gradually increased due to the rapid growth of population and domestic, industrial, and agricultural use. Seawater desalination has been the main, if not only, source of clean water in regions where physical water scarcity is the main challenge [1]. Moreover, drought and desertification have been increasing dramatically in regions across the world for the past few years, resulting from deficiencies in surface and groundwater [2,3]. Refrigeration and air-conditioning demands are also anticipated to increase

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from the rise of global temperatures. Consequently, the environmental impact grows increasingly worse because many common refrigerants in use today pose a threat to the environment due to their global warming potential and ozone depletion potential [4].

In a recent review, Murugan and Horak [5] discussed the research efforts and developments that have been conducted regarding poly- and trigeneration, a subset of polygeneration in which three outputs are generated. They concluded that the selection of the energy conversion device, such as gas turbines and organic Rankine cycles (ORCs), and its size are extremely important for residential and industrial applications. The location of the polygeneration plant is a significant factor to determine the most desirable products. For instance, local climate would play a role in determining the plant configuration and its possible products for an off-grid plant. Thus, they recommended that feasibility studies should be carried out for the installation of a polygeneration system, because every system is different.

Anvari et al. [6] performed a thermoeconomical study on a combined cooling, heating, and power (CCHP) system that consists of three sections, namely, gas turbine and heat recovery steam generator (GT-HRSG), regenerative organic Rankine cycle (RORC), and absorption refrigeration cycle based on LiBr-H₂O. The result showed that adding an RORC and absorption refrigeration cycle to the GT-HRSG cycle increases the overall exergetic efficiency of the CCHP system by 2.5% and 0.75%, respectively, with a 5.5% and 0.45% increase in the total investment cost of the trigeneration cycle.

Ortega-Delgado et al. [7] performed a parametric study of a multiple-effect distillation (MED) unit with a steam ejector—widely known as multiple effect distillation with thermal vapor compression (MED-TVC)—coupled with a Rankine cycle (RC) power block. They studied the effect of the motive and suction steam pressures on the MED-TVC performance, freshwater capacity, and other key variables. They concluded that there is an optimum value of the heat transfer area of the evaporator after the suction point and optimum position of the steam ejector for every suction and motive steam pressure, respectively. When electricity demand is high, it was recommended to extract low-pressure motive steam and place the steam ejector close to the fifth effect in order to maximize the electric power production at the expense of the MED-TVC efficiency. On the other hand, extracting high-pressure motive steam from the RC turbine and locating the thermocompressor closer to the last effect is desirable when electricity demand is low to enhance the MED-TVC performance.

Mohan et al. [8] technically and economically examined the advantages of harnessing the excess waste heat from a gas turbine and rejected heat from a steam RC condenser in a combined power plant in the United Arab Emirates. The trigeneration system was optimized based on the cooling demands of the neighboring community to simultaneously produce electricity, freshwater using air gap membrane distillation, and cooling using LiBr-H₂O absorption refrigeration system. The proposed trigeneration system was projected to have an energy-conversion efficiency of about 83% compared with 51% for the combined cycle power plant with a payback period of only 1.4 years with cumulative net present value of \$66 million over the project lifetime.

Akbari et al. [9] analyzed the effect of the turbine inlet pressure and evaporator outlet temperature on a combined cooling, clean water, and power system from energy and exergy perspectives. The polygeneration system consists of a Kalina cycle¹, a LiBr-H₂O heat transformer, and a water desalination system using a geothermal hot water heat source at 124°C. The energy and exergy efficiencies of the system were found to be about 17% and 65%, respectively, with a maximum freshwater production of 1.32 m³/h. Sahoo et al. [10] studied the viability of coupling a hybrid solar-biomass power plant with cooling using an LiBr-H₂O absorption system and desalination using an MED system in a polygeneration process in India. It was found that the net equivalent power for a polygeneration system increases by 18.2% compared with a conventional power plant with stand-alone cooling and desalination systems.

Ameri and Jorjani [11] conducted exergy and economic analyses on an integrated system comprised of a Brayton cycle with a heat recovery steam generator (HRSG), an ORC, and an MED unit. The gas turbine exhaust energy is initially harnessed by the MED unit by means of employing a single-pressure HRSG before it drives the ORC. It was concluded that the optimum power and freshwater capacities are very sensitive to the MED evaporator approach temperature. Among three organic working fluids, R134a achieved the highest exergy efficiency.

Recently, Salimi and Amidpour [12] investigated the effect of the integration of different desalination systems on cogeneration system performance by utilizing the *R*-curve tool in order to identify the most effective way to decrease the operating cost. They found that the integration of thermally and electrically driven desalination units can result in either the improvement or impairment of the overall cogeneration efficiency based on the operating conditions of the cogeneration system. In particular, they demonstrated that the integration of a 17.8 MW_{th} MED unit could either provide 28.97 MW_{th} fuel savings or cause 47.84 MW_{th} excess fuel consumption.

We propose here a combined cooling, desalination, and power (CCDP) system that is comprised of Rankine power and gas refrigeration (reverse Brayton) cycles, plus a thermally driven desalination unit. This extends our previous introduction of a unit that produces shaft power and refrigeration, but not desalination [13]. The heat rejection from the condenser of the RC is exploited to drive the desalination unit that is based on MED technology. Primarily, our proposed CCDP system utilizes water and air as the working fluid and refrigerant, respectively, which are non-hazardous and environmental friendly with the aim of minimizing carbon emissions. The combined system is designed to be located by a large body of saltwater such as the ocean and to provide freshwater, refrigeration, and power on demand, which makes it potentially attractive to remote and off-grid areas.

¹ The Kalina cycle is a thermodynamic process that converts thermal energy into mechanical power. It uses a mixture of two fluids as working fluid in order to extract more heat from the heat source than a conventional Rankine cycle because heat addition takes place at varying temperature even during phase change.

2. System configuration

A schematic diagram of the proposed CCDP system is shown in Fig. 1. It can be observed from Fig. 1 that the RC's turbine is connected with the compressor, the turbine of the gas refrigeration cycle, and the generator through the same shaft in order to maximize the shaft power output. Nevertheless, this might not always be the case especially if the required cooling (refrigeration) load is irregular in which the gas refrigeration sub-cycle is preferably fed by electrical power via a generator that produces electricity from the Rankine power sub-cycle.

The MED subsystem consists of multiple effects (cells) in which salt and water are separated by vaporizing some of the water content. Flow is driven from cell to cell by maintaining successively decreasing pressure levels. A cascading flow of heat is driven from cell to cell by maintaining successively decreasing temperature levels, corresponding to the decrease in vapor–liquid equilibrium temperature with increasing brine salinity. Rejected heat via the RC's condenser is proposed to provide the required heat to the first effect of the MED desalination system. Note that the mass flow rate of the seawater in the MED unit (stream F) is determined from the rejected heat of the Rankine and reverse Brayton cycles to increase the seawater temperature of 27°C to the top brine (first effect) temperature of 66°C. Incoming seawater is first introduced to the MED subsystem (stream S) by condensing the steam in a final condenser, which is produced by

the last effect. Over 60% of incoming saltwater gets rejected back to the source (stream R) after exchanging heat with the MED's condenser, while the rest is pumped to the first effect (stream F). On its way to the first effect, saltwater is preheated by the gas refrigeration cycle (between points 6 and 7) and partially condenses the steam generated in each effect.

Following the stream labels in Fig. 2, the brine stream (BC_{i-1}) from the preceding effect flashes as it is introduced to the effect (i) because it is superheated at the effect's operating pressure. The remaining brine (BF_i) is then sprayed over a bundle of evaporation tubes, where steam is generated and the rest of the brine stream (BC_i) goes to the succeeding effect. The circulating steam inside the tubes (VM_{i-1}), from the preceding steam mixer, provides the heat needed for evaporation. The generated steam gets partially condensed (LP_i) by preheating incoming seawater (swP_{i+1}), while the rest of the steam (vP_i) is transported to provide the heat needed for the following effect.

3. Mathematical modeling

The mathematical model of our proposed CCDP system is based on a combined model of three separate thermodynamic models, namely, the Rankine power cycle, the gas refrigeration (reverse Brayton) cycle, and the MED desalination unit. Initially, each subsystem was modeled and validated separately before integrating them with each other to form our proposed CCDP system in Fig. 1. The following

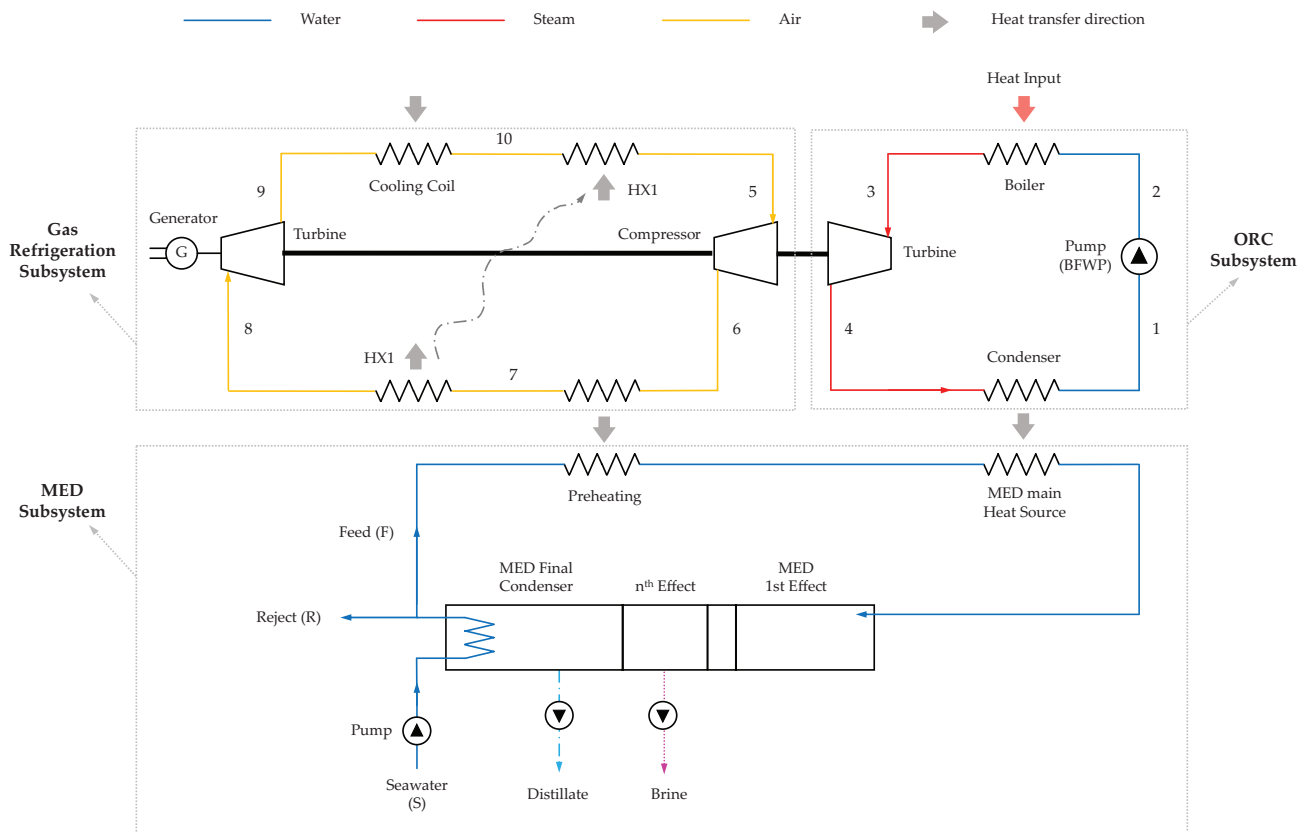


Fig. 1. Schematic diagram of the combined cooling, desalination, and power (CCDP) system.

combined system compared with the energy consumption of the reference separate systems [20–22], and is expressed as follows:

$$PESR = \left(\frac{F_s - F_c}{F_s} \right) \times 100\% = \left(1 - \frac{F_c}{F_s} \right) \times 100\% \quad (3)$$

where F_s and F_c are the fuel energy consumption for the separate reference and combined systems, respectively.

Fig. 3 depicts the energy flows of the proposed CCDP system, while Fig. 4 shows the reference stand-alone cooling, desalination, and power systems. Thus, the fuel energy consumptions F_s and F_c can be expressed as follows:

$$F_c = \frac{\dot{Q}_{hs}}{\eta_b} \quad (4)$$

$$F_s = F_{grid} + F_b \quad (5)$$

where \dot{Q}_{hs} is the rate of main heat source input, η_b is the boiler efficiency, F_{grid} is the electricity consumed from the electrical grid, and F_b is the fuel consumption associated with the stand-alone MED unit, and can be calculated based on Fig. 4 as follows:

$$F_{grid} = \frac{W_{ele}}{\eta_{grid}} + \frac{\dot{Q}_{cool}}{COP_{ref} \times \eta_{grid}} \quad (6)$$

where η_{grid} and COP_{ref} represent an average power plant efficiency with a constant value of 33% and cooling coefficient of performance (COP) with a value of 4.5 as in large-capacity vapor-compression chillers at standard conditions, respectively [21]:

$$F_b = \frac{\dot{Q}_{MED,input}}{\eta_b} \cdot \frac{PR}{PR_{ref}} \quad (7)$$

$$PR = \frac{\dot{m}_{Distilled} \cdot h_{fg}}{\dot{Q}_{MED,input}} \quad (8)$$

where PR is the performance ratio of the MED unit which is defined as the mass of desalinated water produced ($\dot{m}_{distilled}$ in kg/s) per thermal energy input ($\dot{Q}_{MED,input}$ in kW_{th}) which is equal to the heat rejected by the RC's condenser. h_{fg} is the enthalpy of vaporization of H_2O at $73^\circ C$ which corresponds to 2326 kJ/kg, and PR_{ref} represents the performance ratio reference with a constant value of 10 [23,24]. It is worth noting that the proposed CCDP system cannot save energy when the PESR value is negative compared with the stand-alone reference systems.

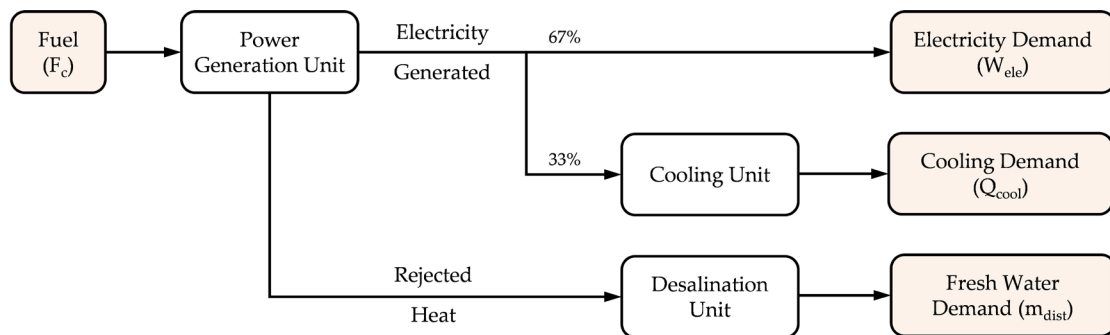


Fig. 3. Energy flows of the proposed CCDP system.

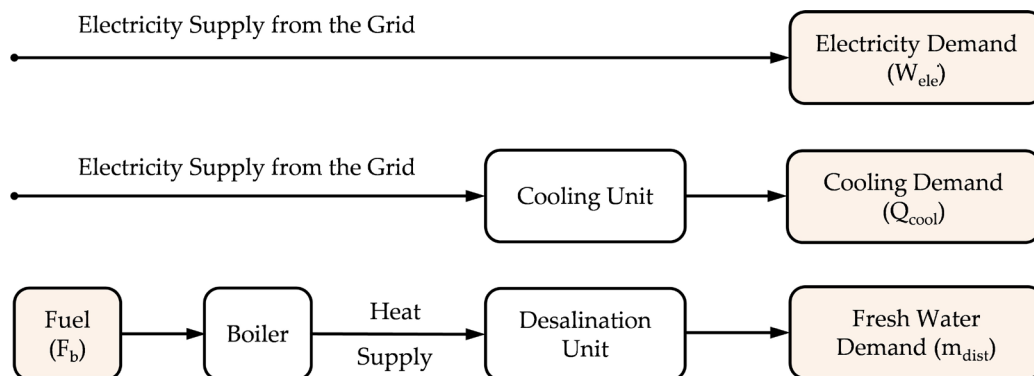


Fig. 4. Energy flows of the reference separate CCDP systems.

Table 1
Main operating condition assumptions for the CCDP system

Parameter	Value	Unit
Rankine cycle		
Temperature (T_3)	200	°C
Boiler saturation temperature	170	°C
Condenser saturation temperature	70	°C
Gas refrigeration cycle		
Low pressure	70	kPa
Pressure ratio	2.5	
Heat exchanger 1 (regenerator) effectiveness	60	%
Temperature (T_{10})	15	°C
MED		
MED number of effects	14	Effects
Top brine (first effect) temperature	66	°C
Temperature rise of seawater in preheater (dT)	2.3	°C
Pressure difference between the effects of MED (dP)	1	kPa
Seawater temperature	27	°C
Seawater salinity	35,000	ppm
Others		
\dot{m}_{hs}	1	kg/s
\dot{Q}_{hs} (steam at 200°C) rate of heat source input per unit mass	1,940	kJ/kg
Cooling ratio	33	%
Shaft efficiency	95	%
Turbine isentropic efficiency (η_t)	85	%
Pump isentropic efficiency (η_p)	85	%
Compressor isentropic efficiency (η_c)	80	%
Boiler efficiency (η_b)	85	%
Ambient temperature (T_o)	35	°C
Natural gas price	1.9	\$/MMBtu

The Rankine power, gas refrigeration cycles, MED unit, and aforementioned equations are solved simultaneously for steady operating conditions (fluid states and mass, energy, and exergy flows) based on the assumptions shown in Table 1. The thermodynamic properties of water, air, helium, carbon dioxide, etc. are calculated at each point in the system by calling on engineering equation solver routines.

3.3. Model validation

The mathematical model was validated by comparing the RC, ORC, and gas refrigeration cycles individually and independently with the related work in the literature [14,15,25–28]. The obtained results of all individual models were within $\pm 0.5\%$ MED same reference conditions. Table 2 demonstrates the MED single model validation by showing good agreement with the related work in literature [16,29–31] under the same operating conditions of the references.

Table 2
Validation of the MED model

	Current model	Reference	Difference (%)
Freshwater production (kg/h) [16]	2,897	2,992	3.2
Exergy efficiency [32]	6.2	6.0	3.3
Performance ratio [16]	9.25	9.6	3.6

4. Results and discussion

Figs. 5–9 depict the impact of input parameter variations such as the gas refrigeration sub-cycle's pressure ratio, the Rankine sub-cycle's condenser temperature (T_1), the heat exchanger (regenerator) effectiveness (ϵ_{HX1}), and the MED number of effects. Exergy efficiency (η_{exergy}), electrical power, cooling capacity, freshwater capacity, and PESR are considered to compare the energy consumption and system productivity. PESR is used to compare the proposed CCDP system with the stand-alone reference systems from an energy-savings point of view. Although the results discuss three different refrigerants, namely air, helium, and carbon dioxide, the electrical power output, cooling capacity, and water production are only shown for air because the same pattern is anticipated. It is worth noting that the study is conducted at a fixed thermal energy input rate of 1940 kW_{th}, which corresponds to the value of enthalpy of vaporization of water at 200°C at 1 kg/s mass flow rate.

4.1. Sensitivity to the pressure ratio (r_p)

Fig. 5(a) shows that the exergy efficiency of the CCDP system increases significantly before it levels off as the pressure ratio increases. It can be observed that the exergy efficiency of the combined system only peaks when helium (He) is used as a refrigerant at a pressure ratio of 3.5. Fig. 5(b) demonstrates the effect of pressure ratio on electrical power output, cooling capacity, and water production when air is used as a refrigerant. At a pressure ratio of about 1.5, the gas refrigeration sub-cycle reaches its optimum operating point (maximum COP) as reflected by the cooling capacity in Fig. 5(b) with only a negligible decrease in the electrical power capacity (to the point that cannot be observed in the figure). Consequently, the rise in the rejected heat by the gas refrigeration sub-cycle leads to an increase in the heat absorption by the MED unit, which increases the freshwater production capacity. Because the electrical power output is constant with respect to the pressure ratio, the PESR is directly dependent on the cooling capacity. Fig. 5(c) shows that the PESR of the CCDP system peaks where the gas refrigeration sub-cycle COP peaks for different refrigerants. Unlike a conventional stand-alone cooling cycle, such a combined system is potentially attractive for industrial applications that require freshwater, power, and refrigeration (cryogenics) where very low temperatures are desirable, as shown in Fig. 5(d), without sacrificing the overall system performance and productivity.

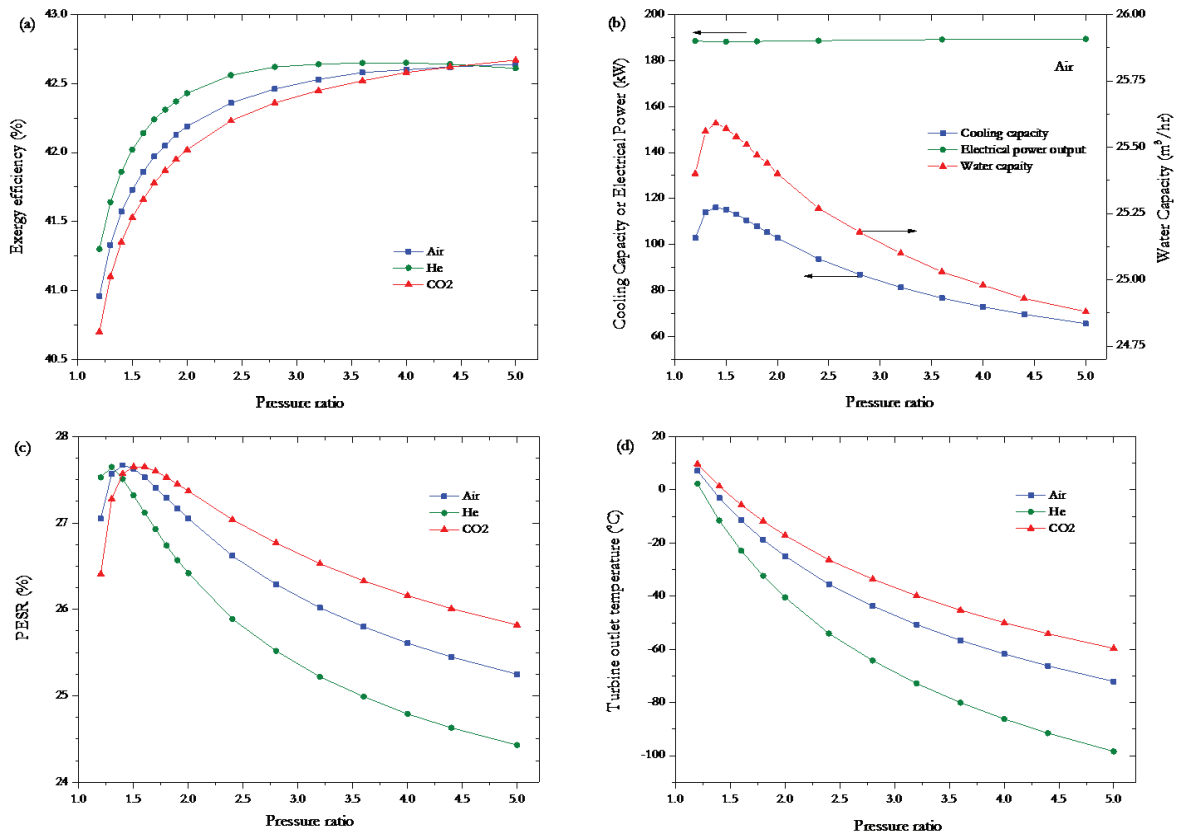


Fig. 5. Effect of the pressure ratio (r_p) of the gas refrigeration sub-cycle on (a) exergy efficiency, (b) electrical power, cooling capacity, and water production, (c) PESR, and (d) gas turbine outlet temperature (T_t) of the proposed CCDP system for different refrigerants (air, He, and CO₂).

4.2. Sensitivity to the Rankine sub-cycle condenser temperature (T_c)

The exergy efficiency of the CCDP system decreases significantly as the condenser temperature (T_c) of the Rankine sub-cycle increases as shown in Fig. 6(a). When air is employed as a refrigerant, the electrical power output increases remarkably as the condenser temperature decreases as depicted in Fig. 6(b). Moreover, since our baseline model assumes that one third of the produced shaft power is used to drive the gas refrigeration cycle, the cooling capacity increases as the electrical power output increases (condenser temperature decreases). Thus, the PESR rises notably as the electrical power output and cooling capacity increases (condenser temperature decreases) as shown in Fig. 6(c). At the same condenser temperature and pressure ratio, the PESR associated with helium is the lowest due to the low output gas turbine temperature. The freshwater production increases marginally with increasing condenser temperature.

4.3. Sensitivity to the reverse Brayton cycle regenerator effectiveness (ϵ_{HX1})

For the reason that the refrigerant leaves the cooling coil at relatively low temperature and is highly desirable to enter the gas turbine at low temperature, a heat exchanger

(regenerator) is vital to recover the cool refrigerant internally. Fig. 7(a) shows that as the regenerator effectiveness increases, the exergy efficiency slightly increases. It can be observed that the exergy efficiencies for different refrigerants are larger at lower regenerator effectiveness, converge as ϵ_{HX1} increases. As the regenerator effectiveness rises, the electrical power output remains constant, while cooling and freshwater capacities increase slightly as shown in Fig. 7(b). Likewise, the PESR increases with increasing regenerator effectiveness in which the growth differs from only a minor effect when CO₂ is employed to none when He is used as shown in Fig. 7(c). Even though the regenerator effectiveness has a slight effect on cooling capacity regardless of the refrigerant type, the PESR is more sensitive to the water production, which is the case when carbon dioxide is used due to the higher heat rejected which is eventually absorbed by the MED unit.

4.4. Sensitivity to the cooling ratio

Based on the type of application, electrical power and cooling demands fluctuate during the day and time of the year which makes control of any polygeneration system very important. Our proposed CCDP system allows the cooling subsystem (gas refrigeration sub-cycle) to be connected or disconnected easily. Therefore, we define the cooling ratio as the fraction of the electrical power consumed by the gas

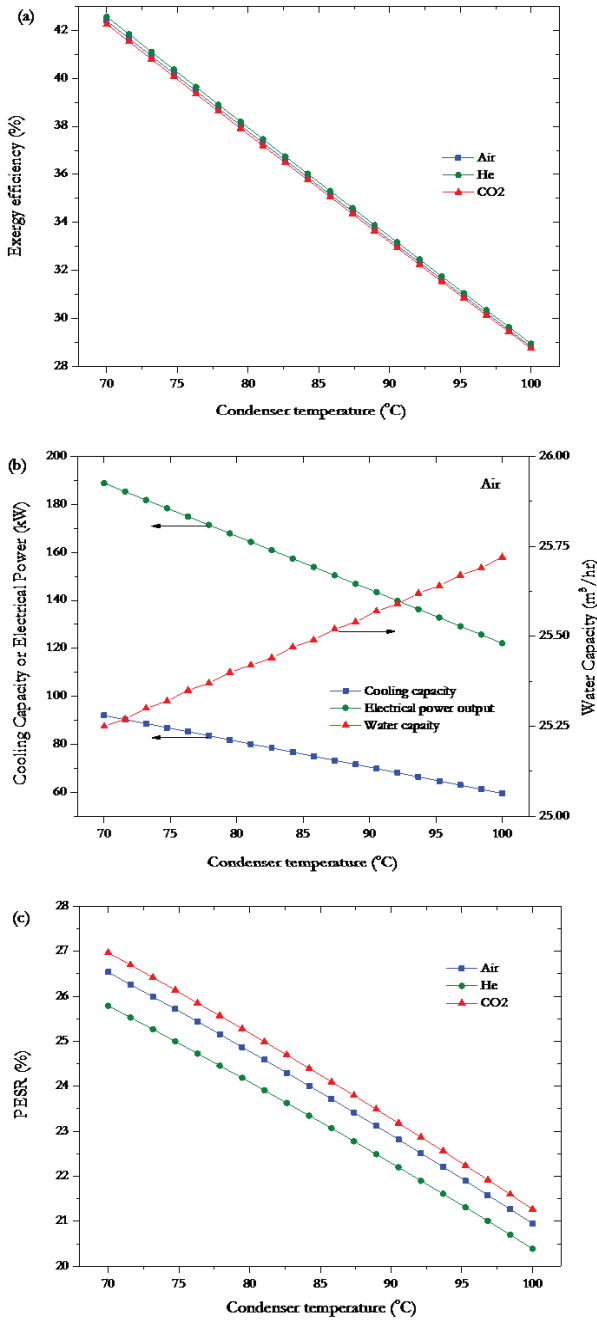


Fig. 6. Effect of the Rankine sub-cycle condenser temperature (T_1) on (a) exergy efficiency, (b) electrical power, cooling capacity, and water production, and (c) PESR of the proposed CCDP system for different refrigerants (air, He, and CO₂).

refrigeration sub-cycle to the total electrical power produced by the Rankine power sub-cycle. Fig. 8(a) shows that the exergy efficiency decreases steeply from about 55% when zero cooling is generated to about 15% when zero electrical power is generated. When air is employed as a refrigerant, the CCDP system is capable of generating between 290 kW_e of electrical power output and 22 m³/h of freshwater production at a cooling ratio = 0. On the other hand, the CCDP system can

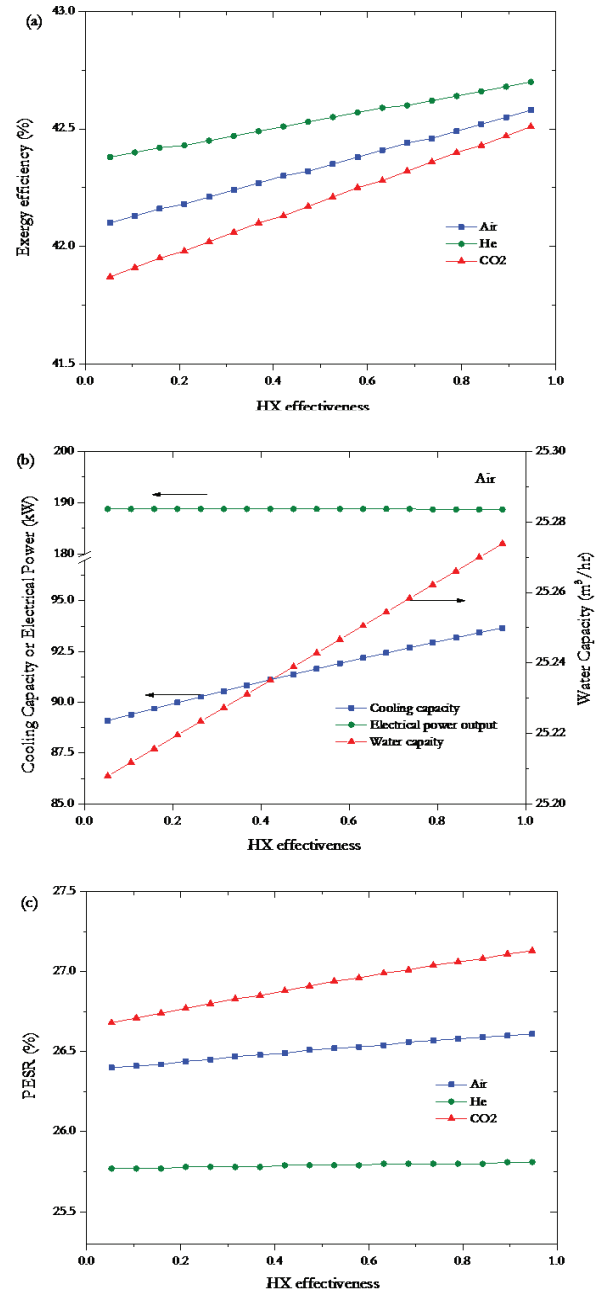


Fig. 7. Effect of the reverse Brayton cycle heat exchanger (regenerator) effectiveness (ϵ_{HX1}) on (a) exergy efficiency, (b) electrical power, cooling capacity, and water production, and (c) PESR of the proposed CCDP system for different refrigerants (air, He, and CO₂).

produce about 275 kW_{th} of cooling and 30 m³/h of freshwater at a cooling ratio = 1, as shown in Fig. 8(b). Furthermore, the PESR decreases as the cooling ratio increases, as shown in Fig. 8(c), at different decreasing (negative) rates of change based on the type of refrigerant. Similar to the last case, the PESR is a strong function of water capacity, which changes as the heat rejected by the gas refrigeration sub-system is absorbed by the MED preheating process.

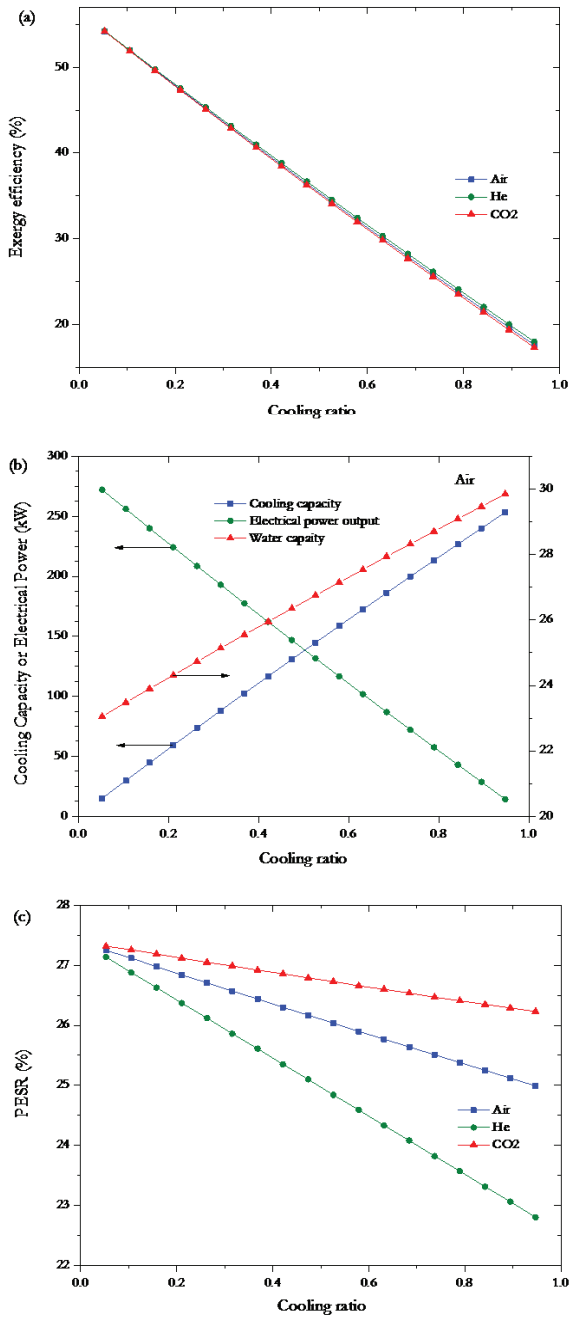


Fig. 8. Effect of the cooling ratio on (a) exergy efficiency, (b) electrical power, cooling capacity, and water production, and (c) PESR of the proposed CCDP system for different refrigerants (air, He, and CO₂).

4.5. Sensitivity to the MED number of effects

Fig. 9(a) depicts that the exergy efficiency sharply decreases as the MED number of effects increases due to the high exergy destruction associated with required pumping system compared with the exergy saved by the MED unit. Nevertheless, the freshwater capacity increases significantly as the MED number of effects increases as shown in Fig. 9(b). Consequently, the PESR increases as the freshwater

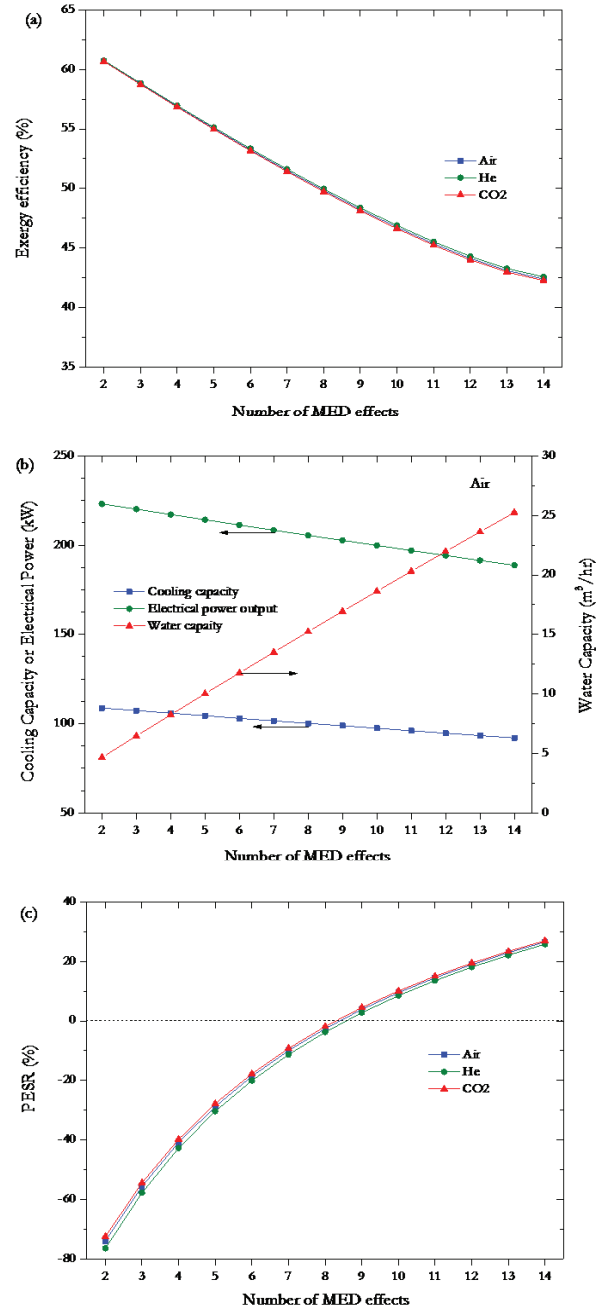


Fig. 9. Effect of the MED number of effects on (a) exergy efficiency, (b) electrical power, cooling capacity, and water production, and (c) PESR of the proposed CCDP system for different refrigerants (air, He, and CO₂).

production increases (MED number of effects increases) as shown in Fig. 9(c). The CCDP system becomes feasible from an energy perspective when the MED number of effects exceeds eight effects (units), which proves that the PESR is a strong function of water production by the MED unit. The reduction of the electrical power output, as the MED number of effects increases, is due to the electrical power consumption associated with the required pumping system, which leads to a reduction in the cooling capacity as well.

4.6. Sensitivity to the Rankine sub-cycle working fluid

Unlike the conventional steam RC, an ORC uses working fluids that are suitable for converting low-temperature heat into electricity [33]. In our case, using an ORC instead of a conventional steam RC is more desirable due to one major advantage: the slope of the saturated vapor curve (right curve of the dome) is almost vertical. Consequently, there is no need for superheating or reheating the vapor before the turbine inlet because the vapor quality problem at the turbine outlet does not exist in the ORC [34]. Under the main assumptions listed in Table 1 (except pressure ratio = 1.4), Table 3 shows a comparison of our proposed CCDP system using different combinations of working fluids and refrigerants for the Rankine sub-cycle and gas refrigeration sub-cycle, respectively. It can be observed from Table 3 that the CCDP system that employs water and air as working fluid and refrigerant, respectively, attains the highest cooling capacity of 116.1 kW_{th} and PESR of 27.7%. Similarly, the CCDP system with water and helium (He) produces the maximum exergy efficiency of 41.9%. In the same way, the highest water production of 26.6 m³/h is achieved by the CCDP system that uses propane as the ORC working fluid due to the low ORC efficiency (highest heat rejection by the condenser).

4.7. Economic impact of the polygeneration system

For the sake of a simple economic analysis, thermal energy is assumed to be supplied to both the combined and stand-alone systems by burning natural gas. The annual fuel savings is calculated as follows and results for different working fluids are shown in the last column of Table 3:

$$AFS = \frac{C_f \cdot PSRE \cdot F_s \cdot AOH \cdot (3600s / hr)}{HHV \cdot \rho_{fuel}} \quad (9)$$

where C_f (\$/m³) is the fuel specific cost, AOH is annual operation hours (assuming 24 h per day, and 345 d per year), HHV (kJ/kg) is the higher heating value in, and ρ_{fuel} (kg/m³) is the fuel density [35]. It can be seen from Table 3 that when water and air are used as working fluids, for instance, the proposed CCDP system can save \$502/year per unit kW_{th} heat input compared with stand-alone systems. Alelyani et al. [18] estimated the total annual costs of an MED unit with matching water capacity to be \$1.05M/year. Accordingly, our proposed CCDP system is capable of cutting the total annual costs by almost 93% compared with a stand-alone MED unit when water and air are used as a working fluid and refrigerant, respectively.

5. Conclusions

This paper proposes the opportunity of a CCDP system based on the Rankine and gas refrigeration (reverse Brayton) cycles, and MED water desalination unit. The proposed CCDP system harnesses heat rejection by the RC condenser to drive the desalination unit and part of the shaft work to drive the gas refrigeration cycle. At a fixed thermal energy input of 1940 kW_{th} (via steam at 200°C), our thermodynamic

Table 3 Comparison of the proposed CCDP system using different working fluid combinations

Power cycle working fluid	Cooling cycle refrigerant	Power cycle efficiency (%)	Cooling cycle COP	T _o (°C)	Exergy efficiency (%)	Power capacity (kW _e)	Cooling capacity (kW _{th})	Water capacity (m ³ /h)	PESR (%)	Annual fuel savings per unit heat input ((\$/kW _{th})/year)
Water ^a	Air	17.8	1.25	-3.0	41.6	188.2	116.1	25.6	27.7	502
Water ^a	CO ₂	17.8	1.23	1.4	41.4	188.3	114.0	25.6	27.6	500
Water ^a	He	17.8	1.22	-11.6	41.9	188.3	112.8	25.5	27.5	498
R123 ^b	Air	14.1	1.25	-3.0	35.3	139.9	86.3	25.8	23.5	426
R123 ^b	CO ₂	14.1	1.23	1.4	35.1	139.9	84.8	25.8	23.4	424
R123 ^b	He	14.1	1.22	-11.6	35.5	140.0	83.9	25.8	23.4	424
Isopentane ^a	Air	12.7	1.25	-3.0	32.0	121.5	75.0	25.9	21.8	395
Isopentane ^a	CO ₂	12.7	1.23	1.4	31.9	121.5	73.6	25.9	21.7	393
Isopentane ^a	He	12.7	1.22	-11.6	32.2	121.6	72.8	25.9	21.7	393
R245fa	Air	11.8	1.25	-3.0	30.9	109.6	67.6	26.0	20.6	373
R245fa	CO ₂	11.8	1.23	1.4	30.7	109.6	66.4	26.0	20.6	373
R245fa	He	11.8	1.22	-11.6	31.1	109.6	65.7	26.0	20.5	371
Isobutene	Air	11.2	1.25	-3.0	29.6	101.6	62.7	26.0	19.8	359

(continued)

Table 3 (continued)

Power cycle working fluid	Cooling cycle refrigerant	Power cycle efficiency (%)	Cooling cycle COP	T_g (°C)	Exergy efficiency (%)	Power capacity (kW _e)	Cooling capacity (kW _{th})	Water capacity (m ³ /h)	PESR (%)	Annual fuel savings per unit heat input ((\$/kW _{th})/year)
Isobutene	CO ₂	11.2	1.23	1.4	29.4	101.7	61.6	26.0	19.8	359
Isobutene	He	11.2	1.22	-11.6	29.8	101.7	60.9	26.0	19.7	357
R134a	Air	5.9	1.25	-3.0	16.5	32.6	20.1	26.4	12.2	221
R134a	CO ₂	5.9	1.23	1.4	16.4	32.6	19.8	26.4	12.2	221
R134a	He	5.9	1.22	-11.6	16.5	32.6	19.5	26.4	12.2	221
Propane	Air	5.0	1.25	-3.0	13.6	21.1	13.0	26.5	10.8	201
Propane	CO ₂	5.0	1.23	1.4	13.6	21.1	12.8	26.5	10.8	201
Propane	He	5.0	1.22	-11.6	13.7	21.1	12.6	26.5	10.8	201

^aORC boiler pressure is at critical pressure

model shows that the proposed CCDP system is more feasible from an energy-saving perspective when the MED number of effects is more than eight effects (units) compared with separate systems that provide the same services. When water and air are utilized as a working fluid and refrigerant, respectively, the CCDP system is capable of generating around 188 kW_e of electrical power output, 116 kW_{th} of cooling capacity, and 26 m³/h freshwater capacity for steam at 200°C and a mass flow rate of 1 kg/s. Additionally, the proposed polygeneration system can achieve an exergy efficiency and PESR of approximately 42% and 28%, respectively. Furthermore, we also explored replacing the conventional steam Rankine sub-cycle with an ORC with the aim of using other working fluids that are suitable for converting low-temperature heat into electricity. The results show that working fluids with the lowest ORC energy efficiency produce slightly more freshwater due to the high heat rejection rate. Additionally, employing helium as a refrigerant instead of air allows the CCDP system to achieve the lowest turbine outlet temperature and highest exergy efficiency.

Symbols

- CCDP — Combined cooling, desalination, and power
- COP — Coefficient of performance
- F — Fuel
- MED — Multiple-effect distillation
- ORC — Organic Rankine cycle
- PESR — Primary energy-saving ratio, %
- dP — Pressure difference between the effects of MED, kPa
- dT — Temperature rise of seawater in preheater, °C
- E — Exergy flow rate, kW
- h — Specific enthalpy, kJ/kg
- h_{fg} — Enthalpy of vaporization, kJ/kg
- ṁ — Mass flow rate, kg
- P — Pressure, kPa
- Q̇ — Heat flow rate, kW
- s — Specific entropy, kJ/kg K
- T — Temperature, °C
- W — Power, kW
- x — Water salinity, ppm

Greek

- η — Efficiency, %

Subscripts

- b — Boiler
- B — brine stream
- c — Combined
- C — Cell (effect)
- con — Condenser
- cool — Cooling
- D — Demister
- Dist — Distilled
- ele — Electrical
- eva — Evaporator
- ex — External surface of the bundle evaporation tubes
- F — Flash

HX	—	Heat exchanger
hs	—	Heat source
<i>i</i>	—	Effect number
L	—	Water saturated liquid
M	—	Mixer
min	—	Minimum
o	—	Dead state
P	—	Preheater
ref	—	Reference
rej	—	Rejected seawater
s	—	Separate
th	—	Thermal
v	—	Water saturated vapor

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Appendix A

With reference to Fig. 2, the mass and energy balance equations of the MED unit are derived and listed as follows.

A. The flash

$$\dot{m}_{BC_{i-1}} = \dot{m}_{BF_i} + \dot{m}_{vF_i} \quad (A1)$$

$$\dot{m}_{BC_{i-1}} x_{BC_{i-1}} = \dot{m}_{BF_i} x_{BF_i} + \dot{m}_{vF_i} x_{vF_i} \quad (A2)$$

$$\dot{m}_{BC_{i-1}} h_{BC_{i-1}} = \dot{m}_{BF_i} h_{BF_i} + \dot{m}_{vF_i} h_{vF_i} \quad (A3)$$

where \dot{m} is the mass flow rate, x is the water salinity in the flash, i is the effect number, B is the brine stream, C is the cell (effect), F is the flash, and v is the freshwater saturated vapor.

B. The MED evaporator

$$\dot{m}_{BF_i} = \dot{m}_{BC_i} + \dot{m}_{vex_i} \quad (A4)$$

$$\dot{m}_{vM_{i-1}} = \dot{m}_{LE_i} + \dot{m}_{vE_i} \quad (A5)$$

$$\dot{m}_{BF_i} x_{BF_i} = \dot{m}_{BC_i} x_{BC_i} \quad (A6)$$

$$\dot{m}_{vM_{i-1}} h_{vM_{i-1}} - \dot{m}_{LE_i} h_{LE_i} - \dot{m}_{vE_i} h_{vE_i} = \dot{m}_{vex_i} h_{vex_i} + \dot{m}_{BF_i} h_{BF_i} - \dot{m}_{BC_i} h_{BC_i} \quad (A7)$$

where ex and E represent the external and internal surfaces of the bundle evaporation tubes, respectively; L the freshwater saturated liquid; M the mixer; and D the demister.

C. The demister

$$\dot{m}_{vex_i} + \dot{m}_{vF_i} = \dot{m}_{vD_i} \quad (A8)$$

$$\dot{m}_{vex_i} h_{vex_i} + \dot{m}_{vF_i} h_{vF_i} = \dot{m}_{vD_i} h_{vD_i} \quad (A9)$$

D. The preheater

$$\dot{m}_{vD_i} = \dot{m}_{vP_i} + \dot{m}_{LP_i} \quad (A10)$$

$$\dot{m}_{swP_i} = \dot{m}_{swP_{i+1}} \quad (A11)$$

$$\dot{m}_{swP_i} h_{swP_i} - \dot{m}_{swP_{i+1}} h_{swP_{i+1}} = \dot{m}_{vD_i} h_{vD_i} - \dot{m}_{vP_i} h_{vP_i} - \dot{m}_{LP_i} h_{LP_i} \quad (A12)$$

where P represents the preheater, and SW the seawater feed.

E. The vapor mixer

$$\dot{m}_{vM_i} = \dot{m}_{vP_i} + \dot{m}_{vE_i} \quad (A13)$$

$$\dot{m}_{vM_i} h_{vM_i} = \dot{m}_{vP_i} h_{vP_i} + \dot{m}_{vE_i} h_{vE_i} \quad (A14)$$

F. The liquid mixer

$$\dot{m}_{Distilled_i} = \dot{m}_{LE_i} + \dot{m}_{LP_{i-1}} + \dot{m}_{Distilled_{i-1}} \quad (A15)$$

$$\dot{m}_{Distilled_i} h_{Distilled_i} = \dot{m}_{LE_i} h_{LE_i} + \dot{m}_{LP_{i-1}} h_{LP_{i-1}} + \dot{m}_{Distilled_{i-1}} h_{Distilled_{i-1}} \quad (A16)$$

where “Distilled” represents the distilled water in liquid form.

G. The MED condenser

$$\dot{m}_{vM_n} = \dot{m}_{LCon} \quad (A17)$$

$$\dot{m}_{sw} = \dot{m}_{sw,rej} + \dot{m}_{swP_n} \quad (A18)$$

$$\dot{m}_{vM_n} h_{vM_n} - \dot{m}_{LCon} h_{LCon} = \dot{m}_{sw,rej} h_{sw,rej} + \dot{m}_{swP_n} h_{swP_n} - \dot{m}_{sw} h_{sw} \quad (A19)$$

where $LCon$ represents the condensate water vapor in the condenser, rej the rejected seawater, and n the total number of effects.

H. MED system minimum work

The minimum separation work, or least amount of work to separate salt and water, is given by Eq. (A20) [30,32]:

$$\dot{W}_{min} = \dot{E}_{Brine} + \dot{E}_{product} - \dot{E}_{incoming\ SW} = \dot{E}_{BC_n} + \dot{E}_{Distilled_n} + \dot{E}_{LCon} - \dot{E}_{sw} \quad (A20)$$

where \dot{E} is the exergy rate and can be calculated using Eq. (2).